

PRACTICAL ASTRONOMY,  
IN THE  
DESCRIPTION and USE  
OF BOTH  
GLOBES,  
ORRERY  
AND  
TELESCOPES.

Wherein the most useful Elements,  
and most valuable modern Discoveries of the  
true ASTRONOMY are exhibited, after a  
very easy and expeditious Manner, in an exact  
Account of Our SOLAR SYSTEM, with  
Ten curious Copper-Plates.

Collected from the best AUTHORS, as Dr.  
HALLET, KEIL, HARRIS, GORDON, &c. For the  
USE of YOUNG STUDENTS.

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By SAMUEL FULLER.

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The Works of the Lord are Great, sought out of all them that have  
Pleasure therein, Psal. cxi. 2.

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the Globe in Meath-Street, 1732.

# PRACTICAL ASTROLOGY

317 M.J.

## Description and Use

H T G H I A O

A circular library stamp from the British Museum Library. The outer ring contains the text "BRITISH MUSEUM LIBRARY" at the top and "LONDON" at the bottom. The inner circle features a heraldic shield with four quadrants, each containing a different symbol. Below the shield, the date "15" is on the left and "FEB" is on the right, with the year "68" at the bottom.



To continue Chloro-Phenol.  
Accordance of our Solvent Experiments with  
that of any chlorinated Monomer in the case of  
that Aromatic Monomer the explosive effect is  
very strong. It is also observed that the  
Chloro-Phenol Experiments are very similar to those  
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COLLEGE OF FINE ARTS LIBRARY  
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word inde made up by two regiments, and the men brought into the garrison at  
the fort, 1812, and did not leave it.

KIDS UK

*Geodes in the granite*

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THE  
DESCRIPTION and USE  
OF THE  
CELESTIAL and TERRESTRIAL  
GLOBES.

**A** *Globe or Sphere* is a round solid Body, having every Part of its Surface equally distant from a Point within it, called its *Center*; and it may be conceived to be formed by the Revolution of a Semicircle round its Diameter.

Any Circle passing through the Center of the Sphere, thereby dividing it into two equal Parts or Segments, is called a *Great Circle*; and the Segments of the Sphere so divided, are called *Hemispheres*.

*Sphere or Globe.*

*Great Circle.*

*Hemispheres.*

Every Great Circle has its Poles and Axis.

The *Poles* of a Great Circle, are two Points on the Surface of the Sphere diametrically opposite to one another, and every where equally distant from the said Circle.

*Poles.*

The *Axis* of a Circle is a right Line passing through the Center of the Sphere, and through the Poles of the said Circle; and is therefore perpendicular to the Plane thereof.

*Axis.*

All Circles passing through the Poles of any great Circle, intersect it in two Places diametrically opposite, and also at right Angles; and with respect to the *Secundaries*, said Great Circle, they may be called its *Secundaries*.

*All*

## The Description and Use

*Parallel or lesser Circles.*

All Circles dividing the Sphere into two unequal Parts, are called *lesser* or *parallel Circles*, and are usually denominated by that Great Circle, to which they are parallel.

The Earth being globular, its outward Parts, as the several Countries, Seas, &c. are best, and most naturally represented upon the Superficies of a Globe; and when such a Body has the outward Parts of the Earth and Sea delineated upon its Surface, and placed in their natural Order and Situation, it is called a *Terrestrial Globe*.

The Celestial Bodies appear to us as if they were all placed in the same Concave Sphere; therefore Astronomers place the Stars according to their respective Situations and Magnitudes; and also the Images of the Constellations, upon the external Surface of a Globe; for it answers the Purposes as if they were placed within a concave Sphere, if we suppose the Globe to be transparent, and the Eye placed in the Center. A Globe having the Stars placed upon its Surface, as above described, is called a *Celestial Globe*. These Globes are both placed in Frames, with other Appurtenances, as shall be described in a proper Place.

*The principal Uses of the Globes* (besides their serving as *Maps* to distinguish the outward Parts of the Earth, and the Situations of the fixed Stars) is to explain and resolve the Phænomena arising from the diurnal Motion of the Earth round its Axis.

It is agreed on by the modern Mathematicians, that the Distance of the Earth from the Sun, is no more than a Point, when compared with the immense Distance of the fixed Stars;

*There will be the same Prospect of the fixed Stars, whether the Spectator be placed on the Earth or in the Sun.* therefore let the Earth be in what Point soever of her Orbit, there will be the same Prospect of the Heavens, as a Spectator would observe, did he reside in the Sun: And if several Circles be imagined to pass thro' the Center of the Earth, and others, parallel to them, be conceived to pass thro' the Center of the Sun, these Circles in the Heavens will seem to coincide, and to pass exactly thro' the same Stars. Wherefore as to the Appearances of the fixed Stars, it is indifferent whether the Earth or the Sun be made the Center of the Universe. But because it is from the Earth that we always observe the Celestial Bodies, and their apparent Motions seem to us to be really made in the Heavens, it is more natural in explaining the Phænomena arising from these Motions, to place the Earth in the Center. And again, because the Semidiameter of the Earth, when compared to her Distance



## Sect I. of the GLOBES. 3

Distance from the Sun, is of no sensible Magnitude, any Point upon the Earth's Surface, let her be in what Part soever of her Orbit, may be considered as being the Center of the Universe. Upon these Principles, the different Phænomena arising from the diurnal Motion of the Earth, and the different Situation of a Spectator upon its Surface, are very naturally illustrated and explained by the Globes.

As to the Alterations of Seasons, &c. arising from the annual Motion of the Earth round the Sun, it is indifferent which we suppose to move, the Earth, or the Sun; for in both Cases, the Effect will be the same: Wherefore because it is the Sun, that appears to us to move, we say the Sun is in such a Part of the Ecliptic, without attributing any Motion to the Earth, any more than if she had actually been at rest. For the same Reason we say, the Sun rises, or the Sun sets; by which we mean, that he begins to appear or disappear, without considering in the least how these Effects are produced. These Things are here mentioned, to obviate the Objections that are sometimes made by Beginners, after they had been told that the Sun stands still.

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## S E C T. I.

### *An Explanation of the Circles of the Sphere, and of some Astronomical Terms arising therefrom.*

**I**N Order to determine the relative Situations of Places upon the Earth, as well as the Positions of the fixed Stars, and other Celestial Phænomena; the Globe of the Earth is supposed to be environ'd by several imaginary Circles, and these are called, the *Circles of the Sphere*. These imaginary Circles are either fixed, and always obtain the same Position in the Heavens; or moveable, according to the Position of the Observer.

Those Circles that are fixed, owe their Origine to the two-fold Motion of the Earth; and are the *Equator*, the *Ecliptic*, with their *Secundaries*, and *Parallels*. These fixed Circles are usually delineated upon the Surface of the Globes.

The moveable Circles are only the *Horizon*, its *Secundaries* and *Parallels*: These are represented by the Wooden-Frame, and

the Brass Ring, wherein the Globe is hung, and a thin Plate of Brass to be screwed in a proper Place upon the said Ring, as Occasion requires.

### I. Of the Equinoctial.

*The Equator or Equinoctial.*

I. The Equator or the Equinoctial, is that Great Circle in the Heavens, in whose Plane the Earth performs its diurnal Motion round its Axis; or it is that Great Circle, parallel to which the whole Heavens seem to turn round the Earth from East to West in 24 Hours.

Note, The Equator and the Equinoctial are generally synonymous Terms; but sometimes the Equator particularly signifies that Great Circle upon the Surface of the Earth, which coincides with the Equinoctial in the Heavens. This Circle is also by Mariners commonly called the Line.

*Northern and Southern Hemispheres.* The Equinoctial divides the Globe of the Earth, and also the whole Heavens into two equal Parts, North and South, which are called the Northern and Southern Hemispheres. The Axis of this Circle is called the Axis of the World, or the Earth's Axis, because the Earth revolves about it (from West to East) in 24 Hours. The Extremes of this Axis are called the Poles of the World, whereof that which lies in the Northern Hemisphere, is called the North-Pole, and the other is called the South-Pole.

The Equinoctial-Circle is always delineated upon the Surface of each Globe, with its Name at length expressed; the Axis of this Circle or the Earth's Axis, is only an imaginary Line in the Heavens, but on the Globes it is expressed by the Wires about which they really turn. The Poles of the World are the two Points upon the Surface of the Globe through which these Wires pass; the North Pole is that which hath the little brass Circle, with a moveable Index placed round it; and the other opposite to it, is the South Pole. The Northern Hemisphere is that wherein the North Pole is placed, and the opposite one is the Southern Hemisphere.

The Astronomers divide all Circles into 360 equal Parts called Degrees, each Degree into 60 equal Parts called Minutes, each Minute into 60 Seconds, &c. But besides this Division into Degrees, the Equinoctial is commonly divided into 24 equal Parts or Hours, each Hour into 60 Minutes, each Minute into 60 Seconds, &c. so that one Hour is equal to 15 Degrees, each Minute of Time is equal to 15 Minutes of a Degree, &c.

2. All

2. All Circles conceived to pass through the Poles of the World, intersecting the Equinoctial at Right-Angles, are with respect to any Point in the Heavens called *Hour-Circles*; and also *Circles of Ascension*, because the Ascension of the Heavenly Bodies, from a certain Point, are by them determined.

*Hour Circles,  
or Circles of A-  
scension, also  
called Meri-  
dians.*

These Circles are also with regard to Places upon the Earth, call'd *Meridians*.

The *Meridians* are commonly drawn upon the Terrestrial Globe thro' every 15 Degrees of the Equinoctial, thereby making an Hour difference betwixt the Places through which they pass. On the Celestial Globe there are commonly drawn but two of these *Meridians* crossing the Equinoctial in four Points equidistant from one another, thereby dividing it into four Quadrants; but the intermediate ones are here supplied, and also upon the Terrestrial Globe, by the Brass Circle in which they are hung, which is therefore called the *Brass Meridian*, and sometimes only the *Meridian*; it serving for this purpose to all the Points upon either Globe.

*The Brass Me-  
ridian.*

There is also a little Brass Circle fixed upon this Meridian, divided into 24 Hours, having an Index moveable round the Axis of the Globe to be turned to any particular Hour. The Use of this Circle is to shew the Difference of Time betwixt any two Meridians, and is therefore called the *Hour-Circle*.

*The Hour Circle.*

3. All Circles parallel to the Equinoctial, are with respect to any Point in the Heavens, called *Parallels of Declination*. So that,

*Parallels of De-  
clination.*

4. The *Declination* of any Point in the Heavens (as the *Sun*, a fixed *Star*, or the like) is an Arch of the Meridian passing through that Point, and intercepted betwixt it and the Equator: And if the said Point be to the

{ Northward } of the Equator, it is called { North } Declination.  
 { Southward } { South } Declination.

*Declination  
North or South.*

Of the Parallels of Declination, four are eminently distinguished by particular Names, viz. The two *Tropics*, and the two *Polar Circles*.

*Tropics and  
Polar Circles.*

5. The *Tropics* are on different Sides of the Equator, each 23 Degrees and 29 Minutes distant from it; that which lies in the Northern Hemisphere, is called the *Tropic of Cancer*; and the Southern one, the *Tropic of Capricorn*.

*Tropics of Can-  
cer; of Capri-  
corn.*

These

## 6 The Description and Use

These Circles are the Limits of the Sun's greatest Declination, and are called Tropics, because whenever the Sun arrives to them; he seems to return back again towards the Equator.

6. The *Polar Circles* are each of them at the same Distance from the Poles of the World, that the Tropics are from the Equator, *viz.*  $23^{\circ} 29'$ .

*Arctic Circle.* That which lies near the North Pole, is called the *Arctic Circle*, from *Arctos* a Constellation situated in the Heavens near that Place; whence also this Pole is sometimes called the *Arctic Pole*.

*Antarctic Circle.* The other Polar Circle, which is situated near the South Pole, is called the *Antarctic Circle*; because its Position is contrary to the other: And the South Pole is sometimes called the *Antarctic Poles*.

The Tropics and the Polar Circles have each their Names expressed upon the Globes.

## II. Of the Ecliptic.

*Ecliptic.*

7. The *Ecliptic* is that great Circle in whose Plane the Earth performs its annual Motion round the Sun; or, in which the Sun seems to move round the Earth once in a Year: This Circle makes an Angle with the Equinoctial of

*Equinoctial Points.*

$23$  Degrees  $29$  Minutes; and intersects it in two opposite Points, which are called the *Equinoctial Points*; and the two Points in the Ecliptic that

*Solstitial Points.*

are at the greatest Distance from the Equinoctial Points, are called the *Solstitial Points*. The two Meridians passing through those Points, are by Way

*Colures.*

of Eminence, called *Colures*; whereof that which passeth thro' the Equinoctial Points is called the *Equinoctial Colure*; and that which is at Right-Angles to it passing through the Solstitial Points, is

*Solstitial Colure.*

called the *Solstitial Colure*.

*The Ecliptic divided into Signs.*

The Ecliptic is divided into  $12$  equal Parts called *Signs*, each Sign being  $30$  Degrees, beginning from one of the Equinoctial Points, and numbered from West to East: The Names and Characters

of the  $12$  Signs are as follow: *viz.*

Aries.	Taurus.	Gemini.	Cancer.	Leo.	Virgo.
1. ♈	2. ♉	3. ♊	4. ♋	5. ♌	6. ♍

Libra.	Scorpio.	Sagittarius.	Capricornus.	Aquarius.	Pisces.
7. ♎	8. ♏	9. ♐	10. ♑	11. ♒	12. ♓

*Northern Signs.*

The first six of these are called the *Northern Signs*, and possess that Half of the Ecliptic which is to the

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the Northward of the Equator; beginning with the first Point of  $\text{\texttt{V}}$ , and ending with the last Point of  $\text{\texttt{w}}$ .

The latter Six are called the *Southern Signs*, because they possess the Southern Half of the Ecliptic, beginning at the first Point of  $\text{\texttt{w}}$ , and ending with the last Point of  $\text{\texttt{X}}$ .

The Division of the Ecliptic into Signs, and the Names of the Colures, are particularly expressed upon the Globes.

The Signs of the Ecliptic took their Names from 12 Constellations situated in the Heavens near those Places. It is to be observed, that the Signs are not to be confounded with the Constellations of the same Name: For the *Sign of Aries* is not the same with the *Constellation Aries*; the latter is a System of Stars digested into the Figure of a Ram; but the Sign of *Aries* is only 30 Degrees of the Ecliptic counted from the Equinoctial Point  $\text{\texttt{V}}$ , (which is reckon'd the first Point in the Ecliptic) to the Beginning of *Taurus*: Or, it is sometimes taken for all that Space upon the Celestial Globe contained between the two Circles passing through the first Points of  $\text{\texttt{V}}$  and  $\text{\texttt{D}}$ . What has been here said of *Aries*, is to be noted of all the rest of the Signs.

The Constellations abovementioned were formerly situated within the Signs, which now bear their Names; but by a slow Motion of the Equinoctial Points, being one Degree in 72 Years, the Constellation *Aries* has now got into the Sign  $\text{\texttt{D}}$ , and so of the rest. So that *Pisces* is now got into the Sign of  $\text{\texttt{V}}$ ; this slow Motion in the Heavens is called the *Precession of the Equinoxes*. By this Motion, that Star, which we now call the *Pole Star* will in process of Time be to the Southward of *London*.

The *Poles of the Ecliptic* are both situated in the Solstitial Colure, at 23 Degrees, 29 Minutes Distance from the Pole of the World; and they take their Denomination from the Hemisphere wherein they are placed, viz. that which lies in the

*Poles of the Ecliptick.*

{ Northern } Hemisphere, is called the { North } Pole of the Ecliptic.  
{ Southern } Hemisphere, is called the { South } Pole of the Ecliptic.  
The Arctic and Antarctic Circles are described by the Poles of the Ecliptic in the Diurnal Motion of the Earth round its Axis, whence it seems these two Circles are called *Polar*.

8. All great Circles passing through the Poles of the Ecliptic, (and consequently intersecting it at Right-Angles) are called *Circles of Longitude*: So that

*Circles of Longitude.*

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*Longitude of any Point in the Heavens.* 9. The *Longitude* of any *Point in the Heavens*, (as a *Star* or *Planet*, &c.) is an Arch of the Ecliptic contained between the Circle of Longitude passing thro' that Point, and the Equinoctial Point  $\gamma$ . And that degree of any Sign which lies under the Circle of Longitude, passing thro' any *Star* or *Planet*, is called the *Place of that Star or Planet*.

*Note;* The *Sun* never goes out of the Ecliptic; and it is not usual to say the *Sun's Longitude*, but we commonly express it the *Sun's Place*, which is that Sign, Degree, Minute, &c. of the Ecliptic, which he at any time possesses.

10. All Circles conceived to be drawn parallel to the Ecliptic, are called *Parallels of Latitude*: So that,

*Latitude of a Star, &c.* 11. The *Latitude* of any *Point in the Heavens*, (as a fixed *Star*, &c.) is an Arch of the Circle of Longitude, passing thro' that Point, and intercepted betwixt it and the Ecliptic; or, the *Latitude* is the Distance from the Ecliptic: And if the said Point be to the Northward of the Ecliptic, it is called *North-Latitude*; but if it be to the Southward, it is called *South-Latitude*.

Upon the *Terrestrial Globe* none of the Circles of Longitude are described; and upon the *Celestial*, they are commonly drawn thro' the Beginning of every *Sign*; but they are all supplied upon both Globes, by fastening a thin Plate of Brass over one of the Poles of the Ecliptic, and so as to be moved to any Degree thereof at pleasure. The Parallels of Latitude are also supplied by the Graduations upon the said Plate, as shall be shewed in a proper Place.

We have now done with all those Circles that are fixed, and such as are drawn upon the Globes themselves; we next proceed to the moveable Circles.

## III. Of the *Horizon*.

*Horizon.*

12. The *Horizon* is that great Circle which divides the upper or visible Hemisphere of the World, from the lower or invisible: This Circle is distinguished into two Sorts, the *Sensible* and the *Rational*.

*Sensible Horizon.* The *Sensible or Apparent Horizon* is that Circle which limits or terminates our Prospect, whether we are at Land or Sea, reaching as far as we can see; or it is that Circle where the *Sky* and the *Earth* or *Water* seem to meet. When we are on *Terra Firma*, this Circle commonly seems rugged and irregular, occasion'd by the unevenness of the Ground terminating our Prospect; but at Sea there are no such Irregularities. The Semidiameter of this

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this Circle varieh according to the Heighth of the Eye of the Observer; if a Man of Six Foot high stood upon a large Plane, or the Surface of the Sea, he could not see above three Miles round.

The *Sensible or Apparent Horizon* is the Extremity of the Earth, that bounds our Sight, which for the most part is uneven; and at Sea is of a greater or less extent, as the Eye is higher or lower: And supposing a Degree of the Circumference of the Earth to be 365000 Feet, *London Measure*, (as agreeing with the most accurate Observations yet made) then will the Circumference be 26280 Miles, each of 5000 Feet, and consequently the Semi-diameter of the Earth will be about 4365, 188 Miles.

And therefore the Eye, at the Heighth of 5 Feet above the Surface of the Water, will see but 2, 262 Miles off: at 20 Feet high, 5, 784 Miles: at 50 Feet, 9, 146 Miles, and at 100 Feet high, 12, 932 Miles every way: Or generally, putting  $d$  for the Diameter of the Earth, and  $b$  for the Heighth of the Eye above the Surface of the Water, the Semi-diameter of the *Sensible Ho-*

*rizon* will be equal to  $\sqrt{d+b^2}$ .

Tho' the Rising and Setting of the Stars respect the *Rational Horizon*, yet by Reason of their vast Distance, it holds true of the *Sensible*, which is more than 4000 Miles above it.

This Circle determines the Rising and Setting of the heavenly Bodies, and distinguishes Day and Night.

The *Rational or true Horizon* is a great Circle Rational Hori- passing thro' the Center of the Earth parallel to the to the below the sensible Horizon, being distant from it by the Earth's Semi-diameter, which is nothing in Comparison of the immense Distance of the Sun and the fixed Stars, therefore Astronomers make no Distinction between these two Circles, but consider the apparent Horizon, or that wherein the Sun appears to rise and set, as passing thro' the Center of the Earth.

This Circle is divided by Astronomers into four Quadrants, and each of these Quadrants into 90 Degrees, &c. position The Four Points quartering this Circle are call'd Cardinal Points of the Horizon. the *Cardinal Points*, and are termed the *East*, *West*, *North* and *South*: The *East* is that Point of the *Horizon* where the Sun rises when he is in the Equinoctial; or on that Day when he ascends above the *Horizon* exactly at Six o'Clock; and the *West* is that Point of the *Horizon* which is directly opposite to the *East*, or where the Sun sets, when he is in the Equinoctial. The *South* is 90 Degrees distant from the *East* and *West*, and is towards that part of the Heavens wherein the Sun always appears to us in Great Britain at Noon; and

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the

the *North* is that Part of the Heavens which is directly opposite to the *South*. Or the North and South Points of the Heavens may be found by turning your self directly either towards the East or the West: If you look towards the

(*East*) the (*South*) will be to the right Hand, and the (*North*) to the Left (*South*)

*Points of the Compass.* Besides the aforementioned Division of the Horizon into Degrees, *Mariners* divide it into 32 equal

Parts, which they call the *Points of the Compass*; to each of which Points they give a particular Name, compounded of the four Cardinals, according to what Quarter of the Compass is intended.

*Zenith,* The Center of the Horizon is the Place of Observation, and the Poles of it are, one exactly over our Heads, called the *Zenith*; and the other exactly under our Feet called the *Nadir*.

*Vertical Circles.*

*Meridian.*

*Azimuth.*

13. All Circles conceived to pass thro' the Zenith and Nadir, are called *Vertical Circles*, or *Azimuths*. Of these Circles, that which passes thro' the North and South Points of the Horizon is called the *Meridian*; so that when any Object is upon the Meridian, it then bears either due South or due North from us; and the *Azimuth* of any Object is an Arch of the Horizon intercepted between the Vertical Circle passing thro' it, and either the North or South part of the Meridian; which Part is commonly specified.

The Meridian passes thro' the Poles of the World, as well as thro' the Zenith and Nadir, and therefore is a Secondary both of the Equinoctial and the Horizon: This Circle divides the Globe into the *Eastern* and *Western Hemispheres*; and the Poles of it are the *East* and *West* Points of the *Horizon*. All the heavenly Objects are during one half of their Continuance above the Horizon, in the Eastern Hemisphere, and for the other half in the Western; so that whenever the Sun arrives upon the upper part of the Meridian, it is then *Noon* or *Mid day*, which is the reason why this Circle is called the *Meridian*; and when he comes to the lower part, it is then *Mid-night*.

*Prime-Vertical.* The Vertical Circle passing thro' the *East* and *West* of the *Horizon*, is called the *Prime-Vertical*, or *Circle of East and West*: so that when any Object is upon this Circle in the Eastern Hemisphere, it appears due *East*; and if it be in the Western Hemisphere it appears due *West*.

That

## Sect. I. of the GLOBES.

II

That Degree in the Horizon wherein any Object rises and sets from the East or West Points is called the *Amplitude*; which for rising is called *Amplitude Oriente* *Amplitude* and *Oscansive* for Setting; which must be also denominated, whether it be Northerly or Southerly.

It may be observed, that the *Amplitude* and *Azimuth* are much the same; the *Amplitude* shewing the bearing of any Object when he rises or sets, from the East or West Points of the Horizon; and the *Azimuth* the bearing of any Object, when it is above the Horizon, either from the North or South Points thereof. As for Example, if an Object rises or sets within 10 Degrees of the East or West, suppose towards the South, we accordingly say its *Amplitude* is 10 Degrees Southerly; but if an Object, that is of any Height above the Horizon should be in the Vertical Circle passing thro' the aforementioned Point, we then say, its *Azimuth* is 80 Degrees from the South, or 100 Degrees from the North, both which Expressions signify the same.

14. All Circles drawn parallel to the Horizon, in the upper Hemisphere, are called *Almicanter*, or *Parallels of Altitude*: so that the *Altitude* of any Point in the Heavens, is an Arch of the Vertical Circle passing thro' that Point, and intercepted betwixt it and the Horizon: and if the Object be upon the Meridian, it is commonly called the *Meridian Altitude*. *Meridian Altitude.* The Complement of the Altitude, or what it wants of 90 Degrees, is called the *Zenith Distance*. *Zenith Distance.*

The Horizon (by which we mean the Rational) is represented by the upper Surface of the Wooden Frame wherein the Globes are placed; upon this Horizon are described several Concentric Circles, the innermost of which is divided into four times 90 Degrees, beginning at the East and the West Points, and counted both ways to the North and South, where they end at 90 Degrees. The Use of these Divisions is to shew the Amplitudes of the Sun and Stars at their Rising and Setting: Also in some convenient Place upon this Horizon, there are commonly noted the Points of the Compass. Without the aforementioned Circle, there is drawn the Ecliptic, with its Divisions into Signs and Degrees, and a Circle of Months and Days: The Use of these two Circles is to serve as a Calendar to shew the Sun's Place at any time of the Year; and by that means to find his Place in the Ecliptic drawn upon the Globe it self.

The *Vertical Circles*, and the *Parallels of Altitude*, are supplied by a thin Plate of Brass, having a Nut and Screw at one end, to fasten it to the Brass Meridian in the Zenith Point; which be-

ing done, the lower End of it may be put between the Globe it self and the inner Edge of the Horizon, and so turned round about to any Point required. The fiducial Edge thereof representing the *Vertical Circles*, and the *Degrees* upon it, describing the Parallels of Altitude. This thin Plate is called the *Quadrant of Altitude*.

The Center of the Horizon being the Place of Observation, it is evident, that this Circle, and all the others belonging to it, are continually changed which way soever we move; wherefore we may suppose the Horizon, with its Secundaries and Parallels, to invest the Globe like a Rete or Net; and to be moyeable every way round it. This is very naturally illustrated by the Globes; if we move directly North or directly South, the Change made in the Horizon is represented, by moving the Brass Meridian (keeping the Globe from turning about its Axis) in the Notches made in the Wooden Horizon just so much as we travelled. If our Course should be due East or due West, the Alterations made thereby are represented, by turning the Globe accordingly about its Axis, the Brass Meridian being kept fixed; and if we steer betwixt the Meridian and the East or West Points, then we are to turn the Brass Meridian, and also the Globe about its Axis accordingly.

The Sum of which is: Let the Spectator be in what Point soever of the Earth's Surface, he'll there gravitate or tend exactly towards its Center, and imagin himself to be on the highest Part thereof, (the unevenness of the Ground not being here considered:) wherefore if we turn the Globe in such a manner, as to bring the several Progressive Steps of a Traveller successively to the Zenith, we shall then have the successive Alterations made in the Horizon, in every Part of his Journey. This Explication being well considered, will be of help to Beginners to conceive how the Earth is every where habitable, and how Passengers can travel quite round it: For since every thing tends towards the Center of the Earth, we are to conceive that Point as being the lowest, and not to carry our Idea of downwards any farther: Those that are diametrically opposite to us, being as much upon the upper part of the Earth as we are; there being no such thing in Nature, as one Place being higher than another, but as it is at a greater distance from the Center of the Earth, let it be in what Country soever.

We have now done with all the Circles of the Sphere, and it may be observed, that the *Equinoctial*, the *Ecliptic*, and the *Horizon*, with their Secundaries and Parallels, are all alike; and altering their Position, may be made to serve for one another. Thus, If the Poles of the World be brought into the Zenith and

Nadir;

Nadir; the Equinoctial will coincide with the Horizon, the Meridians will be the same with the Vertical Circles, and the Parallels of Declination will be the Parallels of Altitude. After the same manner, if shifting the Position we bring the Ecliptic to coincide with the Horizon; the Circles of Longitude will be the Vertical Circles, and the Parallels of Latitude and Altitude will coincide.

The Horizon and the Equator may be either Parallel, Perpendicular, or Oblique to each other.

15. A *Parallel Sphere* is that Position where the *Parallel Sphere*. Equator coincides with the Horizon, and consequently the Poles of the World are in the Zenith and Nadir: The Inhabitants of this Sphere (if there be any) are those who live under the Poles of the World.

16. A *Right or Direct Sphere* is that Position, where *Right Sphere*. the Equator is perpendicular to the Horizon; the Inhabitants whereof are those who live under the Equinoctial.

17. An *Oblique Sphere* is when the Equinoctial *Oblique Sphere*. and the Horizon make Oblique Angles with each other; which every where happens, but under the Equator and the Poles.

The Arch of any Parallel of Declination which stands above the Horizon, is called the *Diurnal Arch*; and the remaining part of it, which is below the *Horizon*, is called the *Nocturnal Arch*. *Diurnal and Nocturnal Arch.*

That Point of the Equinoctial which comes to the Eastern Part of the Horizon, with any Point in the Heavens, is called the Ascension of that Point, counted from the Beginning of  $\text{V}$ ; and if it be in a Right Sphere, the Ascension or Descension is called Right; but if it be in an Oblique Sphere, it is called Oblique Ascension or Descension.

So that,

18. The *Right Ascension* of the Sun, Moon, or any *Right Ascension*. Star, &c. is an Arch of the Equator contained betwixt the Beginning of  $\text{V}$ , and that Point of the Equinoctial which rises with them in a *Right Sphere*; or which comes to the Meridian with them in an *Oblique Sphere*.

19. *Oblique Ascension or Descension*, is an Arch of the Equinoctial intercepted betwixt the Beginning of  $\text{V}$ , and that Point of the Equator which rises or sets with any Point in the Heavens in an *Oblique Sphere*. *Oblique Ascension.*

20. *Ascensional Difference* is the Difference betwixt the *Right and Oblique Ascension or Descension*; and shews how long the Sun rises or sets before or after the Hour of Six. *Ascensional Difference.*

## IV. Of the Division of Time.

The Parts that Time is distinguished into, are *Days, Hours, Weeks, Months and Years.*

A Day is either Natural or Artificial.

A *Natural Day* is the Space of Time elapsed, while the Sun goes from any Meridian or Horary Circle, till he arrives to the same again; or, it is the Time contained from Noon or any particular Hour, to the next Noon or the same Hour again: An *Artificial Day*, is the Time betwixt the Sun's Rising and Setting, to which is opposed the *Night*, that is, the Time the Sun is hid under the Horizon.

The *Natural Day* is divided into 24 *Hours* each Hour into 60 *Minutes*, each Minute into 60 *Seconds*, &c.

The *Artificial Days* are always unequal to all the Inhabitants that are not under the Equator, except when the Sun is in the Equinoctial Points  $\text{V}$  and  $\text{W}$ , which happens (according to our way of reckoning) about the 10th of March and 12th of September; at those Times the Sun rises at six, and

*Equinoxes.*

*Vernal and Autumnal Equinox*

sets at six, to all the Inhabitants of the Earth. These Days are called the *Equinoxes* or *Equinoctial Days*; the first of which, or when the Sun is in the first Point of *Aries*, is called the *Vernal Equinox*, and the latter is called the *Autumnal Equinox*. At all other times of the Year, the Days continually lengthen or shorten and that faster or slower according as the Sun is nearer to or further from the Equinoctial, until he arrives to either of the *Solstitial Points*  $\text{G}$  or  $\text{W}$ . At those Times the Sun seems to stand still for a few Days, and then he begins to return with a slow Motion towards the Equinoctial, still hastening his Pace as he comes nearer to it: The Sun enters the Tropics of  $\text{G}$  and  $\text{W}$ , about the 10th of June and the

21st of December, which Days are sometimes called the *Solstices*; the first of which we call the *Summer Solstice*, and the latter the *Winter-Solstice*.

*Solstices. Summer and Winter Solstice*

All Nations do not begin their Day, and reckon their Hours alike. In *Great-Britain, France* and *Spain*, and in most Places in *Europe*, the Day is reckoned to begin at *Midnight*, from whence are counted 12 Hours till *Noon*, then 12 Hours more till *Midnight*, which make a complete Day: Yet the *Astronomers* (in these Countries) commonly begin their Day at *Noon*, and so

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reckon 24 Hours till next Noon, and not twice twelve, according to the vulgar Computation.

The *Babylonians* began their Day at Sun-rising, and reckoned 24 Hours till he rose again: this way of Computation we call the *Babylonish Hours*. In several Parts of *Germany* they count their Hours from Sun setting, calling the first Hour after the Sun has set, the first Hour, &c. till he sets the next Day, which they call the 24th Hour: these are commonly called the *Italian Hours*. According to both these ways of Computation, their Hours are commonly either a little greater or less than the  $\frac{1}{24}$  part of a natural Day. in Proportion as the Sun rises or sets sooner or later in the succeeding Days: They have also this Inconvenience, that their Mid-day and Mid-night happen on different Hours, according to the Seasons of the Year.

The *Jews* and the *Romans* formerly, divided the *Artificial Days* and Nights each into 12 equal Parts; these are termed the *Jewish Hours*, and are of different Lengths according to the Seasons of the Year, a Jewish Hour in Summer, being longer than one in Winter, and a Night Hour shorter. This Method of Computation is now in Use among the *Turks* and the Hours are styled the *first Hour*, *second Hour*, &c. of the Day or Night; so that *Mid-day* always falls upon the sixth Hour of the Day. These Hours are also called *Planetary Hours*; because in every Hour one of the Seven Planets was supposed to preside over the World, and so take it by turns. The first Hour after Sun rising on Sunday was allotted to the *Sun*; the next to *Venus*; the third to *Mercury*; and the rest in order to the *Moon*, *Saturn*, *Jupiter*, and *Mars*. By this means on the first Hour of the next Day, the Moon presided, and so gave the Name to that Day; and so seven Days by this Method had Names given them from the Planets that were supposed to govern on the first Hour.

A *Week* is a System of seven Days, in which each Day is distinguished by a different Name. In most Countries, these Days are called after the Names of the Seven Planets, as above noted. All Nations that have any Notion of Religion, set apart one Day in seven for public Worship; the Day solemnized by *Christians* is Sunday, or the first Day of the Week, being that on which our Saviour rose from the Grave, on which the Apostles afterwards used more particularly to assemble together to perform divine Worship. The *Jews* observed Saturday, or the seventh Day of the Week, for their Sabbath or Day of Rest, being that appointed in

in the fourth Commandment under the Law. The Turks perform their religious Ceremonies on Friday or the 6th Day of the Week.

*A Month.*

*Periodical and Synodical Months*

A Month is properly a certain Space of Time measured by the Moon in its Course round the Earth. A Lunar Month is either Periodical or Synodical. A Periodical Month is that Space of Time the

Moon takes to perform her Course from one Point of the Ecliptic till she arrives to the same again; which is 27 Days and some odd Hours: And a Synodical Month is the Time betwixt one new Moon and the next new Moon, which is commonly about 29½ Days, But a Civil Month is different from these, and consists of a certain Number of Days, fewer or more, according to the Laws and Customs of the Country wherein they are observed.

The completest Period of Time is a Year, in which all the Variety of Seasons return, and afterwards begin a-new. A Year is either Astronomical or Civil. An Astronomical Year is either a Sydereal, wherein the Sun departing from a fixed Star, returns to it again; or, Tropical, which is the Space of Time the Sun takes to perform its Course from any Point of the Ecliptic till he returns to it again.

A Tropical Year consists of 365 Days, 5 Hours, and 49 Minutes; this is the Time in which all the Seasons completely return, which is a small matter less than a Sydereal Year.

The Civil Year is the same with the Political established by the Laws of a Country, and either moveable or immovable. The moveable Year consists of 365 Days, being less than the Tropical Year by almost six Hours; and is called the Egyptian Year, because observed in that Country.

The Romans divided the Year into 12 Kalendar Months, to which they gave particular Names, and are still retained by most of the European Nations. viz. January, February, March, April, May, June, July, August, September, October, November and December. The Number of Days in each Month may be known by the following Verses:

Thirty Days hath September,  
April, June, and November;  
February hath Twenty-Eight alone,  
And all the rest have Thirty One.

The

The Year is also divided into four Quarters or Seasons, viz. The Spring, Summer, Autumn and Winter. These Quarters are properly made, when the Sun enters into the Equinoctial and Solstitial Points of the Ecliptic: But in civil Uses they are differently reckon'd, according to the Customs of several Countries. In England we commonly reckon the first Day of January to be the first in the Year, which is therefore vulgarly called New-year's-Day; but in Political and Ecclesiastical Affairs, the Year is reckoned to commence on *Lady-Day*, (so called) which is the 25th of March; and from thence to *Midsummer-Day*, which is the 24th of June, is reckoned the first Quarter; from *Midsummer-Day* to *Michaelmas-Day*, which is the 29th of September, is the second Quarter; the third Quarter is reckon'd from *Michaelmas-Day* to *Christmas-Day*, which is the 25th of December; and from *Christmas-Day* to *Lady-Day*, is reckoned the last Quarter in the Year. In common Affairs, a Quarter is reckoned from a certain Day to the same in the fourth Month following. Sometimes a Month is reckoned four Weeks or 28 Days, and so a Quarter 12 Weeks. To all the Inhabitants in the

{ Northern } Hemisphere, their *Midsummer* is properly when  
{ Southern } the Sun appears in the Tropic of { Cancer } and their *Midwinter*  
the opposite Time of the Year. But those who live under  
the Equinoctial, have two *Winters*, viz. when the Sun is in ei-  
ther Tropic; tho' indeed properly there is no Season that may  
be called *Winter* in those Parts of the World.

The *Egyptian Year* of 365 Days, being less than the true Solar Year, by almost six Hours, it follows that four such Years are less than four Solar Years, by a whole Day; and therefore in 365 times four Years, that is, in 1460 Years, the Beginning of the Years moves through all the Seasons. To remedy this Inconveniency, *Julius Cæsar* (considering that the six Hours which remain at the End of every Year, will in four Years make a natural Day) ordered that every fourth Year should have an intercalary Day, which therefore consists of 366 Days; the Day added was put in the Month of *February*, by postponing *St. Mathias's Day*, which in common Years falls on the 24th, to the 25th of the said Month: All the fixed Feasts in the Year from thenceforwards falling a Week-day later than otherwise they would.

According to the *Roman Way* of reckoning, Bissextile or Leap-Year.  
the 24th of *February* was the sixth of the Kalends of *March*, and it was ordered that for this Year there should be two Sixths, or that the Sixth of the Kalends of

of March should be twice repeated; upon which Account the Year was called *Bisextile*, which we now call the *Leap year*.

To find whether the Year of our Lord be Leap-Year, or the First, Second, or Third after; divide it by four, and the Remainder, if there be any, shews how many Years it is after Leap-Year; but if there be no Remainder, then that Year is Leap-Year: Or, omit the Hundreds and Scores, and divide the Residue by 4. Example, 1731, omitting the Hundreds and the Twenty, I divide the Residue 11 by 4, and the Remainder 3, shews it to be the Third after Leap-Year.

This Method of reckoning the Year, viz. making the common Year to consist of 365 Days, and every fourth Year to have 366 Days, is now used in *Great-Britain* and *Ireland*, and some of the Northern Parts of *Europe*, and is Julian Account, called the *Julian Account*, or the *Old Style*. But the or the Old Style. Time appointed by *Julius Cæsar* for the Length of a Solar Year is too much; for the Sun finishes his apparent Course in the Ecliptic in 365 Days, 5 Hours, and 49 Minutes, which is 11 Minutes less than the Civil Year; and therefore he agajn begins his Circuit 11 Minutes before the Civil Year is ended: And so much being gained every Year, amounts in 131 Years to a whole Day. So that if the Sun in any Year entred the Equinox upon the 20th of March at Noon, after the Space of 131 Years, he'll enter the same Point on the same Hour of the 19th of March. And therefore the Equinoxes will not always fall on the same Day of the Month, but by degrees will move towards the Beginning of the Year.

At the Time of the *Council of Nice*, (when the Terms were settled for Observing of *Easter*) the *Vernal Equinox* fell upon the 21st of *March*; but by its falling backwards 11 Minutes every Year, it was found that in *Anno 1582*, when the *Kalendar* was corrected, the Sun entred the Equinoctial Circle on the 11th of *March*, having departed ten whole Days from its former Place in the Year: And therefore Pope *Gregory* the XIII<sup>th</sup> designing to place the Equinoxes in their former Situation with respect to the Year, took these ten Days out of the *Kalendar*, and order'd that the Eleventh of *March* should be reckon'd as the Twenty-first: And to prevent the Seasons of the Year from going backwards for the Future, he ordered that every hundredth Year, which in the *Julian Form* was to be a *Bisextile*, should be a common Year, and consist only of 365 Days; but that being too much, every fourth Hundred was to remain

*Bisextile*. This Form of reckoning being established by the Authority of Pope *Gregory XIII*, is called the *Gregorian Account*, or the *New Style*; and is observed in all the Countries where the Authority

Gregorian Account, or New Style.

## Sect. I. of the GLOBES. 19

Authority of the Pope is acknowledged, and likewise, by several Nations of the reformed Religion. There being now above a hundred Years past, since this Reformation was made in the Kalendar, the *Gregorian* Account has accordingly got before the *Julian* one Day more than it was at the Time of its Institution, the Difference between these two Accounts being now eleven Days; so that the first Day of any Month, according to our Way of reckoning, is the 12th of the same Month according to the New Style.

I shall conclude this Section with a brief Account of the *Atmosphere*.

The *Atmosphere* is that thin Body of Air which *Atmosphere*, surrounds the Earth, in which the Clouds however, and by which in their Descent they are broke into Drops of Rain; which sometimes, according to the Warmth or Coldness of the Air, are froze into Snow, or Hailstones. Thunder and Lightning are also made in the *Atmosphere*; and Wind is nothing else but a Percussion of the Air, occasion'd by its different Density in different Places. The Benefits we receive from the *Atmosphere* are innumerable; without Air no earthly Creature could live, as is plainly proved by Experiments made by the *Air-Pump*; and the Wholesomnels of a Climate chiefly depends upon that of its Air: If there was no *Atmosphere* to reflect the Rays of the Sun, no Part of the Heavens would be lucid and bright, but that wherein the Sun was placed; and if a Spectator should turn his Back towards the Sun, he would immediately perceive it to be quite dark, and the least Stars would be seen shining as they do in the clearest Night; and the Sun immediately before his setting would shine as brisk as at Noon. But in a Moment, as soon as he is got below the Horizon, the whole *Hemisphēre* of the Earth would be involved in as great a Darkness, as if it were Midnight.

But by Means of the *Atmosphere*, it happens that while the Sun is above the Horizon, the whole Face of the Heavens is strongly illuminated by its Rays, so as to obscure the faint Light of the Stars and render them invisible; and after Sun-setting, though we receive no direct Light from him, yet we enjoy its reflected Light for some Time: For the *Atmosphere* being higher than we are, is a longer Time before it is withdrawn from the Sun. (as if a Man was to run up to the Top of a Steeple, he may see the Sun after it had been set to those at the Bottom.) The Rays which the *Atmosphere* receives from the Sun, after he is withdrawn from our Sight, are by Refraction faintly transmitted to us; until the Sun having got about 18 Degrees below the Horizon, he no longer enlightens our *Atmosphere*, and then all that Part thereof which is over us becomes

comes dark. After the same Manner, in the Morning, when the Sun comes within 18 Degrees of our Horizon, he again begins to enlighten the *Atmosphere*, and so more and more by degrees, until he rises and makes full Day. This *Twilight, or the Crepusculum.* small Illumination of the *Atmosphere*, and State of the Heavens between Day and Night, is called the *Twilight, or the Crepusculum.*

The Duration of Twilight is different in different Climates, and in the same Place at different Times of the Year. The Beginning or Ending of Twilight being accurately given, we may from thence easily find the Height of the *Atmosphere*, which is not always the same. The mean Height of the *Atmosphere* is computed to be about 48 English Miles; but it is probable, the Air may expand it self a great deal further, there being properly no other Limits to it, as we can conceive, but as it continually decreases in Density the farther remote it is from the Earth, in a certain Ratio; which at last, as to our Conception, must terminate.

By the *Crepusculum* or Twilight to determin the true Height of our *Atmosphere*; which is like a Husk, or Shell surrounding the Earth on every Side.

Let ADB be half of the Earth's enlighten'd Hemisphere, D our Sub-Zenith, E the Sun when depress'd  $17^{\circ} 27'$  below the Horizon (that is, allowing  $33'$  for Refraction) DG our Horizontal Line, GE an Horizontal Line of Sun-set to them at E; bisect the Arch DE in G: So is there two right-angled Triangles, viz. DCG=GCE, whose Quantity is  $8^{\circ} 43\frac{1}{2}'$ : Let C be the Earth's Center, CF=CD=CE the Earth's Semi-diameter. 3984.58 English Miles; the Height of the *Atmosphere* is FG: To find which in the right-angled plane Triangle CFG, I lay, [See Plate I. Fig. 3.]

As S. Angle CGE	$81^{\circ} 36' 30''$	9.994945
To CE the $\odot$ 's Semi-diameter	3984.58	3.600383
Radius	90 00 00	10.000000
CG	4031.7	3.605438
Earth's Semi-diameter Subtract CF	3984.58	
Remains FG	47.12	which is the Height of the <i>Atmosphere</i> in English Miles.

And if you would know, what Proportion its Height bears to the Earth's Semi-diameter, you will find it to be as 1 to 84.56. Soe the Height of the *Atmosphere* to the Earth's Semi-diameter, thus 47.12) 3984.580 (84.56.

## SECT. II.

GEOGRAPHICAL DEFINITIONS: Of the Situations of Places upon the Earth; of the different Situations of its Inhabitants; of Zones and Climates.

THE Situation of Places upon the Earth are determined by their Latitude and Longitude.

1. The Latitude of any Place (upon the Earth) *Latitude.* is its nearest Distance, either North or South, from the Equator; and if the Place be in the

$\begin{cases} \text{Northern} \\ \text{Southern} \end{cases}$  Hemisphere, it is accordingly called  $\begin{cases} \text{North} \\ \text{South} \end{cases}$  *Latitude;*

and is measured by an Arch of the Meridian passing thro' the Zenith of the said Place, and intercepted betwixt it and the Equator. And all Places that lie on the same Side, and at the same Distance from the Equator, are said to be in the same Parallel of Latitude: The Parallels of Latitude in *Geography* being the same with the Parallels of Declination in *Astronomy.*

From this Definition arise the following Corollaries,

(1.) That no Place can have above 90 Degrees of Latitude, either North or South.

(2.) Those Places that lie under the Equinoctial (or thro' which the Equator passes) have no Latitude, it being from thence that the Calculation of Latitude is counted. And those Places that lie under the Poles have the greatest Latitude, those Points being at the greatest Distance from the Equator.

(3.) The Latitude of any Place is always equal to the Elevation of the Pole in the same Place, above the Horizon; and is therefore often expressed by the Pole's Height, or Elevation of the Pole: The Reason of which is, because from the Equator to the Pole, there is always the Distance of 90 Degrees, and from the Zenith to the Horizon the same Number of Degrees, each of these including the Distance from the Zenith to the Pole. That Distance therefore being taken away from both, will leave the Distance from the Zenith to the Equator, (which is the Latitude) equal to the Distance from the Pole to the Horizon.

(4.) The Elevation of the Equator in any Place, is always equal to the Complement of the Latitude of the same Place.

(5.) A

*The Description and Use*

(5.) A Ship sailing directly  $\left\{ \begin{array}{l} \text{towards} \\ \text{from} \end{array} \right\}$  the Equator,  $\left\{ \begin{array}{l} \text{Lessens} \\ \text{Augments} \end{array} \right\}$  her Latitude, or  $\left\{ \begin{array}{l} \text{Depresses} \\ \text{Raises} \end{array} \right\}$  the Pole, just so much as is her Distance sailed.

*Difference of Latitude.* 2. *Difference of Latitude* is the nearest Distance betwixt any two Parallels of Latitude, shewing how far the one is to the Northward or Southward of the other; which can never exceed 180 Degrees. And when the two Places are in the same Hemisphere (or on the same Side of the Equator) the lesser Latitude subtracted from the greater, and when they are on different Sides of the Equator, the two Latitudes added, gives the Difference of Latitude.

*Longitude.* 3. The *Longitude* of any Place (upon the Earth) is an Arch of the Equator, contained betwixt the Meridian of the given Place, and some fixed or known Meridian: or, it is equal to the Angle formed by the two Meridians; which properly can never exceed 180 Degrees; tho' sometimes the Longitude is counted Easterly quite round the Globe.

Since the Meridians are all moveable, and not one that can be fixed in the Heavens, (as the Equinoctial Circle is fixed, from whence the Latitudes of all Places are determined to be so much either *North* or *South*) the Longitudes of Places cannot so well be fixed from any one Meridian; but every Geographer is at his Liberty to make which he pleases his first Meridian, from whence to calculate the Longitudes of other Places. Hence it is, that the Geographers of different Nations, reckon their Longitudes from different Meridians, commonly chusing the Meridian passing thro' the Metropolis of their own Country for their first: Thus, the English Geographers generally make the Meridian of London to be their first; the French, that of Paris; and the Dutch, that of Amsterdam, &c. And Mariners generally reckon their Longitude from the last known Land they saw. This arbitrary Way of reckoning the Longitude from different Places, makes it necessary, whenever we express the Longitude of any Place, that the Place from whence it is counted be also expressed.

From the preceding Definitions arise the following *Corollaries*.

I. If a Body should steer directly North, or South, quite round the Globe, he'll continually change his Latitude; and pass thro' the two Poles of the World, without deviating the least from the Meridian of the Place before

parted from; and consequently at his Return, will not differ in his Account of Time from the People residing in the said Place.

2. If a Body should steer round the Globe, either due East or due West, he'll continually change his Longitude, but will go quite round without altering his Latitude; and if his Course should be due East, he'll gain a Day completely in his reckoning, or reckon one Day more than the Inhabitants of the Place from whence he departed: And if his Course had been West, he would have lost one Day, or reckoned one less.

The Reason of which is evident: For, admitting our Traveller steers due East so many Miles in one Day, as to make his Difference of Longitude equivalent to a Quarter of an Hour of Time; it is evident, that the next Day the Sun will rise to him a Quarter of an Hour sooner, than to the Inhabitants of the Place from whence he departed: And so daily, in Proportion to the Rate he travels, which in going quite round will make up one natural Day. In like Manner, if he steers due West after the same Rate, he'll lengthen each Day a Quarter of an Hour, and consequently the Sun will rise to him so much later every Day; by which Means, in going quite round, he'll lose one Day complete in his reckoning. From whence it follows,

3. If two Bodies should set out from the same Place, one steering East, and the other West, and so continue their Courses quite round, until they arrive at the Place from whence they set out, they'll differ two Days in their Reckoning at the Time of their Return.

4. If a Body should steer upon an oblique Course (or any where betwixt the Meridian and the East or West Points) he'll continually change both Latitude and Longitude, and that more or less, according to the Course he steers; and if he should go quite round the Globe, he'll differ in his Account of time, as by the 2d Corol.

5. The People residing in the Eastermost of any two Places, will reckon their Time so much the sooner than those who live in the other Place, according to the Difference of Longitude betwixt the two Places, allowing 1 hour for every 15 Degrees, &c. and the contrary.

## II. Of Zones and Climates, &c.

4. Zones are large Tracts of the Surface of the Earth, distinguished by the Tropics and Polar Circles; being five in Number, viz. one Torrid, two Temperate, and two Frigid.

*Zones Torrid,  
Temperate, and  
Frigid.*

The Torrid or Burning Zone is all the Space comprehended between the two Tropics; the Antients imagined this Tract of the

the Earth to be uninhabitable, because of the excessive Heat, it being so near the Sun. All the Inhabitants of the *Torrid Zone* have the Sun in their Zenith, or exactly over their Heads, twice in every Year; excepting those who live exactly under the two *Tropics*, where the Sun comes to their Zenith only once in a Year.

The two *Temperate Zones* lie on either Side of the Globe, between the *Tropics* and the *Polar Circles*.

The two *Frigid Zones* are those Spaces upon the Globe that are included within the two *Polar Circles*.

The Dimensions of each *Zone* in square *English Statute Miles* (69,5 whereof make a Degree) are as follow, viz. Of the *Torrid Zone* 415474528457; of each *Temperate Zone* 270025710933; of each *Frigid Zone* 43209396510.

So that if the whole Earth be divided into 520 equal Parts, the *Torrid*, both *Temperate*, and both *Frigid Zones*, would bear nearly the following Proportions to one another.

The whole Surface of the Earth	—	—	—	—	520
The <i>Torrid Zone</i>	—	—	—	—	20
Both <i>Temperate Zones</i>	—	—	—	—	27
Both <i>Frigid Zones</i>	—	—	—	—	4

To find the exact Proportion of the *Zones*, tho' the Quantit of the Earth's Surface is unknown.

The Distance of the *Polar Circles* from the Pole is  $23^{\circ} . 29'$ , whose Complement is  $66^{\circ} . 31'$ , its natural Sine is .917176 which deduct from 10.00000 gives .82824, and doubled, .165648 for the exact Proportion of the two *Frigid Zones*.

The Distance of the *Tropic* from the Equator is  $23^{\circ} . 29'$ , its natural Sine is .398482, which deduct from the natural Sine of  $66^{\circ} . 31' = .917176$ , remains .518694, and this doubled .1037388 for the Proportion of the two *Temperate Zones*.

And for the *Torrid Zone*, which is  $23^{\circ} . 29'$  from the Equator on either Side, only double the natural Sine of  $23^{\circ} . 29' = .398482$ , which will be — — — — — .79696

The aforesaid 2 <i>Temperate</i>	1.037388
The aforesaid 2 <i>Frigid</i>	.165648

Proof In all, double Radius 2.00000

The Inhabitants of the Earth are also distinguished by the Diversity of their *Shadows*. Those who live in *Amphibians*. the *Torrid Zone*, are called *Amphibians*; because their Noon-Shadow is cast different Ways, according as the Sun is to the Northward or Southward of the Zenith: But when the Sun is in their Zenith, they are called *Arians*. T

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The Inhabitants of the Temperate Zones, are called *Heteroscians*, because their Noon-Shadow is always cast the same Way: But those who live under the Tropics are called *Ascians Heteroscians*. Those who live in the Frigid Zones are called *Periscians*, because sometimes their Shadow is cast round about them.

*Heteroscians.*

*Ascians Heteroscians.*

*Periscians.*

These hard Names are only Greek Words importing how the Sun casts the Shadow of the several Inhabitants of the Earth; which would be a too trifling Distinction to be made here, was it not for the Sake of complying with Custom.

The Inhabitants of the Earth, are also distinguished into three Sorts, in respect to their relative Situation to one another; and these are called, the *Periaci*, *Antaci*, and *Antipodes*.

5. The *Periaci* are those who live under opposite Points of the same Parallel of Latitude. They have their Seasons of the Year at the same Time, and their Days and Nights always of the same Length with one another; but the one's *Noon* is the other's *Midnight*: And when the Sun is in the Equinoctial, he rises with the one, when he sets with the other. Those who live under the Poles have no *Periaci*.

*Periaci.*

6. The *Antaci* live under the same Meridian, and in the same Latitude, but on different Sides of the Equator; their Seasons of the Year are contrary, and the Days of the one are equal to the Nights of the other: But the Hour of the Day and Night is the same with both; and when the Sun is in the Equinoctial, he rises and sets to both exactly at the same Time. Those who live under the Equator have no *Antaci*.

*Antaci.*

7. The *Antipodes* are those who live diametrically opposite to one another, standing, as it were, exactly Feet to Feet: Their Days and Nights, Summer and Winter, are at direct contrary Times.

*Antipodes.*

The Surface of the Earth is by some distinguished into *Climates*.

8 A *Climate* is a Tract of the Surface of the Earth included between two such Parallels of Latitude, that the Length of the longest Day in the one, exceeds that in the other by half an Hour.

*Climates.*

The whole Surface of the Earth, is considered as being divided into 60 *Climates*, viz. from the Equator to each of the Polar Circles 24, arising from the Difference of  $\frac{1}{2}$  Hour in the Length of their longest Days; and from the Polar Circles to the Poles themselves are six, arising from the Difference of an entire Month; the Sun being seen in the first of these, a

whole Month without setting; in the Second, two; and in the Third, three Months, &c. These Climates continually decrease in Breadth the farther they are from the Equator. How they are framed, viz. the Parallel of Latitude in which they end with the respective Breadth of each of them, is shewed in the following Table.

## A TABLE of the CLIMATES.

### CLIMATES between the Equator and the Polar Circles.

Climates.	Longest Day.	Latitude Breadth.				Climates.	Longest Day.	Latitude Breadth.			
		D.	M.	D.	M.			D.	M.	D.	M.
1	12 $\frac{1}{2}$	8	25	8	25	13	18 $\frac{1}{2}$	59	58	1	29
2	13	16	25	8	00	14	19	61	18	1	20
3	13 $\frac{1}{2}$	23	50	7	25	15	19 $\frac{1}{2}$	62	25	1	07
4	14	30	20	6	30	16	20	63	22	0	57
5	14 $\frac{1}{2}$	36	28	6	08	17	20 $\frac{1}{2}$	64	06	0	44
6	15	41	22	4	54	18	21	64	49	0	43
7	15 $\frac{1}{2}$	45	29	4	07	19	21 $\frac{1}{2}$	65	21	0	32
8	16	49	01	3	32	20	22	65	47	0	26
9	16 $\frac{1}{2}$	51	58	2	57	21	22 $\frac{1}{2}$	66	06	0	19
10	17	54	27	2	29	22	23	66	20	0	14
11	17 $\frac{1}{2}$	56	37	2	10	23	23 $\frac{1}{2}$	66	28	0	08
12	18	58	29	1	52	24	24	66	31	0	03

### CLIMATES between the Polar Circles and the Poles.

Length of Days.	Latitude.	Length of Days.	Latitude.
Months.	D. M.	Months.	D. M.
1	67 21	4	78 30
2	69 48	5	84 05
3	73 37	6	90 00

## III. Of the Poetical Rising and Setting of the Stars.

The antient Poets make frequent mention of the Stars Rising and Setting, either *Cosmically*, *Achronically*, or *Heliacally*; whence these Distinctions are called *Poetical*. *Cosmical, Achronical and Heliacal Rising and Setting.*

A Star is said to *Rise* or *Set Cosmically*, (i. e. in the Morning) when it rises or sets at Sun-rising; and when it rises or sets at Sun-setting, it is said to rise or set *Achronically*, (i. e. in the Evening.) A Star *rises Heliacally*, (i. e. out of the Sun's-beams) when first it becomes visible, after it had been so near the Sun as to be hid by the Splendor of his Rays: And a Star is said to *set Heliacally*, (i. e. into the Sun's-beams) when 'tis first immersed, or hid by the Sun's Rays.

The Fixed Stars, and the three superior Planets, *Mars*, *Jupiter*, and *Saturn*, rise *Heliacally* in the Morning: But the *Moon* rises *Heliacally* in the Evening; because the Sun is swifter than the superior Planets, and slower than the Moon.

The Arch of Vision is the Arch of a Vertical Circle contained between the Horizon and the Center of the Sun after it is set, or before it riseth, this altereth according to the several Magnitudes of the Stars, for the Greater the Star is, the Less is the Arch of Vision, and the contrary.

*The Arches of Vision belonging to the Stars according to their several Magnitudes, are these.*

	D.		D.
To the First	12		To the Planets.
Second	13		Venus            5
Third	14		Mercury        10
Fourth	15		Saturn          11
Fifth	16		Jupiter        9
Sixth	17		Mars            12½
Least	18		Moon uncertain.

*Jupiter* and *Venus* when brightest may be seen by Day.

A Star is said to *rise Cosmically* when it rises with the Sun. So *Virg. Geo. L. I.*

*Candidus auratis aperit cum cornibus annum*

*Taurus*, &c. i. e. When the Sun enters *Taurus*, and they both rise at once.

A Star *sets Cosmically* when it sets at Sun-rising. So *Virg. Geo. L. I.*

*Ante tibi Eoē Atlantides abscondantur  
Debita quam sulcis committas semina, quamq;  
Invita properes anni spem credere terra.*

Harvest-Time is meant when the Sun being in Scorpio, the Pleiades set Cosmically.

A Star is said to rise Achronically, when it rises at Sun-setting.

*Et Careo vobis scythicas detrusus in oras,  
Quatuor autumnos Pleias Orta facit. Ovid.*

The Sun being in Scorpio, the Pleiades rise Achronically and set Cosmically.

A Star is said to set Achronically when it sets with the Sun: So Ovid. fast. L. 2.

*Quem modo cælatum stellis Delphina videbas  
Is fugiet visus nocte sequente tuos.*

February the 3d, When the Sun being in Aquary, the Delphin sets Achronically.

Hence, the Sign, in which the Sun is, rises Cosmically, and sets Achronically, and [the opposite Sign, at Night rises Achronically, and in the Morning sets Cosmically, according to this Distich.

*Cosmice descendit signum, quod Achronice surgit,  
Chronice descendit signum, quod Cosmice surgit.*

The Heliac rising of a Star is when the Star appears in View after having been for some Time lost in the Sun's greater Light. So Ovid. fast. L. 2.

*Iam levis obliqua subsedit Aquarius urna  
Proximus æthereos excipe Piscis equos.*

About the latter End of February.

*Ante tibi Eoē Atlantides abscondantur,  
Gnosiaque ardantis decadat stella coronæ,*

*Debita quam sulcis committas semina &c. Virg. G. 1.*

The Sun being in Scorpio, the Pleiades set Cosmically, and the Corona Septentrionalis arise Heliacally.

The Heliac Setting of a Star is when the Sun's greater Light obscures that Star.

*Candidus auratis aperit cum cornibus annum  
Taurus, & adverso cedens canis occidit astro.*

#### IV. Of the Surface of the Earth, considered as it is composed of Land and Water.

The Earth consists naturally of two Parts. Land and Water; and therefore it is called the Terraqueous Globe. Each of these Elements

Elements are subdivided into various Forms and Parts, which accordingly are distinguished by different Names.

### I. Of the Land.

The Land is distinguished into *Continents*, *Islands*, *Peninsula's*, *Isthmus's*, *Promontories*, *Mountains*, or *Coasts*.

9. A *Continent* is a large Quantity of Land, in *Continents*, which many great Countries are joined together, without being separated from each other by the Sea: Such are *Europe*, *Asia*, *Africa*, and the vast *Continent* of *America*; which four are the principal Divisions of the Earth.

A *Continent* is sometimes called the *Main Main Land*.

10. An *Island* is a Country, or Portion of Land environed round with Water: Such are *Great Britain* and *Ireland*; *Sardinia*, *Ci-  
cily*, &c. in the Mediterranean Sea; the *Isles of Wight*, *Anglesey*, &c. near *England*. Also a small Part of dry Land in the midst of a River, is called an *Island*. Sometimes a large *Island*, when compared to a lesser, is called the *Continent*; as if we compare the *Isle of Wight* to *England*, the latter may be properly called the *Continent*.

11. A *Peninsula* is a Part of Land almost environed with Water, save one narrow Neck adjoining it to the *Continent*; Or, which is almost an *Island*. Such *Denmark* joining to *Germany*; also *Africa* is properly a large *peninsula* joining to *Asia*.

12. And *Isthmus* is a narrow Neck of Land joining a *Peninsula* to the *Continent*; as the *Isthmus* of *Sue*, which joins *Africa* to *Asia*; that of *Panama* joining North and South *America*, &c.

13. A *Promontory* is a high Part of Land stretching out into the Sea; and is often called a *Cape*, *Headland*: Such is the *Cape* of *Good-Hope*, in the South of *Africa*; *La-  
pe-Finister* on the West of *Spain*; also the *Lizard-Point*, and the *Cape-  
End*, are two *Capes* or *Headlands* on the West of *England*. A *Mountain* is a high Part of Land in the Midst of a Country, over-topping adjacent Parts.

14. A *Coast* or *Shore* is that Part of Land, which borders upon the Sea, whether it be in Islands or a *Continent*: And that Part of the Land which is far distant from the Sea, is called the *Inland Country*. These are the usual Distinctions of the Land.

*A Coast or Shore*

*Inland*

The

*The Water is distinguished into Oceans, Seas, Lakes, Gulf, Streighes, and Rivers.*

*The Ocean or Main Sea.* 15. The Ocean or Main-Sea, is a vast spreading Collection of Water, not divided or separated by Land running between: Such is the *Atlantic* or *Western Ocean*, between *Europe* and *America*; the *Pacific Ocean* or *South-Sea*, &c.

Note, Those Parts of the Ocean, which border upon the Land, are called by various Names, according to those of the adjacent Countries; as the *British Sea*; the *Irish Sea*; the *French* and *Spanish Sea*.

*A Lake.* 16. A Lake is a Collection of deep standing Water, inclosed all round with Land, and not having any visible and open Communication with the Sea. But when this Lake is very large, it is commonly called a Sea, as the *Caspian Sea* in *Asia*, &c.

*A Gulf.* 17. A Gulf is a Part of the Sea, almost encompassed with Land, or, that which runs up a great Way into the Land; as the *Gulf of Venice*, &c. But if it be very large, 'tis rather called an *Inland Sea*; as the *Baltic Sea*, the *Mediterranean Sea*, the *Red Sea*, or the *Arabian Gulf*, &c. And a small Part of the Sea thus environed with Land, is usually called a *Bay*. If it be but a very small Part, or as it were, a small Arm of the Sea that runs but a few Miles between the Land, it is called a *Creek* or *Haven*.

*A Streight.* 18. A Streight is a narrow Passage lying between two Shores, whereby two Seas are joined together; as the *Streights of Dover*, between the *British Channel*, and the *German Sea*; the *Streights of Gibraltar*, between the *Atlantic* and the *Mediterranean Sea*. The *Mediterranean* it self is also sometimes called the *Streights*.

These are all the necessary Terms commonly used in *Geography*. The Names of the several Countries, Seas, and all the principal Divisions of the Earth, the Reader will find express'd upon the Terrestrial Globes. To give a tolerable Account of the Produce of each Country, the Genius of the People, their Political Institutions, &c. is properly a particular Subject of it self; and quite foreign to our Design, and therefore refer to GORDON's *Geography*, or MOLL's, for further Information therein. We shall next proceed to the Use of the Globes; but first it may not be amiss to give a short Review of their Appurtenances.

Those Circles of the Sphere that are fixed are (as has been already said) drawn upon the Globes themselves; those that are moveable, are supplied by the *Brass Meridian*, the *Wooden Horizontal*, and the *Quadrant of Altitude*.

*Brass Meridian.* 1. That Side of the *Brass Meridian*, which is divided into Degrees, represents the true *Meridian* of the

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this Side is commonly turned towards the East, and 'tis usual to place the Globe so before you, that the North be to the Right-Hand, and the South to the Left. The Meridian is divided into 4 Quadrants, each being 90 Degrees, two of which are numbered from that Part of the Equinoctial, which is above the Horizon, towards each of the Poles; the other two Quadrants are numbered from the Poles towards the Equator. The Reason why two Quadrants of the Meridian are numbered from the Equator, and the other two from the Poles, is because the Former of these two serve to shew the Distance of any Point on the Globe from the Equator, and the other to elevate the Globe to the Latitude of the Place.

2. The upper Side of the Wooden Frame, *Wooden Horizon.* called the *Wooden Horizon*, represents the true Horizon; the Circles drawn upon this Plane have been already escribed; we may observe, that the first Point of  $\text{V}$  is the *East*, and the Opposite, being the first Point of  $\text{S}$  is the *West*, the Meridian passing thro' the *North* and *South* Points.

3. The *Quadrant of Altitude* is a flexible Plate of *Quadrant of Altitude.* thin Brass, having a Nut or Screw at one End, to be fastned to the Meridian of either Globe, Occasion requires. The Edge of this Quadrant, which has Graduations upon it, called the *Fiducial Edge*, is that which is always meant, whenever we make mention of the *Quadrant of Altitude.*

4. The *Horary or Hour-Circle* is divided into twice *Hour-Circle.* twelve Hours; the two XII's coinciding with the Meridian: The uppermost XII is that at *Noon*, and the lowermost towards the Horizon is XII at *Night*. The Hours on the *East* Side of the Meridian are the *Morning Hours*, and those on the *West* Side the *Hours after Noon*. The Axis of the Globe carries round the *Hand or Index* which points the Hour, and it the Center of the Hour-Circle.

The Things above described are common to both Globes; but there are some others which are peculiar, or proper to one sort of Globe. The two *Cohures*, and the *Circles of Latitude*, from the Ecliptic, belong only to the *Celestial Globe*; also the Ecliptic itself does properly belong only to this Globe, tho' it is always drawn on the Terrestrial, for the Sake of those that might not have the other Globe by them. The Equinoctial on the Celestial Globe is always numbered into 360 Degrees, beginning at the Equinoctial Point  $\text{V}$ ; but on the Terrestrial, it is arbitrary, where these Numbers commence, according to the Meridian what Place you intend for your first; and the Degrees may be counted either quite round to 360. or both Ways, till they meet in the opposite Part of the Meridian at 180.

S E C T.

S E C T. - III.

The U S E of the G L O B E S.

*General Observations concerning the Great Circles on the Artificial Globes.*

On the Horizon seek the	Sun's Place.	Sun or Stars Declination
	Day of the Month.	
Amplitude.	Meridian Altitude.	Meridian Depression.
	Azimuth.	
Point of the Compass.	Latitude of a Place.	Distance from the Poles
	{ Rising or setting of the Stars.	
{ Distinction between Day and Night.	Zenith and Nadir Points	{ Distinction between Forenoon and After noon.
	Degrees for Hours in an Horizontal Dial.	

On the Equinoctial seek the	Right Ascension.	Sun's Place or Longitude
	Oblique Ascension.	
Oblique Descension.	{ Apparent and Annual	{ Motion.
	Ascensional Difference.	
Longitude of Places.	Stars Longitude.	{ Poetical Rising and Setting.
	Semi-diurnal { Arches.	
Semi-nocturnal { Planetary Hour.	Cusps of all the Houses	{ Increase & Decrease of Days.
	{ Distinction betwixt North and South Lat- itude of Places.	
{ Most exact and equal Measure of Time.	Culminating Degree.	Eclipses of Sun & Moon
On the Ecliptic seek the	{ Distinction of North and South Latitude of the Stars.	To try any app

Colure seek the	Spring. Autumn. { Equality of Day and Night. Distinction of North and South Decliners. Things in Trigono- tropy and Dialling.	On the Solstitial Co- lurn seek the	Summer. Winter. { Greatest Declination North and South. Longest and Shortest Days.
seek the	{ Stars Altitude at any Time. Stars Latitude. { Distance of Places or Stars. Almicanter. { Degrees of declining Dials.	On the Hour Index seek the	Hour. Also Sun's { Rising. Length of { Setting. Twilight { Day. { Night. Babilonic { Beginning. Italic { Ending. Jewish { Hour. Astronomic

## Geographical PROBLEMS.

Solv'd by the

# GLOBES.

### PROBLEM I.

To try the Globes whether they are well made or not.

SEE that the Papers unite without lapping over, and that the Parts of one and the same Circle neatly meet, without any apparent Distance or Deviation; that the Equator always

cut the Horizon in the *East* and *West* Points, and in Degrees exactly 180 asunder : Mind also, that 15 Degrees pass thro' the Meridian as the Index changes Hours : That they be well illuminated and glazed, the Images of the Constellations correspond in Figure to what they should represent : That they be corrected from the best and newest Discoveries in *Astronomy* and *Geography*, especially such Observations in the Heavens as agree with Itineraries well examin'd on Earth.

Mind that the Globe hang evenly between the Meridian and Horizon not inclining more to one Side than the other, and not too far asunder, also when the Pole is in the Zenith, let the Equinoctial be neither above nor under the Horizon in any Point. See also, that Half the Meridian be above and Half under the Horizon, so will the Degrees at the *North* and *South* Points of the Horizon always make  $90^{\circ}$ . and last of all: Let the Horizon be made strong and substantial.

### *In using them.*

Keep the *East* Side of the Horizon next, and the graduated Side of the Meridian before your Eyes, for the true Meridian is the *Eastern* graduated Face, and the upper Face of the Horizon is also the true Horizon, both which on the *Artificial Globe* have for Strength and Service some Thickness; yet in the *Natural Globe* they are *Great Circles*, without either Breadth or Depth.

**P R O B. II.** *To find the Latitude and Longitude of any given Place upon the Globe; and on the contrary, the Latitude and Longitude being given, to find the Place.*

1. Turn the Globe round its Axis, till the given Place lies exactly under the (Eastern Side of the Brass) Meridian; then that Degree upon the Meridian, which is directly over it, is the *Latitude*: Which is accordingly North or South, as it lies in the Northern or Southern Hemisphere. The Globe remaining in the same Position.

That Degree upon the Equator which is cut by the Brass Meridian, is the *Longitude* required, from the first Meridian upon the Globe. If the Longitude is counted both Ways from the first Meridian upon the Globe, then we are to consider, whether the given Place lies Easterly or Westerly from the first Meridian, and the Longitude must be expressed accordingly.

### Sect. 3. Solv'd by the Globes.

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The Latitudes of the following Places; and upon a Globe where the Longitude is reckoned both Ways from the Meridian of London, their Longitudes also will be found as follow.

	Latitude.	Longitude.
	Deg.	Deg.
Rome	41 $\frac{1}{4}$	13 East.
Paris	48 $\frac{3}{4}$	2 $\frac{1}{4}$ E.
Mexico	20 N.	102 W.
Cape-Horn	58 S.	80 W.

#### . The Latitude and Longitude being given, to find the Place.

Seek for the given Longitude in the Equator, and bring that point to the Meridian; then count from the Equator on the Meridian, the Degree of Latitude given, towards the Arctic or Antarctic Pole, according as the Latitude is Northerly or Southerly; and under that Degree of Latitude lies the Place required.

#### P R O B. III. Any Place being given, to find all those Places that are in the same Latitude with the said Place.

The Latitude of the given Place being marked upon the Meridian, turn the Globe round its Axis, and all those Places that pass under the said Mark, are in the same Latitude with the given Place, and have their Days and Nights of equal Lengths. And when any Place is brought to the Meridian, all the Inhabitants, that lie under the upper Semi-circle of it, have their Noon or Mid-day at the same Point of absolute Time exactly.

#### P R O B. IV. To find the Distance between any two given Places upon the Globe, and to find all those Places upon the Globe that are at the same Distance from a given Place.

Lay the Quadrant of Altitude over both the Places, and the Number of Degrees intercepted between them being reduced into Miles, will be the Distance required: Or, you may take

the Distance betwixt the two Places with a Pair of Compasses, and applying that Extent to the Equator, you'll have the Degrees of Distance as before. Note, A *Geographical Mile* is the  $\frac{1}{70}$ th Part of a Degree; wherefore if you multiply the Number of Degrees by 60, the Product will be the Number of Geographical Miles of Distance sought; but to reduce the same into *English Miles*, you must multiply by 70, because about 70 English Miles make a Degree of a great Circle upon the Superficies of the Earth.

Thus, the Distance betwixt *London* and *Rome* will be found to be about 13 Degrees, which is 780 Geographical Miles.

If you rectify the Globe for the Latitude and Zenith of any given Place, and bring the said Place to the Meridian; then turning the Quadrant of Altitude about, all those Places that are cut by the same Point of it, are at the same Distance from the given Place.

**P R O B. V.** *To find the Angle of Position of Places; or, the Angle formed by the Meridian of one Place, and a great Circle passing through both the Places.*

Having rectified the Globe for the Latitude and Zenith of one of the given Places, bring the said Place to the Meridian, then turn the Quadrant of Altitude about until the Fiducial Edge thereof cuts the other Place, and the Number of Degrees upon the Horizon contained between the said Edge and the Meridian, will be the Angle of Position sought.

Thus the *Angle of Position* at the *Lizard*, between the Meridian of the *Lizard* and the *Great Circle* passing from thence to *Barbadoes*, is 69 Degrees South-Westerly; but the *Angle of Position* between the same Places at *Barbadoes*, is but 38 Degrees North-Easterly.

**S C H O L I U M.**

The *Angle of Position* between two Places is a different Thing from what is meant by the *Bearings* of Places; the *Bearings* of two Places is determined by a Sort of *Spiral-Line* called a *Rhumb-Line*, passing between them in such a Manner, as to make the same or equal Angles with all the Meridians through which it passeth: But the *Angle of Position* is the very same Thing with what we call the *Azimuth* in *Astronomy*; both being formed by the Meridian and a *Great Circle* passing thro' the *Zenith* of a given Place, and a given Point, either in the Heavens, then called

called the *Azimuth*, or upon the Earth, then called the *Angle of Position*:

From hence may be shewn the Error of that *Geographical Paradox*, viz. If a Place *A* bears from another *B* due *West*, *B* shall not bear from *A* due *East*. I find this Paradox vindicated by an Author, who at the same Time gives us a true Definition of a *Rhumb-Line*: But his Arguments are *Un-geometrical*; for if it be admitted that the *East* and *West* Lines make the same Angles with all the Meridians, through which they pass, it will follow that these Lines are the Parallels of Latitude. For the Path described in Travelling from *East* to *West*, is the Continuation of the Surface of a *Cone*, whose Sides are the *Radii* of the Sphere, and *Base* the Parallel of Latitude of the Traveller: And it is evident, that all the Meridians cut the said Surface at Right (and therefore at equal) Angles; whence it follows, that the *Rhumbs* of *East* and *West* are the Parallels of Latitude; though the Case may seem different, when we draw inclining lines (like Meridians) upon Paper, without carrying our Ideas any further.

#### PROB. VI. To find the *Antæci*, *Periæci*, and *Antipodes* to any given Place.

Bring the given Place to the Meridian, and having found its Latitude, count the same Number of Degrees on the Meridian from the Equator towards the contrary Pole, and that will give the Place of the *Antæci*. The Globe being still in the same Position, set the Hour-Index to XII at Noon, then turn the Globe about till the Index points to the lower XII; the Place which then lies under the Meridian, having the same Latitude with the given Place, is the *Periæci* required. As the globe now stands, the *Antipodes* of the given Place are under the same Point of the Meridian, that its *Antæci* stood before; if you reckon 180 Degrees upon the Meridian from the given Place, that Point will be the *Antipodes*.

Let the given Place be *London* in the Latitude of  $51\frac{1}{2}$  Degrees *North*; that Place which lies under the same Meridian, and in the Latitude of  $51\frac{1}{2}$  Degrees *South*, is the *Antæci*: That which is in the same Parallel with *London*, and 180 Degrees of *Longitude* from it, is the *Periæci*; and the *Antipodes* is that Place whose *Latitude* from *London* is 180 Degrees, and *Latitude*  $51\frac{1}{2}$  Degrees *South*.

**P R O B. VII.** *The Hour of the Day at one Place, being given; to find the correspondent Hour, (or what o'Clock it is at that Time) in any other Place.*

The Difference of Time betwixt two Places is the same with their Difference of *Longitude*; wherefore having found their Difference of *Longitude*, reduce it into Time. (by allowing one Hour for every 15 Degrees, &c.) and if the Place where the

Hour is required lies  $\begin{cases} \text{Easterly,} \\ \text{Westerly,} \end{cases}$  from the Place where the Hour is given,  $\begin{cases} \text{Add,} \\ \text{Subtract,} \end{cases}$  the Difference of *Longitude* reduced into Time  $\begin{cases} \text{to,} \\ \text{from,} \end{cases}$  the Hour given; and the Sum or Remainder will accordingly be the Hour required. Or,

Having brought the Place at which the Hour is given to the Meridian, set the Hour-Index to the given Hour; then turn the Globe about until the Place where the Hour is required comes to the Meridian, and the Index will point out the Hour at the said Place.

Thus, when it is Noon at London, it is

	H. M.
Rome	52 P. M.
Constantinople	2 07 P. M.
Vera-Cruz	5 30 A. M.
Pequin in China	7 50 P. M.

**P R O B. VIII.** *The Day of the Month being given to find those Places on the Globe where the Sun will be Vertical, or in the Zenith, that Day.*

Having found the Sun's Place in the Ecliptic, bring the same to the Meridian, and note the Degree over it; then turning the Globe round, all Places that pass under that Degree will have the Sun Vertical that Day.

PROB. IX. *A Place being given in the Torrid Zone, to find those two Days in which the Sun shall be Vertical to the same.*

Bring the given Place to the Meridian; and mark what Degree of Latitude is exactly over it; then turning the Globe about those two Points of the Ecliptic, which pass exactly under the said Mark, give the Sun's Place at the Times required; look upon the Wooden-Horizon for those two Points of the Ecliptic, and right against them are the Days required.

PROB. X. *To find where the Sun is Vertical at any given Time assigned; or, the Day of the Month and the Hour at any Place (suppose London) being given, to find in what Place the Sun is Vertical at that very Time.*

Having found the Sun's Declination, and brought the first place (London) to the Meridian, set the Index to the given Hour, then turn the Globe about until the Index points to 12 at noon; which being done, that Place upon the Globe which stands under the Point of the Sun's Declination upon the Meridian, has the Sun that Moment in the Zenith.

PROB. XI. *The Day, and the Hour of the Day at one Place, being given; to find all those Places upon the Earth, where the Sun is then Rising, Setting, Culminating, (or on the Meridian;) also where it is Day-Light, Twilight, Dark-Night, Mid-night; where the Twilight then begins, and where it ends: The Height of the Sun in any Part of the illuminated Hemisphere; also his Depression in the obscure Hemisphere.*

Having found the Place where the Sun is Vertical at the given Hour, rectify the Globe for the Latitude, and bring the said Place to the Meridian.

Then

Then all those Places that are in the Western Semicircle of the Horizon, have the Sun rising at that Time.

Those in the Eastern Semicircle have it setting.

To those who live under the upper Semicircle of the Meridian, it is 12 o'Clock at Noon. And,

Those who live under the lower Semicircle of the Meridian have it Midnight.

All those Places that are above the Horizon, have the Sun above them, just so much as the Places themselves are distant from the Horizon; which Height may be known by fixing the Quadrant of Altitude in the Zenith, and laying it over any particular Place.

In all those Places that are 18 Degrees below the Western Side of the Horizon, the Twilight is just beginning in the Morning, or the Day breaks. And in all those Places that are 18 Degrees below the Eastern Side of the Horizon, the Twilight is ending, and the total Darkness beginning.

The Twilight is in all those Places whose Depression below the Horizon does not exceed 18 Degrees. And,

All those Places that are lower than 18 Degrees have day Night.

The Depression of any Place below the Horizon is equal to the Altitude of its Antipodes, which may be easily found by the Quadrant of Altitude. Of,

### *The same another Way.*

At one Position of the Globe to demonstrate where 'tis Day, where Night, where the Sun is in their Zenith, what is its Declination, where it is Morning, Noon, Evening, how and where Night comes on, and Day break appears, where 'tis continual Day or continual Night, the Hour of the Day, &c.

1. Take the Terrestrial Ball out of the Horizon, and fasten Thread to the Latitude of the Place.
2. Hang it up safe in open Sun-shine.
3. Turn its Meridian due North and South, the Help of the Compas, or rather a true Meridian-Line.
4. Bring the Place to the Meridian, consequently to the Zenith and the North Pole pointing to the North Pole in the Heavens so will the Terrestrial Globe correspond in all Respects to the Earth it self.

5. The

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5. Then with Pleasure may one behold the little *Globe*, like the big *Earth*, having one Half light, the other dark, and consequently where Day is, and where it is Night.

6. If a *Spheric Gnomon* be set in the Middle of the enlightened Hemisphere, it will project no Shadow, which demonstrates the Sun to be in the Zenith of that Place, which Place moved to the Meridian, gives the Latitude of that Place, and the present Declination of the Sun.

7. A *Spheric Gnomon* may be a Pin perpendicularly erected on a small Basis of Wood or Cork, with an hollow Bottom to stand on the *Globe*, not unlike a Coffee-cup inverted.

8. All Places then under the Meridian have their Noon or Mid-night according as they are Light or Dark: Those on the West have their Morning, for with them the Sun is East: Those on the East have their Evening, for with them the Sun is West.

9. Bring then your Place to the Meridian, and all those Places lying betwixt the enlightened and dark Half have the Sun in their Horizon Rising, if Westward off the Meridian; but Setting, if Eastward.

10. Keeping the *Globe* steady, one may see on the East, what Places grow dark, there Night comes on; and on the West, what Places grow light, there Day approaches.

11. Observe in what Degree of *Longitude* the Light is parted from the Dark Half; the Difference of *Longitude* betwixt it and the *Longitude* of any Place reduced into Time, shows how long it is to or since Sun-rise, or Sun-set, according to the Situation of the Place.

12. As many Degrees as the Sun-shine reaches beyond either North or South-Pole, so many Degrees is his Declination North or South.

13. In all Places about the Pole where it is Sun-shine, while the *Globe* is turned round, there is constant Day, till the Sun decrease in Declination.

14. In the opposite Pole where 'tis dark, while the *Globe* is turned round, there will be continual Night, till the Sun decrease in Declination.

R O B. XII. To find the Length of the longest and shortest Day and Night in any given Place, not exceeding  $66\frac{1}{2}$  Degrees of Latitude.

Note. The longest Day at all Places on the

North } Side of the Equator, is when the Sun is in the first  
South } point of Cancer: } Wherefore having rectified the Globes  
Capricorn: } for

for the Latitude, find the Time of Sun-rising and Setting, and thence the Length of the Day and Night, according to the Place of the Sun : or having rectified the Globe for the Latitude, bring the solstitial Point of that Hemisphere to the East Part of the Horizon, and set the Index to 12 at Noon ; then turning the Globe about till the said Solstitial Point touches the Western Side of the Horizon ; the Number of Hours from Noon to the Place, where the Index points (being counted according to the Motion of the Index) is the Length of the Longest Day ; the Complement wherof to 24 Hours, is the Length of the shortest Night, and the Reverse gives the shortest Day and the longest Night.

	Longest Day. Deg.	Short. Night. Hours.
Thus in Lat.	Hours.	Hours.
	45 — 15½	8½
	51½ — 16½	7½
	60 — 18½	5½

If from the Length of the longest Day, we subtract 12 Hours, the Number of Half-Hours remaining will be the *Climate*: Thus, that Place where the longest Day is 16½ Hours, lies in the 9th Climate. And by the Reverse, having the *Climate*, we have thereby the Length of the longest Day.

**P R O B. XIII.** *A Place being given in one of the Frigid Zones (suppose the Northern) to find what Number of Days (of 24 Hours each) the Sun doth constantly shine upon the same, how long he is absent, and also the first and last Day of his Appearance.*

Having rectified the Globe according to the Latitude, turn it about until some Point in the first Quadrant of the Ecliptic (because the Latitude is North) intersect the Meridian in the North Point of the Horizon ; and right against that Point of the Ecliptic on the Horizon, stands the Day of the Month when the longest Day begins.

And if the Globe be turned about till some Point in the second Quadrant of the Ecliptic cuts the Meridian in the same Point of the Horizon, it will shew the Sup's Place when the longest Day ends ; whence the Day of the Month may be found as before. Then the Number of Natural Days contain'd between the Times the longest Day begins and ends, is the Length of the longest Day required.

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Again turn the Globe about, until some Point in the third Quadrant of the Ecliptic cuts the Meridian in the *South* Part of the Horizon; that Point of the Ecliptic will give the Time when the longest Night begins. *Lastly,* Turn the Globe about until some Point in the fourth Quadrant of the Ecliptic cuts the Meridian in the *South* Point of the Horizon; and that Point of the Ecliptic will be the Place of the Sun, when the longest Night ends.

Or, the Time when the longest Day or Night begins, being known, their End may be found by counting the Number of Days from that Time to the succeeding Solstice; then counting the same Number of Days from the Solstitial Day, will give the Time when it ends.

Or, if we bring the Solstitial Point  $\odot$  to the *North* Part of the Meridian, then keep the Globe in that Position; the Place where the Ecliptic cuts the *North-Eastern* and *North Western* Parts of the Horizon, will be the Sun's Place when the longest Day begins and ends; and where it cuts the *South-Western*, and *South-Eastern* Parts of the Horizon, will be the Place of the Sun when the longest Night begins and ends.

Thus at the *North-Cape* on the Coast of *Lapland*, in the Latitude of  $71\frac{1}{2}$  Degrees, the longest Day begins about the 4th of May, and ends the 19th of July following, during the Space of 7 Days; after which, the Sun rises and sets till the 4th of November, when he but first touches the Horizon in the Southermost Point of it, and then continues below it till the 16th of January, when he'll just appear to rise in the Meridian after he had been hid below the Horizon, for the Space of 73 Natural Days, which is the Length of the longest Night. So that the longest Day is longer than the longest Night by the Space of 4 Days, which Inequality arises from the Eccentricity of the Earth's Orbit.

After the same Manner may these Things be easily found, for any Place either within the *Arctic* or *Antarctic Circle*.

*A TABLE shewing the longest Day in all Places, from the Equinoctial to the Poles of the World, viz.*

Pol. Height.	Longest Day.		Pol. Height.	Longest Day.		Pol. Height.	Longest Day, containing.	
	H.	M.		H.	M.		Days.	H.
0	12	0	47	15	42	68	42	16
6	12	20	48	15	52	69	54	16
12	12	42	49	16	0	70	64	13
16	12	58	50	16	10	71	74	00
20	13	12	51	16	20	72	82	6
24	13	26	52	16	30	73	89	4
27	13	42	53	16	42	74	96	17
30	13	56	54	16	54	75	104	01
32	14	6	55	17	08	76	110	07
34	14	16	56	17	22	77	116	14
35	14	22	57	17	36	78	122	17
36	14	28	58	17	52	79	127	9
37	14	34	59	18	10	80	134	4
38	14	38	60	18	30	81	139	1
39	14	44	61	18	54	82	145	6
40	14	52	62	19	20	83	152	2
41	14	58	63	19	50	84	156	3
42	15	4	64	20	24	85	161	5
43	15	12	65	21	10	86	166	11
44	15	18	66	22	18	87	171	21
45	15	26	66½	24	00	88	176	5
46	15	34	67	24	Days	89	181	21
						90	187	06
								39

**P R O B. XIV.** To find the Time when total Darkness ceases, or when the Twilight continues from Sun-setting to Sun-rising, in any given Place.

Let the Place be in the Northern Hemisphere; then if the Complement of the Latitude be greater than (the Depression) 18 Degrees, subtract 18 Degrees from it, and the Remainder

will be the Sun's Declination *North*, when total Darkness ceases; but if the Complement of the Latitude is less than 18 Degrees, their Difference will be the Sun's Declination *South*, when the Twilight begins to continue all Night. If the Latitude is *south*, the only Difference will be, that the Sun's Declination will be on the contrary Side.

Thus at London, when the Sun's Declination *North* is greater than  $20\frac{1}{2}$  Degrees, there is no total Darkness, but constant Twilight, which happens from the 15th of May to the 7th of July, being near two Months. Under the *North Pole* the Twilight ceases, when the Sun's Declination is greater than 18 Degrees *South*; which is from the ad of November, till the 18th of January: So that notwithstanding the Sun is absent in this Part of the World for half a Year together, yet total Darkness does not continue above 11 Weeks; and besides, the Moon is above the Horizon once a Month for a whole Fortnight, throughout the Year.

**R O B. XV.** *The Day of the Month being given, to find those Places of the Frigid Zones, where the Sun begins to shine constantly without setting; and also those Places where he begins to be totally absent.*

Bring the Sun's Place to the Meridian, and mark the Number of Degrees contained betwixt that Point and the Equator; then count the same Number of Degrees from the nearest Pole (*viz.* the *North-Pole*, if the Sun's Declination is Northerly, otherwise the *South-Pole*) towards the Equator, and note that Point upon the Meridian; then turn the Globe about, and all the Places which pass under the said Point, are those where the Sun begins to shine constantly, without setting on the given Day. If we lay the same Distance from the opposite Pole towards the Equator, and turn the Globe about, all the Places which pass under that Point, will be those where the longest Night begins.

*Or, Otherwise.*

1. Find the Sun's Declination for that Day.
2. Reckon the Number of Degrees with the Declination from the Pole towards

towards the Equator on the Meridian. 3. All the Places passing under that Degree, while the Globe is turned round, are those Places on which the Sun begins to shine or disappear, with this Distinction.

When the Declination is North increasing, the Sun begins to { Shine } in the { North } Frigid Zone.  
 to { Disappear } in the { South } Frigid Zone.

But when the Declination is South increasing, the Sun begins to { Shine } in the { South } Frigid Zone.  
 to { Disappear } in the { North } Frigid Zone.

Let the Day given be in Spring or Autumn.

**PROB. XVI.** In the Frigid Zones to find the Time of Sun-shine, and his Disappearance; also the first and last Day of his Appearance, having a Place given.

1. Find its Latitude. 2. Count how many Degrees its Latitude wants of  $90^{\circ}$ . or is distant from the Pole, which Number account the Sun's Declination both North and South, increasing and decreasing. 3. By this Declination find the Sun's Place which will be four, as is evident, by observing what Degree of the Ecliptic are cut by the Degree of Declination on the Meridian on both Sides of the Equator. 4. Against the said four Places of the Sun in the Horizon, find the four Days and Months in all the Quarters. Then observe,

If the Place be in the North Frigid Zone, the Day in the

{ Spring }	{ Quarter is the }	{ First }	{ Appearance }	{ betwixt which the Sun never Sets. }
{ Summer }		{ Last }	{ of the }	
{ Autumn }		{ First }	{ Sun's }	
{ Winter }		{ Last }	{ Disappearance }	{ betwixt which the Sun never Rises. }

But if the Place be in the South Frigid Zone, the Day in the

{ Spring }	{ Quarter is the }	{ First }	{ Disappearance }	{ betwixt which the Sun never Rises. }
{ Summer }		{ Last }	{ of the }	
{ Autumn }		{ First }	{ Sun's }	
{ Winter }		{ Last }	{ Appearance }	{ betwixt which the Sun never Sets. }

In a Table of Declination may the Days be easily found and reckoned exactly.

**PROB. XVII.** Any Number of Days less than 182, to find the Latitude, wherein the Sun setteth not, during those Days.

1. Count from ♈ on the Ecliptic so many Degrees as half the Number of Days given, save one. 2. Bring that Point where the Count ends to the Meridian. 3. The Degree of the Meridian just over it deduct from 90, the Remainder is the Latitude North; if it were required in the South Latitude; do the like from ♎, ♋, &c. as before.

## Astronomical PROBLEMS.

Solv'd by the

# GLOBES.

### PROBLEM I.

the Day of the Month being given; to find the Sun's Place in the Ecliptic, and his Declination.

**T**O find the Sun's Place: Look for the Day of the Month given in the Kalendar of Months upon the Horizon, and right against it we find that Sign and Degree of the Ecliptic which the Sun is in: The Sun's Place being thus found, look for the same in the Ecliptic Line which is drawn upon the Globe, and bring that Point to the Meridian; then that Degree of the Meridian which is directly over the Sun's Place is the Declination required, which is accordingly either North or South, as the Sun is in the Northern or Southern Signs. Thus

April

	Sun's Place.		Declination.	
	Deg.	Min.	Deg.	Min.
April 12	♈ 3	00	12	32 N.
July 20	♉ 7	51	18	20 N.
October 15	♏ 2	49	12	28 S.
January 9	♐ 9	17	20	07 S.

P R O B. II. To rectify the Globes for the Latitude  
Zenith, and the Sun's Place

1. For the Latitude: If the Place be in the Northern Hemisphere, raise the Arctic Pole above the Horizon; but for South Latitude, raise the Antarctic; then move the Meridian up and down in the Notches, until the Degrees of the Latitude counted upon the Meridian below the Pole, cuts the Horizon and then the Globe is adjusted to the Latitude.

2. To rectify the Globe for the Zenith: Having elevated the Globe according to the Latitude, count the Degrees thereof upon the Meridian from the Equator towards the elevated Pole, and the Point will be the Zenith or the Vertex of the Place: To the Point of the Meridian fasten the Quadrant of Altitude, so that the graduated Edge thereof may be joined to the said Point.

3. Bring the Sun's Place in the Ecliptic to the Meridian, and then set the Hour-Index to XII at Noon, and the Globe will be rectified to the Sun's Place.

If there be a little Mariner's Compass, the Meridian of the Globe may be easily set to the Meridian of the Place.

P R O B. III. The Day of the Month being given to shew, at one View, the Length of Day and Night in all Places upon the Earth at that Time; and to explain how the Vicissitudes of Day and Night are really made by the Motion of the Earth round its Axis in 24 Hours, the Sun standing still.

The Sun always illuminates one half of the Globe, or the Hemisphere which is next towards him, while the other remains in Darkness: And if we elevate the Globe according to the Sun's Place in the Ecliptic, it is evident, that the Sun (being at an immense Distance from the Earth) illuminates all that Hemisphere, which is above the Horizon; the Wooden

Horizon

### Sect. 3. Solv'd by the Globes.

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Horizon it self will be the Circle terminating Light and Darkness; and all those Places that are below it, are wholly deprived of the Solar Light.

The Globe standing in this Position; those Arches of the Parallels of Latitude which stand above the Horizon, are the *Diurnal Arches*, or the Length of the Day in all those Latitudes at that Time of the Year; and the remaining Parts of those Parallels, which are below the Horizon, are the *Nocturnal Arches*, or the Length of the Night in those Places. The Length of the *Diurnal Arches* may be found, by counting how many Hours are contained between the two Meridians, cutting any Parallel of Latitude, in the Eastern or Western Parts of the Horizon.

In all those Places that are in the Western Semicircle of the Horizon, the Sun appears Rising: For, the Sun standing still in the Vertex, (or above the Brass-Meridian) appears Easterly, and 90 Degrees distant from all those Places that are in the Western Semicircle of the Horizon; and therefore in those Places he is then Rising. Now if we pitch upon any particular Place upon the Globe, and bring it to the Meridian, and then bring the Hour-Index to the lower XII, which in this Case we'll suppose to be 12 at Noon, (because otherwise the Numbers upon the Hour-Circle will not answer our Purpose;) and afterwards turn the Globe about, until the aforesaid Place be brought to the Western Side of the Horizon; the Index will then shew the Time of Sun-rising in that Place. Then turning the Globe gradually about from *West* to *East*, and finding the Hour-Index; we shall see the Progress made in the Day every Hour, in all Latitudes upon the Globe, by the real Motion of the Earth round its Axis; until, by their continual Approach to the Brass-Meridian (over which the Sun stands still all the while) they at last have Noon-Day, and the Sun appears at the highest; and then by degrees, as they move Easterly, the Sun seems to decline Westward, until, as the Places successively arrive in the Eastern Part of the Horizon, the Sun appears to set in the Western; for the Places that are in the Horizon, are 90 Degrees distant from the Sun. We may observe, that all Places upon the Earth, that differ in Latitude, have their Days of different length, (except when the Sun is in the Equinoctial) being longer or shorter, in Proportion to what Part of the Parallels stand above the Horizon. Those that are in the same Latitude have their Days of the same Length; but have them commence sooner or later, according as the Places differ in Longitude.

H

P R O B.

**P R O B. IV.** To explain in general the Alteration of Seasons, or Length of the Days and Nights, made in all Places of the World, by the Sun's (or the Earth's) annual Motion in the Ecliptic.

It has been shewn in the last *Problem*, how to place the Globe in such a Position, as to exhibit the Length of the *Diurnal* and *Nocturnal Arches*, in all Places of the Earth, at a particular Time: If the Hour-Circle be taken off, so that the Poles of the Globe may be brought to the Horizon; and the Globe be continually rectified, according as the Sun alters his Declination, (which may be known by bringing each Degree of the Ecliptic successively to the Meridian) we see the gradual Increase or Decrease made in the Days in all Places of the World according as a greater or lesser Portion of the Parallels of Latitude stand above the Horizon. We shall illustrate this *Problem* by Examples taken at different Times of the Year.

1. Let the Sun be in the first Point of  $\text{\textcircled{S}}$ , (which happens on the 10th of June) that Point being brought to the Meridian will shew the Sun's Declination to be  $23\frac{1}{2}$  Degrees North; then the Globe must be rectified to the Latitude of  $23\frac{1}{2}$  Degrees, and for the better Illustration of the *Problem*, let the first Meridian upon the Globe be brought under the Brass Meridian. The Globe being in this Position, we see at one View the Length of the Days in all Latitudes, by counting the Number of Hours contained between the two extreme Meridians, cutting any particular Parallel we pitch upon, in the Eastern and Western Part of the Horizon. And we may observe that the lower Part of the Arctic Circle just touches the Horizon, and consequently all the People who live in that Latitude have the Sun above their Horizon for the Space of 24 Hours, without setting; only when it is in the lower Part of the Meridian (which they would call 12 at Night) he just touches the Horizon.

To all those who live between the Arctic Circle and the Pole, the Sun does not set, and its Height above the Horizon, when he is in the lower Part of the Meridian, is equal to their Distance from the Arctic Circle: For Example, Those who live in the 80th Parallel have the Sun, when he is lowest, at this Time  $13\frac{1}{2}$  Degrees high.

If we cast our Eye Southward, towards the Equator, we shall find, that the Diurnal Arches, or the Length of the Day in the several Latitudes, gradually lessen: The Diurnal Arch

### Sect. 3. Solv'd by the Globes.

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If the Parallel of London at this Time is  $16\frac{1}{2}$  Hours; that of the Equator (is always) 12 Hours; and so continually less, till we come to the Antarctic Circle, the upper Part of which just touches the Horizon; and those who live in this Latitude, have just one sight of the Sun, peeping as it were in the Horizon, and all that Space between the Antarctic Circle and the South Pole, lies in total Darkness.

If from this Position we gradually move the Meridian of the Globe, according to the progressive Alterations made in the Sun's Declination, by his Motion in the Ecliptic; we shall find the Diurnal Arches of all those Parallels, that are on the Northern Side of the Equator continually decrease; and those on the Southern Side continually increase, in the same Manner as the Days in those Places shorten and lengthen. Let us again observe the Globe, when the Sun has got within 10 Degrees of the Equinoctial; now the lower Part of the 60th Parallel of North Latitude just touches the Horizon, and all the Space betwixt this and the Pole, falls in the illuminated Hemisphere; but all those Parallels that lie betwixt this and the Arctic Circle, which before were wholly above the Horizon, do now intersect it, and the Sun appears to them to rise and set. From hence to the Equator, we shall find that the Days have gradually shortened; and from the Equator southward, they have gradually lengthened, until we come to the 80th Parallel of South Latitude; the upper Part of which just touches the Horizon, and all Places betwixt this and the South Pole are in total Darkness: But those Parallels betwixt this and the Antarctic Circle, which before were wholly above the Horizon, are now partly above it; the Length of their Days being exactly equal to that of the Nights in the same Latitude in the contrary Hemisphere. This also holds universally, that the Length of the Day in one Latitude North, is exactly equal to the Length of the Night in the same Latitude South; and vice versa.

Let us again follow the Motion of the Sun, until he has got to the Equinoctial, and take a View of the Globe while it is in this Position. Now all the Parallels of Latitude are cut into two equal Parts by the Horizon, and consequently the Days and Nights are of equal Lengths. viz. 12 Hours each in all Places of the World; the Sun rising and setting at Six Clock, excepting under the two Poles, which now lie exactly in the Horizon: Here the Sun seems to stand still in the same Point of the Heavens for some Time, until by Degrees, by his Motion in the Ecliptic, he ascends higher to one, and disappears to the other, there being properly no Days and Nights

under the Poles ; for there the Motion of the Earth round its Axis can't be observed.

If we follow the Motion of the Sun towards the Southern Tropic, we shall see the Diurnal Arches of the Northern Parallels continually decrease, and the Southern ones increase in the same Proportion, according to their respective Latitudes. The North Pole continually descending, and the South Pole ascending above the Horizon, until the Sun arrives into  $\textcircled{w}$ , at which Time, all the Space within the Antarctic Circle is above the Horizon ; while the Space between the Arctic Circle and its Neighbouring Pole, is in total Darkness. And we shall now find all other Circumstances quite reverse to what they were when the Sun was in  $\textcircled{s}$  ; the Nights now all over the World being of the same Length that the Days were of before.

We have now got to the Extremity of the Sun's Declination ; and if we follow him thro' the other half of the Ecliptic, and rectify the Globe accordingly, we shall find the Seasons return in their Order, until at length we bring the Globe into its first Position.

**P R O B. V.** *To shew by the Globe, at one View, the Length of the Days and Nights in any particular Place, at all Times of the Year.*

Because the Sun by his Motion in the Ecliptic, alters his Declination a small Matter every Day ; if we suppose all the Torrid Zone to be filled up with a Spiral Line, having so many Turnings ; or a Screw having so many Threads, as the Sun is Days in going from one Tropic to the other ; and these Threads at the same Distance from one another in all Places, as the Sun alters his Declination in one Day in those Places respectively. This Spiral Line or Screw will represent the apparent Paths described by the Sun round the Earth every Day ; and by following the Thread from one Tropic to the other, and back again, we shall have the Path the Sun seems to describe round the Earth in a Year. But because the Inclinations of these Threads to one another are but small, we may suppose each Diurnal Path to be one of the Parallels of Latitude, drawn, or supposed to be drawn upon the Globe. Thus much being premised, we shall explain this Problem, by placing the Globe according to some of the most remarkable Positions of it ; as before we did for the most remarkable Seasons of the Year.

In the preceding Problem, the Globe being rectified according to the Sun's Declination, the upper Parts of the Parallels of Latitude, represented the *Diurnal Arches*, or the Length of the Days all over the World at that particular Time: Here we are to rectify the Globe according to the Latitude of the Place, and then the upper Parts of the Parallels of Declination are the *Diurnal Arches*; and the Length of the Days at all Times of the Year, may be here determined, by finding the Number of Hours contained between the two extreme Meridians, which cut any Parallel of Declination, in the Eastern and Western Points of the Horizon; after the same Manner as before we found the Length of the Day in the several Latitudes at a particular Time of the Year.

1. Let the Place proposed be under the Equinoctial, and let the Globe be accordingly rectified for 00 Degrees of Latitude, which is called a direct Position of the Sphere. Here all the Parallels of Latitude, which in this Case we'll call the Parallels of Declination, are cut by the Horizon into two equal parts; and consequently those who live under the Equinoctial have the Days and Nights of the same Length at all Times of the Year; also in this Part of the Earth, all the Stars rise and set, and their Continuance above the Horizon, is equal to their Stay below it, viz. 12 Hours.

If from this Position we gradually move the Globe according to the several Alterations of Latitudes, which we will suppose to be Northerly; the Lengths of the Diurnal Arches will continually increase, until we come to a Parallel of Declination, as far distant from the Equinoctial, as the Place itself is from the Pole. This Parallel will just touch the Horizon, and all the Heavenly Bodies that are betwixt it and the Pole never descend below the Horizon. In the mean Time, while we are moving the Globe, the Lengths of the Diurnal Arches of the Southern Parallels of Declination, continually diminish in the same Proportion that the Northern ones increased; until we come to that Parallel of Declination which is so far distant from the Equinoctial Southerly, as the Place itself is from the North Pole. The upper Part of this Parallel just touches the Horizon, and all the Stars that are betwixt it and the South Pole, never appear above the Horizon. All the Diurnal Arches of the Southern Parallels of Declination, are exactly of the same Length with the Diurnal Arches of the correspondent Parallels of North Declination.

2. Let us take a View of the Globe, when it is rectified for the Latitude of London, or  $51\frac{1}{2}$  Degrees North. When the Sun is in the Tropic of  $\text{\textcircled{S}}$ , the Day is about  $16\frac{1}{2}$  Hours; as he removes from this Tropic, the Days proportionably shorten, until

til he arrives into  $\text{V}^{\circ}$ , and then the Days are at the shortest being now of the same Length with the Night when the Sun was in  $\text{G}$ , viz.  $7\frac{1}{2}$  Hours. The lower Part of that Parallel of Declination, which is  $38\frac{1}{2}$  Degrees from the Equinoctial Northerly, just touches the Horizon; and all the Stars that are betwixt this Parallel and the *North Pole*, never set to  $\text{N}$  at London. In like Manner the upper Part of the Southern Parallel of  $38\frac{1}{2}$  Degrees just touches the Horizon, and all the Stars that lie betwixt this Parallel and the *South Pole* are never visible in this Latitude.

Again, let us rectify the Globe for the Latitude of the *Aries Circle*, we shall then find, that when the Sun is in  $\text{G}$ , he touches the Horizon on that Day, without setting, being 24 Hours complete above the Horizon; and when he is in *Capricorn*, he once appears in the Horizon, but does not rise for the Space of 24 Hours: When he is in any other Point of the Ecliptic the Days are longer or shorter, according to his Distance from the Tropics. All the Stars that lie between the Tropic of *Cancer*, and the *North Pole*, never set in this Latitude; and those that are between the Tropic of *Capricorn* and the *South Pole*, are always hid below the Horizon.

If we elevate the Globe still higher, the Circle of *perpetual Apparition* will be nearer the Equator, as will that of *perpetual Occultation* on the other Side. For Example, Let us rectify the Globe for the Latitude of  $80^{\circ}$  Degrees *North*; when the Sun's Declination is  $10^{\circ}$  Degrees *North*, he begins to turn above the Horizon without setting, and all the while he is making his Progress from this Point to the Tropic of  $\text{G}$ , and back again, never sets. After the same Manner, when his Declination is  $10^{\circ}$  Degrees *South*, he is just seen at Noon in the Horizon; and all the while he is going Southward, and back again, he disappears, being hid just so long as before, at the opposite Time of the Year, he appeared visible.

Let us now bring the *North Pole* into the Zenith, then will the Equinoctial coincide with the Horizon; and consequently all the Northern Parallels are above the Horizon, and the Southern ones below it. Here is but one Day and one Night throughout the Year; it being Day all the while the Sun is to the Northward of the Equinoctial, and Night for the other half Year. All the Stars that have *North Declination* always appear above the Horizon, and at the same Height; and those that are on the other Side, are never seen.

What has been here said of rectifying the Globe to *North Latitude*, holds for the same Latitude *South*; only that before the longest Days were, when the Sun was in  $\text{G}$ : the same happening now when the Sun is in  $\text{V}^{\circ}$ ; and so of the rest of the Parallels.

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llels, the Seasons being directly opposite to those who live in different Hemispheres.

The three foregoing Problems are very useful, as they give a general Idea how the Seasons are altered in all Places of the World, and do very well deserve the particular Attention of the Reader; it being undoubtedly entertaining, to know how these Things are brought about by the regular Course of Nature.

For the Sake of the Reader, I shall explain some Things delivered above in general Terms, by particular Problems.

But from what has been already said, we may first make the following Observations.

1. All Places of the Earth do equally enjoy the Benefit of the Sun, in respect of Time, and are equally deprived of it; the Days at one Time of Year being exactly equal to the Nights at the opposite Season.
2. In all Places of the Earth, save exactly under the Poles, the Days and Nights are of equal Length, (viz. 12 Hours each) when the Sun is in Equinoctial.
3. Those who live under the Equinoctial, have the Days and Nights of equal Lengths, at all Times of the Year.
4. In all Places between the Equinoctial and the Poles, the Days and Nights are never equal, but when the Sun is in the Equinoctial Points V, &.
5. The nearer any Place is to the Equator, the less is the Difference between Length of the Artificial Days and Nights in the said Place; and the more remote, the Greater.
6. To all the Inhabitants lying under the same Parallel of Latitude, the Days and Nights are of equal Lengths, and that at all Times of the Year.
7. The Sun is Vertical twice a Year, to all Places between the Tropics; to once under the Tropics, once a Year, but never anywhere else.
8. In all Places between the Polar Circles, and the Poles, the Sun appears the Number of Days without setting; and at the opposite Time of the Year, is for the same Length of Time without rising: and the nearer unto, or the remote from the Pole, those Places are, the longer or shorter is the continued Presence in, or Absence from the same.
9. In all Places lying exactly under the Polar Circles, the Sun, when he is in the nearest Tropic, appears 24 Hours without setting; and when he is in the contrary Tropic, he is for the same length of Time without rising; at all other Times of the Year he rises and sets there, as in other Places.
10. In all Places lying in the { Northern Southern } Hemisphere, the longest Day, and shortest Night, is when the Sun is in the { Northern Southern } Tropic; and the contrary.

P R O B.

**P R O B. VI.** *The Latitude of any Place, not exceeding  $66\frac{1}{2}$  Degrees, and the Day of the Month being given, to find the Time of Sun-rising and setting and the Length of the Day and Night.*

Having rectified the Globe according to the Latitude, bring the Sun's Place to the Meridian, and put the Hour-Index to 12 at Noon; then bring the Sun's Place to the Eastern Part of the Horizon, and the Index will shew the Time when the Sun rises. Again, turn the Globe until the Sun's Place be brought to the Western Side of the Horizon, and the Index will shew the Time of Sun-setting.

The Hour of Sun-setting doubled, gives the Length of the Day; and the Hour of Sun-rising doubled, gives the Length of the Night.

Let it be required to find when the Sun rises and sets at London on the 20th of April. Rectify the Globe for the Latitude of London, and having found the Sun's Place, corresponding April the 20th, viz.  $\textcircled{S} 10\frac{1}{4}$  Degree, bring  $\textcircled{S} 10\frac{1}{4}$  Degrees to the Meridian, and set the Index to 12 at Noon; then turn the Globe about till  $\textcircled{S} 10\frac{1}{4}$  Degrees be brought to the Eastern Part of the Horizon, and we'll find the Index point  $4\frac{1}{2}$  Hours; this being doubled, gives the Length of the Night  $9\frac{1}{2}$  Hours. Again, bring the Sun's Place to the Western Part of the Horizon, and the Index will point  $7\frac{1}{2}$  Hours, which is the Time of Sun-setting; this being doubled, gives the Length of the Day  $14\frac{1}{2}$  Hours.

**P R O B. VII.** *To find in what Latitude the long Day is, of any given Length less than 24 Hours.*

Bring the Solstitial Point to the Meridian, and set the Index to 12 at Noon; then turn the Globe Westward till the Index points at half the Number of Hours given: Which being done, keep the Globe from turning round its Axis, and leave the Meridian up or down in the Notches, till the Solstitial Point comes to the Horizon, then that Elevation of the Point will be the Latitude.

If the Hours given be 16, the Latitude is 49 Degrees; if 18 Hours, the Latitude is  $63\frac{1}{4}$  Degrees.

**P R O B. VIII.** To find in what Latitude the longest Day is of any given Length less than 182 Natural Days, in the Frigid Zones.

Find a Point in the Ecliptic, half so many Degrees distant from the Solstitial Point, as there are Days given, and bring that Point to the Meridian; then keep the Globe from turning round its Axis, and move the Meridian up or down until the foresaid Point of the Ecliptic comes to the Horizon: That elevation of the Pole will be the Latitude required.

If the Days given were 78, the Latitude is  $71\frac{1}{2}$  Degrees. This Method is not accurate, because the Degrees in the Ecliptic do not correspond to Natural Days; and also because the Sun does not always move in the Ecliptic at the same rate; however such Problems as these may serve for Amusements.

**P R O B. IX.** Concerning the Equation of Civil Days; and to find how much any Number of Days in one Month is longer or shorter, than the like Number of Days in another Month, even by the Globe.

That one Day is longer than another, proceeds from 2 Causes 1st, The Sun's apparent Motion is unequal, being slower in *pogee* than in *Perigee*; in the First, scarce moving 58° daily, in the other above 61°.

The Second is the Difference of Right Ascension, answerable to equal Parts of the Ecliptic, being far greater about the Tropics than the Equinoxes.

Now, then suppose the given Number of Days were 20 in two different Months.

Find the Sun's Places for the Beginning and End of each 20 Days, which will give four Points on the Ecliptic, answerable to which, find the Right Ascensions of the four Points foresaid, then subtract the Right Ascension of the Beginning from the Right Ascension of the Ending of those Days respectively, if the Remains be equal, then are each 20 Days equal to the other: But if one Remainder be greater than the other find their Difference, and change those Degrees and Minutes of Difference of Right Ascension into Time, by allowing 4 minutes for every Degree, so will be found the Difference in Time, being one 20 Days are longer than the other.

**Prob. X.** *The Day of the Month being given, to find when the Morning and Evening Twilight begins and ends, in any Place upon the Globe.*

In the foregoing *Problems*, by the Length of the Day, meant the Time from Sun-rising to Sun-set; and the Night reckoned from Sun-set till he rose next Morning. But it is found by Experience, that total Darkness does not commence in the Evening, till the Sun has got 18 Degrees below the Horizon; and when he comes within the same Distance of the Horizon next Morning, we have the first *Dawn of Day*. This faint Light which we have in the Morning and Evening before and after the Sun's rising and setting, is what we call the *Twilight*.

**Prob. II.** Having rectified the Globe for the Latitude, the Zenith, and the Sun's Place; turn the Globe, and the Quadrant of Altitude until the Sun's Place cuts 18 Degrees below the Horizon, (if the Quadrant reaches so far) then the Index upon the Hour-Circle will shew the Beginning or Ending of Twilight, after the same Manner, as before we found the Time of Sun-rising and setting, in *Prob. 6.* But by Reason of the Thickness of the Wooden-Horizon, we can't conveniently see, or compute when the Sun's Place is brought to the Point aforesaid. Wherefore the Globe being rectified above directed, turn the Globe, and also the Quadrant of Altitude Westward, until that Point in the Ecliptic, which is opposite to the Sun's Place, cuts the Quadrant in the 18th Degree above the Horizon; then the Hour-Index will shew the Time, when Day breaks in the Morning. And if we turn the Globe and the Quadrant of Altitude, until the Point opposite to the Sun's Place cuts the Quadrant in the 18th Degree in the Eastern Hemisphere; the Hour-Hand will shew, when Twilight ends in the Evening. Or, having found the Time from Midnight when the Morning Twilight begins, if we reckon so many Hours before Midnight, it will give the Time when the Evening Twilight ends. Having found the Time when Twilight begins in the Morning, find the Time of Sun-rising, by *Prob. 6.* and the Difference will be the Duration of Twilight.

Thus at London, on the first of May, Twilight begins at three Quarters past One o'Clock; the Sun rises at about half an Hour past Four; whence the Duration of Twilight then is two Hours, both in the Morning and Evening. On the first of November,

November

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November, the Twilight begins at half an Hour past Six, being somewhat above an Hour before Sunrising.

#### PROB. XI. To find the Sun's Altitude when it shines, by the Globe.

Having set the Frame of the Globe truly horizontal or level, turn the North Pole towards the Sun, and move the Meridian up or down on the Notches, till the Axis casts no Shadow; then the Arch of the Meridian, contained betwixt the Pole and the Horizon, is the Sun's Altitude.

Note. The best Way to find the Sun's Altitude, is by a little Quadrant graduated into Degrees, and having Sights and a Plummeter to it: Thus, hold the Quadrant in your Hands, so as the Rays of the Sun may pass thro' both the Sights; the Plummeter then hanging freely by the Side of the Instrument, will tell in the Limb the Altitude required. These Quadrants are to be had at the Instrument-Makers, with Lines drawn upon them; for finding the Hour of the Day, and the Azimuth, with several other pretty Conclusions, very entertaining for Beginners.

#### PROB. XII. To find in what Place else, the Sun bath the same Altitude with us, at the same Time.

This is two-fold: First, When the Sun is on the Meridian; secondly, When not.

I. When the Sun is on our Meridian, observe what Place is exactly under the Declination of the Sun, when the Globe is rectified, and the Place brought to the Zenith, to this Place will you find rectify the Globe, as before, then turn about the Quadrant, all the Places that pass under any one Degree of the Quadrant have the Sun that same Number of Degrees high.

But when the Sun is not on our Meridian, rectify the Globe, and turn it about till the Index point at our present Hour. Pitch one Foot of a Pair of Compasses in the Sun's Place, extending the other to the Zenith Point on the Meridian. Turn about that Foot back, till it touch the Meridian on some Degree, which is the Latitude of the other Place, and the Longitude is the same as ours.

Before I conclude this, I shall detect one vulgar Error in Astronomy. Tho' 'tis true that the Sun comes to the Meridian

of a Place different in Longitude 15 Degrees West from Dublin exactly one Hour later, but 'tis not always, and exactly true on any other Hour or Azimuth if the Latitude differ.

Now follows an *Example*, plainly elucidating the Truth hereof.

Here the Sun, when in  $\odot$ , rises at half an Hour past 3. Now supposing a Place in Latitude 10 Degrees, but differing in Longitude from Dublin 90 Degrees, then and there the Sun rises about three Quarters past 5, unto which add Six Hours, the Difference in Time betwixt the Meridians of the two Places gives three Quarters past 11 with us, when the Sun rises there which is no less than 8 Hours and a Quarter after Sun-rise with us, whereas many believe it to be exactly 6 Hours after Sun-rise with us, but are mistaken full 2 Hours and a Quarter, and would, whether the Longitude differ or not more or less wherefore have respect to the Latitude, when Questions of the Sun's present Altitude, Azimuth, Rising and Setting in other Places is required.

**P R O B. XIII. *The Latitude, and the Day of the Month being given, to find the Hour of the Day when the Sun shines.***

Having placed the Wooden Frame upon a Level, and the Meridian due North and South, rectify the Globe for the Latitude, and fix a Needle perpendicularly over the Sun's Place. The Sun's Place being brought to the Meridian, set the Hour Index to 12 at Noon, then turn the Globe about until the Needle points exactly to the Sun, and casts no Shadow. and then the Index will shew the Hour of the Day.

**P R O B. XIV. *The Sun's Azimuth being given, to place the Meridian of the Globe due North and South, or to find a Meridian Line, when the Sun shines..***

Let the Sun's Azimuth be 30 Degrees South-Easterly, set the Horizon of the Globe upon a Level, and bring the North Pole into the Zenith; then turn the Horizon about, until the Shade of the Axis cuts as many Hours as is equivalent to the Azimuth, (allowing 15 Degrees to an Hour) in the North-West Part of the Hour-Circle; viz. X at Night; which being done, the Meridian of the Globe stands in the true Meridian of the Place.

place. The Globe standing in this Position, if we hang two Plummets at the North and South Points of the Wooden Horizon, and draw a Line betwixt them, we'll have a Meridian Line; which if it be on a fixed Plane (as a Floor or Window) it will be a Guide for placing the Globe due North and South at any other Time.

PROB. XV. *The Latitude, Hour of the Day, and the Sun's Place being given, to find the Sun's Altitude and Azimuth.*

Rectify the Globe for the Latitude, the Zenith, and the Sun's Place; then the Number of Degrees contained betwixt the Sun's Place and the Vertex is the Sun's Meridional Zenith-Distance; the Complement of which, to 90 Degrees, is the Sun's Meridian Altitude. If we turn the Globe about until the Index points at any other given Hour, then bringing the Quadrant of Altitude to cut the Sun's Place, we'll have the Sun's Altitude at that Hour; and where the Quadrant cuts the Horizon, is the Sun's Azimuth at the same Time. Thus May the 1st at London, the Sun's Meridian Altitude will be  $61\frac{1}{2}$  Degrees; and at 10 o'Clock in the Morning, the Sun's Altitude will be 52 Degrees; and his Azimuth about 50 Degrees from the South Part of the Meridian.

PROB. XVI. *The Latitude of the Place, and the Day of the Month being given; to find the Depression of the Sun below the Horizon, and his Azimuth at any Hour of the Night.*

Having rectified the Globe for the Latitude, the Zenith, and the Sun's Place; take a Point in the Ecliptic, exactly opposite to the Sun's Place, and find the Sun's Altitude, and Azimuth, as by the last Problem; and these will be the Depression and the Altitude required. Thus, If the Time given be the 1st of November, at 10 o'Clock at Night, the Depression and Azimuth will be the same as was found in the last Problem.

**PROB. XVII.** *The Declination and Meridian Altitude of the Sun, or of any Star being given; to find the Latitude of the Place,*

Mark the Point of Declination upon the Meridian, according as it is either *North* or *South*, from the Equator; then slide the Meridian up or down in the Notches, till the Point of Declination be so far distant from the Horizon, as is the given Meridian Altitude; that Elevation of the Pole will be the Latitude.

Thus, If the Sun's, or any Star's Meridian Altitude be 11 $\frac{1}{2}$  Degrees *South*, and its Declination 11 $\frac{1}{2}$  Degrees *North*, the Latitude will be 31 $\frac{1}{2}$  Degrees *North*.

**PROB. XVIII.** *Two known Stars having the same Azimuth, or the same Height, being given; to find the Hour of the Night.*

Rectify the Globe for the Latitude, the Zenith, and the Sun's Place.

1. When the two Stars are in the same Azimuth. Turn the Globe, and also the Quadrant about, until both the Stars coincide with the Edge thereof; then will the Index shew the Hour of the Night: And where the Quadrant cuts the Horizon, is the common Azimuth of both Stars.

2. If the two Stars are of the same Altitude, move the Globe so, that the same Degree on the Quadrant will be over both Stars; then the Index will shew the Hour.

This Problem is useful when the Quantity of the Azimuth of the two Stars, in the first Case, or of their Altitude in the latter Case, is not known.

**PROB. XIX.** *The Latitude, Day of the Month, and the Altitude of any known Star being given; to find the Hour of the Night.*

Rectify the Globe for the Latitude, Zenith, and the Sun's Place: Turn the Globe, and the Quadrant of Altitude, backward or forward, till the Center of that Star meets the Quadrant in the Degree of Altitude given; then the Index will point the true Hour of the Night; and also where the Qua-

Quadrant cuts the Horizon, will be the Azimuth of the Star at that Time.

**R O B. XX.** If the Latitude, Sun's Altitude, and his Declination (instead of his Place in the Ecliptic) are given; to find the Hour of the Day and Azimuth.

Rectify the Globe for the Latitude and Zenith; and having brought the Equinoctial Colure to the Meridian, set the Index to 12 at Noon: Which being done, turn the Globe and the Quadrant, until the given Declination in the Equinoctial Colure puts the Altitude on the Quadrant; then the Index will shew the Hour of the Day, and the Quadrant cut the Azimuth in the Horizon.

**R O B. XXI.** The Day and Hour of a Lunar or Solar Eclipse being known; to find all those Places upon the Globe in which the same will be visible.

Find where the Sun is Vertical at the given Hour, and bring that Point to the Zenith; then the Eclipse will be visible in all those Places that are under the Horizon: Or, if we bring the Antipodes to the Place where the Sun is Vertical, into the Zenith, we'll have the Places where the Eclipse will be visible above the Horizon.

Note, Because Lunar Eclipses continue sometimes for a long while together, they may be seen in more Places than one Hemisphere of the Earth; for by the Earth's Motion round its Axis, during the Time of the Eclipse, the Moon will rise in several Places after the Eclipse began.

Or, more exactly thus.

Having found the Declination of the Sun, elevate that Pole of the Globe which is most remote from the Sun, till its Height be equal to the Sun's Declination, convert the Time of the beginning of the Eclipse from Noon into Degrees and Minutes, and if the Hour given be between Noon and Midnight, subtract it from the Longitude of the given Place to which it is computed; but if it happen between Midnight and the succeeding Noon, add to it the Longitude of the given Place, and bring the Point in the Equinoctial opposite to this to the Meridian, then a Line drawn by the Eastern Edge of the Horizon, will pass thro' all those Places where the Moon appears to begin to be eclipsed at her setting; and if from the

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Degree of the Equator then under the Meridian, be subtracted the Duration of the Eclipse reduced into Time, and the Globe be turn'd about, till that degree under the Equinoctial come to the Meridian, a Line drawn by the Western Edge of the Horizon will pass thro' all those Places where the Eclipse will end, at the Time of the Moon's Rising, and consequently within all that Tract of the Earth's Superficies will the Eclipse be visible.

### *But for a Solar Eclipse.*

When an Eclipse of the Sun is Central, if we bring the Place where the Sun is Vertical at that Time, into the Zenith, some Part of the Eclipse will be visible in most Places within the upper Hemisphere: But by reason of the short Duration of Solar Eclipses, and the Latitude which the Moon commonly has at that Time, (tho' but small) there is no certainty in determining the Places where those Eclipses will be visible, by the Globe; but recourse must be had to Calculations. Howbeit, by the Globes we thus come to a near Approximation.

*First, Say, As the Semidiameter of the Earth's Disk seen from the Moon : is to 89 Degrees :: So is the Arch between the Centers of the Umbra and Penumbra : to the Degree of a great Circle belonging to it :: And is the Semidiameter of the Penumbra : to its Degrees.*

2. Then bring to the Meridian the Place lying vertical under the Sun, and from thence South or North, according to the Moon's Latitude, number as many Degrees as answer to the Arch between the Centers first found, the End of this Number gives the Place of the Earth lying in the Center of the Penumbra. 3. In this Center set one Foot of the Compass and the other Foot being turned about at the Distance of a Degree answering to the Semidiameter of the Penumbra aforesaid, shews that all those Parts of the Earth included within its Ambit are to suffer the Eclipse; and consequently will see an apparent one in the Sun. A greater Eclipse the nearer they lie to the Center of the Penumbra aforesaid: But if this Semidiameter of the Penumbra on the Globe be divided into 12 equal Parts, thro' which, if Concentric Circles be drawn, then may the Digits of the Eclipse in those Places be estimated, where the Center falls is either a total or annular Eclipse: In the Circle next it is an Eclipse of 11 Digits, of that, of 10, next that, of 9 Digits, and so on.

R. O. B. XXII. To find all that Space upon the Earth, where an Eclipse of one of the Satellites of Jupiter will be visible.

Having found that Place upon the Earth, in which the Sun is Vertical, at the Time of the Eclipse. Elevate the Globe according to the Latitude of the said Place; then bring the Place to the Meridian, and set the Hour-Index to 12 at Noon. If Jupiter be in Consequence of the Sun, draw a Line with Jack-Lead, or the like, along the Eastern Side of the Horizon, which Line will pass over all those Places where the Sun is setting at that Time: Then count the Difference betwixt the Right Ascension of the Sun, and that of Jupiter; and turn the Globe Westward, until the Hour-Index points to this Difference; then keep the Globe from turning round its Axis, and elevate the Meridian, according to the Declination of Jupiter. The Globe being in this Position, draw a Line along the Eastern Side of the Horizon, then the Space between this Line, and the Line before drawn, will comprehend all those Places of the Earth, where Jupiter will be visible, from the setting of the Sun, to the setting of Jupiter.

But if Jupiter be in Antecedence of the Sun, (i. e. rises before him) having brought the Place where the Sun is Vertical, to the Zenith, and put the Hour-Index to 12 at Noon, draw a Line on the Western Side of the Horizon; then elevate the same according to the Declination of Jupiter, and turn it about Eastwards, until the Index points to so many Hours distant from Noon, as is the Difference of Right Ascension of the Sun and Jupiter. The Globe being in this Position, draw a Line along the Western Side of the Horizon; then the Space contained between this Line, and the other last drawn, will comprehend all those Places upon the Earth, where the Eclipse will be visible, between the Rising of the Sun and Jupiter.

R. O. B. XXIII. To find the Right Ascension and Declination of the Sun or any Fixed Star.

Bring the Sun's Place in the Ecliptic to the Meridian, then the Degree of the Equator, which is cut by the Meridian, will be the Sun's Right Ascension; and that Degree of the Meridian, which is exactly over the Sun's Place, is the Sun's Declination. After the same Manner, bring the Place of any Fixed Star to

the Meridian, and we'll find its Right Ascension in the Equinoctial, and Declination on the Meridian.

Thus, the Right Ascension and Declination is found, after the same Manner as the Longitude and Latitude of a Place upon the Terrestrial Globe.

Note, The Right Ascension and Declination of the Sun vary every Day; but the Right Ascension, &c. of the Fixed Stars is the same throughout the Year. \*

	The Sun's Right Ascension.	Declination.
	Deg.	Deg.
January	20	17 $\frac{1}{2}$
March	23	6
July	10	20 $\frac{1}{2}$
November 15	242	21

	Right Ascension.	Declination.
	Deg.	Deg.
Aldebaran	—	6 $\frac{1}{2}$
Spica Virginis	—	197 $\frac{1}{4}$
Cafella	—	74 $\frac{1}{2}$
Syrius, or the Dog-Star	—	98 $\frac{1}{4}$

Note, The Declination of the Sun may be found after the same Manner, by the Terrestrial Globe; and also his Right Ascension, when the Equinoctial is numbered into 360 Degrees, commencing at the Equinoctial Point V.

By the Converse of this Problem, having the Right Ascension and Declination of any Point given, that Point it self may easily found upon the Globe.

#### P R O B. XXIV. To find the Longitude and Latitude of a given Star.

Having brought the Solstitial Colure to the Meridian, the Quadrant of Altitude over the proper Pole of the Ecliptic, whether it be North or South; then turn the Quadrant over the given Star; and the Arch contained betwixt the Star and the Ecliptic, will be the Latitude, and the Degree cut on the Ecliptic will be the Star's Longitude.

\* The insensible Change in the Longitude, Right Ascension, and Declination of the Fixed Stars, made by their slow Motion, parallel to the Ecliptic (being but 1 Degree in 72 Years) is not worth Notice in this Place.

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Thus, the Latitude of *Arcturus* will be found to be 31 Degrees North, and the Longitude 200 Degrees from  $\gamma$ , or 20 Degrees from  $\alpha$ : The Latitude of *Fornax* in the Southern Fish, 15 Degrees South, and Longitude  $299\frac{1}{2}$  Degrees, or  $\nu\pi 29\frac{1}{2}$  Degrees. By the Converse of this Method, having the Latitude and Longitude of a Star given, it will be easy to find the star upon the Globe.

The Distance betwixt two Stars, or the Number of Degrees contained between them, may be found, by laying the Quadrant of Altitude over each of them, and counting the Number of Degrees intercepted; after the same manner, as we found the Distance betwixt two Places on the Terrestrial Globe.

**ROB. XXV.** *The Latitude of the Place being given; to find the Amplitude, Oblique Ascension and Descension, Ascensional Difference; Semi-Diurnal Arch, and the Time of Continuance above the Horizon, of any given Point in the Heavens.*

Having rectified the Globe for the Latitude, and brought the given Point to the Meridian, set the Index to the Hour of 12; then turn the Globe until the given Point be brought to the Eastern Side of the Horizon, and that Degree of the Equinoctial which is cut by the Horizon at that Time, will be the *Oblique Ascension*; and where the given Point cuts the Horizon, is the *Amplitude Ortive*: If the Globe be turned about until the given Point be brought to the Western Side of the Horizon, will there shew the *Amplitude Occasive*; and where the Horizon cuts the Equinoctial at that Time, is the *Oblique Descension*. The Time between the Index at either of these two Positions, and the Hour of 6, or the Difference between the Oblique Ascension and Right Ascension, is the *Ascensional Difference*. If the Place be in *North Latitude*, and the Declination of the given Point be  $\begin{cases} \text{North} \\ \text{South} \end{cases}$ , the Ascensional Difference reduced

to Time, and  $\begin{cases} \text{added to} \\ \text{subtracted from} \end{cases} \begin{cases} 6 \text{ o'Clock, gives the Semi-} \\ \text{Nocturnal Arch; the Complement whereof to a Semicircle, is the} \\ \text{Anti-Nocturnal Arch. If the Place be in South Latitude, then the} \\ \text{contrary is to be observed with respect to the Declination.} \end{cases}$

The Semi- $\begin{cases} \text{Diurnal} \\ \text{Nocturnal} \end{cases}$  Arch being doubled, gives the Time of Continuance  $\begin{cases} \text{above} \\ \text{below} \end{cases}$  the Horizon. Or the Time of Continuance above the Horizon, may be found by counting the

Number of Hours contained in the upper Part of the Horary Circle, betwixt the Places where the Index pointed, when the given Point was in the Eastern and Western Parts of the Horizon. If the given Point was the Sun's Place, the Index pointed the Time of his Rising and Setting, when the said Place was in the Eastern and Western Parts of the Horizon. Or the Time of Sun-rising may be found by adding or subtracting his Ascensional Difference, to or from the Hour of Six according as the Latitude and Declination are either contrarie or the same Way.

Thus, at London on the 20th of April, the Sun's

Amplitude, is 24 Degrees Northerly.	}	Oblique Ascension, 20.
Oblique Descension, 58.		
Ascensional Difference, 19.		
Semi-Diurnal Arch, 109.		

Continuance above the Horizon 1  
Hours.

Sun rises at three Quarters past Four.

Sun sets at a Quarter past Seven.

These Things for the Sun vary every Day; but for a fixed Star, the Day of the Month need not be given, for they are the same all the Year round.

Thus the several Requisites for the Stars *Aldebaran*, *Castor*, *Regel* and *Syrius*, will be found as follows.

For	<i>Aldebaran</i>	<i>Castor</i>	<i>Regel</i>	<i>Syrius</i>
Right Ascension	65 03	109 16	75 21	98 16
Declination	15 55 N	32 27 N	08 33 S	16 21 S
Meridional Altitude	54 23	70 55	29 55	22 07
Meridional Zenith-distance	35 37	19 05	60 05	67 53
Oblique Ascension	44 00	56 06	64 27	76 36
Amplitude	26 09 N	59 36 N	13 50 S	26 54 S
Oblique Descension	86 06	162 26	86 15	119 56
Ascensional Difference	21 03	53 10	10 54	21 40

P R O B. XXVI. *The Latitude and the Day of the Month being given; to find the Hour, when a known Star will be on the Meridian, and also the Time of its Rising and Setting.*

Having rectified the Globe for the Latitude and the Sun's Place; bring the given Star to the Meridian, and also to the

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aff or West Side of the Horizon, and the Index will shew accordingly, when the Star Culminates, or the Time of its Rising Setting.

Thus at London on the 10th of January, *Syrius* will be upon the Meridian at a Quarter past Ten in the Evening; rises at  $5\frac{1}{2}$  hours, and sets at three Quarters past two in the Morning.

By the Converse of this Problem, knowing the Time, when any Star is upon the Meridian, we may easily find the Sun's Place. Thus, bring the given Star to the Meridian, and set the Index to the given Hour; then turn the Globe until the Index points to 12 at Noon, and the Meridian will cut the Sun's Place in the Ecliptic. Thus when *Syrius* comes to the Meridian at  $10\frac{1}{2}$  hours after Noon, the Sun's Place will be  $\approx 1\frac{1}{2}$  Degrees.

**R O B. XXVII.** *To find at what Time of the Year a given Star will be upon the Meridian, at a given Hour of the Night.*

Bring the Star to the Meridian, and set the Index to 12 at Noon, then turn the Globe till the Index points to the given hour, and the Meridian will cut the Ecliptic in the Sun's Place; whence the Day of the Month may be easily found in the Kalendar upon the Horizon.

**R O B. XXVIII.** *The Latitude of the Place being given, to find the Hour of the Day, when the Sun shines.*

If it be in the Summer, elevate the Pole according to the Latitude, and let the Meridian due North and South; then the Shade of the Axis will cut the Hour on the Dial-Plate: For the Obelisk being rectified in this Manner, the Hour-Circle is a true *equinoctial-Dial*; the Axis of the Globe being the *Gnomon*. This holds true in Theory, but it might not be very accurate in Practice, because of the Difficulty in placing the Horizon of the Obelisk truly Horizontal, and its Meridian due North and South. If it be in the Winter Half-Year, elevate the South Pole according to the Latitude North; and let the North Part of the Horizon in the South Part of the Meridian: Then the Shade of the Obelisk will shew the Hour of the Day as before. But this cannot be so conveniently performed, tho' the Reason is the same as in the former Case.

**P R O B. XXIX.** *The Latitude, the Sun's Place and his Altitude, being given; to find the Hour of the Day, and the Sun's Azimuth from the Meridian.*

Having rectified the Globe for the Latitude, the Zenith, and the Sun's Place; turn the Globe, and the Quadrant of Altitude, so that the Sun's Place may cut the given Degree of Altitude; then the Index will shew the Hour, and the Quadrant will cut the Azimuth in the Horizon. Thus, If at London, on the 10th of August, the Sun's Altitude be 36 Degrees in the Forenoon, the Hour of the Day will be IX, and the Sun's Azimuth about 58 Degrees from the South Part of the Meridian.

**P R O B. XXX.** *The Latitude, the Sun's Place and his Azimuth being given; to find his Altitude and the Hour.*

Rectify the Globe for the Latitude, the Zenith, and Sun's Place; then put the Quadrant of Altitude to the Sun's Azimuth in the Horizon, and turn the Globe till the Sun's Place meets the Edge of the Quadrant; then the said Edge will shew the Altitude, and the Index point to the Hour. Thus, May 10th at London, when the Sun is due East, his Altitude will be about 24 Degrees, and the Hour about VII in the Morning. And when his Azimuth is 60 Degrees South-Westerly, the Altitude will be about  $44\frac{1}{2}$  Degrees, and the Hour about  $2\frac{1}{2}$  in the Afternoon.

Thus, the Latitude and the Day being known, and having besides either the Altitude, the Azimuth, or the Hour; the other two may be easily found.

**P R O B. XXXI.** *The Latitude, the Sun's Altitude, and his Azimuth, being given; to find his Place in the Ecliptic and the Hour.*

Rectify the Globe for the Latitude and Zenith, and set the Edge of the Quadrant to the given Azimuth; then turning the Globe about, that Point of the Ecliptic which cuts the Altitude, will be the Sun's Place. Keep the Quadrant of Altitude.

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Place in the same Position, and having brought the Sun's Place to the Meridian, and the Hour-Index to 12 at Noon; turn the Globe about till the Sun's Place cuts the Quadrant of Altitude, and then the Index will point to the Hour of the Day.

R O B. XXXII. *Given the Time that a Star comes to the Meridian; to find the Sun's Place.*

Bring the Star to the Meridian, set the Index to the given time, turn the Globe about till the Index point to 12 at noon; then will the Meridian cut the Ecliptic in the Sun's place.

R O B. XXXIII. *The Day of the Month, and the Azimuth of any known Star being given; to find the Hour of the Night.*

Having rectified the Globe for the Latitude and the Sun's place; if the given Star be due *North* or *South*, bring it to the Meridian, and the Index will shew the Hour of the Night. If the Star be in any other Direction, fix the Quadrant of Altitude in the Zenith, and set it to the Star's Azimuth in the Horizon; then turn the Globe about until the Quadrant cuts the Center of the Star, and the Index will shew the Hour of Night.

The Bearing of any Point in the Heavens may be found by following Methods.

Having a Meridian-Line drawn in two Windows, that are opposite to one another, we may cross it at Right Angles with another Line, representing the *East* and *West*; from the Point of Intersection describe a Circle, and divide each Quadrant into 90 Degrees; then get a smooth Board, of about 2 Feet long, and  $\frac{1}{4}$  Foot broad, (more or less as may be judged convenient) and on the back Part of it fix another small Board crosswise, so that it may serve as a Foot to support the biggest End upright, when it is set upon a Level, or an Horizontal Plane. The Board being thus prepared, set the lower Edge of the smooth, or Fore-Side of it, close to the Center of the Circle, then turn it about to the Meridian, or to any Azimuth required, (keeping the Edge of it always close to the Center) and casting our Eye along the flat Side of it, we'll easily perceive what Stars are upon the Meridian, or any other Line that the Board is set to.

P R O B.

**P R O B. XXXIV.** *If two Stars were given, one on the Meridian, and the other in the East or West Part of the Horizon; to find the Latitude.*

Bring that Star, which was observed on the Meridian, to the Meridian of the Globe, and keep the Globe from turning round its Axis; then slide the Meridian up or down in the Notches till the other Star is brought to the *East* or *West* Part of the Horizon, and that Elevation of the Pole will be the *Latitude* sought.

**P R O B. XXXV.** *Given two Altitudes of the Sun and Space of Time between the Observations; to find the Latitude of such a Place.*

Take the Complement of Altitude of the first Observation in the Compasses, and set one Foot in the Sun's Place, and sweep a Circle on the Globes Surface with the other; then bring the Sun's Place to the Meridian, and turn the Globe *East*, till so many Degrees as answer to the Space of Time thro' it; then under the Declination mark the Place the Meridian cuts, and set one Foot of the Compasses in it, with the other extended to the Complement of Altitude of the second Observation, cross the former Circle in the Vertical Point, Zenith of the Place, which bring to the Meridian, thereon the Latitude sought.

**P R O B. XXXVI.** *Given the Sun's Declination and Amplitude; to find the Latitude.*

Elevate the Pole so many Degrees as the Complement of Amplitude is, and screw the Quadrant in the Zenith, bring the first Point of  $\Sigma$  to the Meridian; then count the Quadrant of Altitude to the Degree of the Sun's Declination, and bring that Degree to the Equinoctial, and the Degree of the Equinoctial cut by that Degree of the Quadrant of Altitude, is the Degree of Latitude sought.

R O B. XXXVII. Given the Sun's Amplitude and Difference of Ascension; to find the Latitude and Sun's Declination.

Elevate the Pole so many Degrees as the Sun's Difference of Ascension is, and screw the Quadrant of Altitude to the Zenith, and bring the first Point of  $\gamma$  to the Meridian, then turner on the Quadrant of Altitude the Complement of the Sun's Amplitude, and move the Quadrant of Altitude, till at Number of Degrees cuts the Equator, so shall the Quadrant cut in the Horizon the Degree of Latitude, and in the Equator the Sun's Declination.

R O B. XXXVIII. The Sun's Declination and Hour at East given; to find the Latitude.

Elevate the Pole so many Degrees as the Sun's Declination and screw the Quadrant of Altitude in the Zenith, then range the Time after 6 of its being due East into Degrees and minutes, which Number in the Horizon from the East Southwards, and bring the Quadrant of Altitude to that Degree, so all the Degree of the Quadrant cut by the Equator be the complement of the Latitude sought.

R O B. XXXIX. Given the Day of the Month, and Hour of the Night, and a known Star, either Rising or Setting; to find the Latitude.

Rectify the Globe, and turn the Globe till its Hour-Index int at the given Hour, and there fasten the Globe; then turn the Meridian thro' the Notches of the Horizon, till the known Star come to the East-Side of the Horizon, if Rising, or the West, if Setting; so shall the Elevation of the Pole then be the Latitude sought.

R O B. XL. By the Sun's Declination and Azimuth at Six; to find the Latitude and Altitude.

Elevate the Pole so many Degrees as is the Sun's given Azimuth, and screw the Quadrant in the Zenith: Bring the

first Point of  $\text{V}$  to the Meridian, then number on the Quadrant of Altitude upwards the Complement of the Sun's Declination, and bring that Degree to the Equator, so shall the Degree of the Horizon cut by the Quadrant of Altitude be the Complement of the Latitude, and the Degree of the Equator cut by the Quadrant, shall be the Altitude of the Sun at 6 of the Clock.

**P R O B. XLI.** *The Sun's Declination and Altitude at East given; to find the Latitude.*

Elevate the Pole to the Complement of the Sun's given Altitude, and screw the Quadrant to the Zenith; then bring the Equinoctial Point  $\text{V}$  to the Meridian, and number on the Quadrant of Altitude the Degree of the Sun's Declination and bring that Degree to the Equinoctial, and note the Degree it cuts; for its Complement to 90 is the Latitude sought.

*Or,*

With a Pair of Compasses, take from the Equator the Degree of Altitude given, then place one Foot in the Beginning of  $\text{V}$  on the inner Edge of the Horizon, and extend the other directly upwards towards the Zenith, then move the Brazen Meridian thro' the Notches of the Horizon, till the other Point of the Compasses reach the Parallel of the Sun's Declination; so shall the Number of Degrees that the Pole elevated above the Horizon be the Latitude sought; which either North or South, according as the Sun's Declination is.

**P R O B. XLII.** *If the Altitude of two Stars at the same Azimuth, were given; to find the Latitude of the Place.*

Set the Quadrant over both Stars at the observed Degree of Altitude, and keep it fast upon the Globe with your Fingers, then slide the Meridian up or down in the Notches, till the Quadrant cuts the given Azimuth in the Horizon; that Elevation of the Pole will be the Latitude required.

**P R O**

R O B. XLIII. Having the Latitude of the Place, to find the Degree of the Ecliptic, which rises or sets with a given Star; and from thence to determine the Time of its Cosmical and Achronical Rising and Setting.

Having rectified the Globe for the Latitude, bring the given Star to the Eastern Side of the Horizon, and mark what Degree of the Ecliptic rises with it: Look for that Degree in the Wooden Horizon, and right against it in the Kalendar, we'll find the Month and Day, when the Star rises *Cosmically*. If we bring the Star to the Western Side of the Horizon, that Degree of the Ecliptic which rises at that Time, will give the Day of the Month, when the said Star sets *Cosmically*. So likewise against the Degree which sets with the Star, we'll find the Day of the Month of the *Achronical Setting*; and if we bring it to the Eastern Part of the Horizon, that Degree which sets at that time will be the Sun's Place when the Star rises *Achronically*.

Thus, in the Latitude of London, *Syrius*, or the *Dog Star*, rises *Cosmically* the 30th of July; and sets *Cosmically* the 30th of October. *Aldebaran*, or the *Bull's Eye*, rises *Achronically* on the 11th of May, and sets *Achronically* on the 8th of December.

R O B. XLIV. Having the Latitude of the Place, to find the Time when a Star rises and sets Heliacally.

Having rectified the Globe for the Latitude, bring the Star to the Eastern Side of the Horizon, and turn the Quadrant round till it cuts the Ecliptic in twelve Degrees Altitude above the Horizon, if the Star be of the first Magnitude; then that Point of the Ecliptic which is cut by the Quadrant, is 12 Degrees High, above the Western Part of the Horizon, when the Star rises; but at the same Time the opposite Point in the Ecliptic is 12 Degrees below the Eastern Part of the Horizon, which is the Depression of a Star of the same Magnitude, when it rises *Heliacally*; or has got so far from the Sun's Beams, that it may be seen in the Morning before Sun-rise. Wherefore look for the said Point of the Ecliptic on the Horizon, and right against it will be the Day of the Month when the Star rises *Heliacally*. To find the *Heliacal Setting*: Bring the Star to the West-Side of the Horizon, and turn the Quadrant about to the Eastern Side, till the 12th Degree of it a-

bove the Horizon cuts the Ecliptic; then that Degree of the Ecliptic, which is opposite to this Point, is the Sun's Place when the Star sets Heliacally.

Thus, we'll find that *Arcturus* rises Heliacally the 17th of September; and sets Heliacally, November the 21st.

**P R O B. XLV.** *To find the Place of any Planet on the Globe; and so by that Means, to find its Place in the Heavens: Also to find at what Hour any Planet will rise or set, or be on the Meridian any Day in the Year.*

We must first seek in an *Ephemerides*, (Parker's *Ephemeris* will well enough) for the Place of the Planet proposed, on the Day; then mark that Point of the Ecliptic, either with Chalk or by sticking on a little black Patch; and then for that Night we may perform any Problem, as before, by a Fixed Star.

Let it be required to find the Situation of *Jupiter* among Fixed Stars in the Heavens, and also what Time it rises and sets, and comes to the Meridian, on the 20th of November, 1730, at London.

Looking for the 20th of November, 1730, in Parker's *Ephemeris*, I find that *Jupiter's* Place at that Time is in about 9 Degrees  $\frac{1}{2}$ ; Latitude 1 Degree North. Then looking for that Point on the Celestial Globe, I find that  $\chi$  is then among the small Stars that lie under the Belly of the Constellation *Leo*.

To find when he rises and sets, and comes to the Meridian. Having put a little black Patch on the Place of *Jupiter*, elevate the Globe according to the Latitude; and having brought the Sun's Place to the Meridian, set the Hour-Index to noon: Then turning the Mark which was made for *Jupiter*, the Eastern Part of the Horizon. I find  $\chi$  will rise at about Quarter past 11 o'Clock at Night; and turning the Globe about, I find it comes to the Meridian a little after Six in the Morning; and sets about 1 o'Clock in the Afternoon.

This Example being understood, it will be easy to find what either of the other two superior Planets, viz. *Mars* and *Saturn*, Rise, Set, and come to the Meridian.

*GNOMONICAL or DIALLING  
PROBLEMS,  
Solv'd by the  
GLOBES.*

S E C T. IV.

**D**IALS take their Names from the Circles of the Sphere to which their Planes are parallel ; or with whose Planes they coincide.

- I. The *Hour-Lines* are the common Sections of the Hour-Circles of the Sphere with those Planes.
- II. The *Stile* or *Gnomon* is a Line parallel to the common Section of the Planes of all the Hour-Circles of the Sphere, i.e. parallel to the Axis of the World. Hence, The Elevation of the Stile above the Dial-Plane must be always equal to the Elevation of the Axis of the World above the Plane of the Circle to which the Dial-Plane is parallel ; the Stile must always be directed towards the elevated pole.
- III. A *Horizontal* Dial is whose Plane is parallel to the Horizon.
- V. A *Vertical* Dial is whose Plane coincides with that of the Vertical Circle.

V. A

## 78 Gnomonical or Dialling Problems,

V. A Direct Erect Vertical Dial is whose Plane is perpendicular to the Horizon, and whose Face looks directly South or North.

VI. An Erect Declining Vertical Dial is whose Plane is perpendicular to the Horizon, but its Face declines from South or North Eastward or Westward.

VII. A Direct Reclining Vertical Dial is whose Plane looks directly South or North, but falls back from the Zenith.

VIII. A Direct Reclining Vertical Dial whose Reclination is towards the same Parts with the Latitude of the Place, and equal to the Co Latitude, is called a Polar Dial, its Plane passing through the Poles of the World.

IX. A Direct Inclining Vertical Dial is whose Plane looks directly South or North; but makes an acute Angle with the Horizon.

X. If the Latitude of the Place and the Inclination of the Plane be towards contrary Parts, and the Inclination equal to the Co-Latitude, that Dial is called an Equinoctial Dial.

N.B. Every Dial-Plane having two Faces, it is plain, the upper Face of the Equinoctial Dial shall have its Reclination equal to the Latitude, and the under Face of the Polar Dial an Inclination equal to the Latitude.

XI. From what has been said, it may be easily known what is meant by Reclining Declining, and Inclining Declining Vertical Dials.

XII. An Erect Vertical Dial whose Face looks directly East or West, is called a Meridian-Dial.

XIII. The Substilus is the Line in the Dial-Plane, upon which the Stile is set: It is the common Section of the Dial-Plane and the Plane of a great Circle passing thro' the Poles of the World and those of the Plane.

### P R O B L E M I.

To find the Inclination of a Plane, Plate 2. Fig.

Let AB be a Plane inclin'd to the Horizon HR. apply to the Plane, AB a Quadrant DCF, so as the Plumbmet CE may strike the Surface of the Quadrant, I say, the Arch DE is the Measure of the Angle of Inclination ABH. Draw BG at Right-Angles to HR, because CE is Parallel to BG, the Angle ECF is equal to CBG, but DCF is equal to GBH both being Right-Angles. the Angle DCF less ECF is equal to GBH less CBG, that is, DCE is equal to ABH.

Q.E.D.

P R O

## P R O B. II. To find the Reclination of a Plane.

Plate 2. Fig. 2.

Let AB be the reclining Plane. Draw BG perpendicular to HR, representing the Prime Vertical: so ABG is the Angle of Reclination. Raise KL perpendicular to AB, apply a Quadrant CDF to KL; so as the Plum-Line CE may strain the Face of the Quadrant, I say, DE is the Measure of the Angle of Reclination ABG.

In the Right-angle Triangle NBK the Angles BNK more NBK are equal to a Right Angle equal to DCF: But, because CE is parallel to BG, the Angle ECF is equal to BNK, therefore DCE is equal to NBK. Q.E.D.

## P R O B. III. To find the Declination of any Plane.

Plate 2. Fig. 3.

Take a Piece of Board, whose upper Surface is a Right-angled Parallelogram as DB, on it describe a Circle CXZ; on the Center C erect a Pin perpendicularly. Draw FG parallel to BE, Mn perpendicular to BE, LN perpendicular to FG, and place the Plane DB horizontally, with the Side BE applied to the Dial-Plane: Observe when the Shadow of the Top of the Pin is on the Periphery of the Circle as at z in the forenoon, and at x in the Afternoon the same Day; bisect the Arch  $xz$  with the Diameter KL. 'tis plain KL is the Meridian, and KLN equal to KMn is the Angle of Declination.

## P R O B. IV. To make an Horizontal Dial.

## The Operation by the G L O B E.

Elevate the Pole to the Latitude of the Place for which we would make our Dial (suppose to London, in the Latitude of  $51^{\circ} 30'$ ) and bring the Vernal Colure to the Meridian, and the Hour-Index to 12 on the Hour-Circle.

1 2 3 4 5 6	a Clock, or till $15^{\circ}$ of the Equator pass through the Meridian, and the Colure will cut the Ho- rizon in	$11^{\circ} 50'$ $24^{\circ} 20'$ $38^{\circ} 03'$ $53^{\circ} 36'$ $71^{\circ} 06'$ $90^{\circ} 00'$	From the Meridian.

These

## 80 Gnomonical or Dialling Problems,

These are the Distances of the Hour-Lines from Noon till at Night, and the same Distances serve for the Hours between 6 in the Morning, and 12 at Noon, for the one a Clock Hour-Line in the Afternoon is equidistant from the Meridian, or Noon-Line, with the 11 a Clock Hour-Line before Noon, and so all the other Morning Hour-Lines are distant from the Noon-Line by the same Space that the same Number after Noon-Hour-Lines (numbred from the Meridian on the contrary Side of the Noon-Line) are distant from the Meridian.

If we would have the half Hour-Lines placed on our *Dial*, we must turn the Globe till the Index points to every half Hour on the Hour-Circle, and mark the Degrees of the Horizon, cut by the Vernal Colure, for those are the Degrees belonging to the half Hours required.

### The Geometrical Construction of this DIAL.

1. Upon the Plane on which we design to draw our *Dial* (in Plate 2. Fig. 4.) draw a right Line A B, representing the Meridian of our Globe, and the Hour-Line of 12.

2. Towards one End of this Line, assign a Point C, representing the Center of our *Dial*, and through that Point draw another Line at Right Angles to A B, which shall be the Hour-Line at 6, as the Line K M; and upon the Point C, with the Radius of some Line of *Chords*, describe a Semicircle D E F.

3. Then seeing 11 and 1 a Clock are distant from the Meridian 11 Deg. 50 Min. take 11 Deg. 50 Min. from our Line of *Chords*, and set it upon the Semicircle from E to 11, and from E to 1, and draw the Lines C 11, and C 1, for the Hour-Lines between 11 and 1.

4. The Distance of 10 and 2, being 24 Deg. 20 Min. we must take from our Line of *Chords* 24 Deg. 20 Min. and set it from E to 10, and from E to 2, and draw the Hour-Lines of 10 and 2, do thus with the rest of the Hour-Lines, till 6 in the Morning and 6 at Night; and for the Hour-Lines of 4 and 5 in the Morning, and of 7 and 8 at Night: Continue the Hour-Lines of 4 and 5 in the Afternoon thro' the Center to the other Side of the *Dial*, and they will be the Hour-Lines of 4 and 5 in the Morning; and the Hour-Lines of 7 and 8 in the Forenoon continued will be the Hour-Lines of 7 and 8 in the Afternoon.

5. For the *Stile* or *Cock* of our *Dial* take 51 Deg. 30 Min. the Latitude from our Line of *Chords*, and set that Distance upon the Semicircle from E to G, and draw the Line C G for the Stile, which must stand upon the Line of 12, without inclining to the East or West, and so is our *Dial* finished.

P R O

**R O B. V.** *By one Position of the Globe, to find the Hour-Lines in all manner of Planes.*

Let a Meridian from Pole to Pole pass thro' every 15 Degrees of the Equinoctial, to represent the Horary Motion of the Sun, both Day and Night; then rectify the Globe to the Latitude, bring also one of those Meridians under the brazen meridian, all the rest of the Meridian-Lines shall cut any Circle, representing the Plane of a Dial, in the Number of Degrees on the same Circle that each respective Hour-Line is distant from the Noon-Line Point in the same Circle.

**R O B. VI.** *To find in what Place of the Earth any manner of Plane, that in their Latitude is not Horizontal, shall become Horizontal.*

Seeing all Manner of Planes, however situate, are parallel some Country on the Earth, therefore what is not Horizontal in one Place, may become so in another Latitude, and Horizontal Dial made for it will answer.

Thus, an *Erect direct South or North Dial* becomes an *Horizontal Dial* in the same Longitude, but whose Latitude shall be Complement; wherefore an *Erect Direct Dial* is the same the *Horizontal* in the Latitude 45; and an *Erect Plane* under the Pole will be an *Horizontal* under the Equator, and an *Erect* the Latitude 30, will be an *Horizontal* in the Latitude 60, and *contra*.

But if the *Plane* be an *Erect Decliner*, it shall be an *Horizontal Plane*, at that Point of the *Globe*, which is against the *degree of Declination* found on the *Horizon*; the *Latitude* and *Longitude* of which Point find by the *Globe*, and if the *Plane* declines *Westward*, the *Sun* comes sooner to the *Meridian* of it, than to the *Meridian* of the *Place* where it becomes an *Horizontal Plane*, and that by so many *Hours* or *Minutes* as the *Difference of Longitude* amounts to; but if *Eastward*, then it comes so much later.

If the *Plane* be a *direct Recliner*, the *Complement* of the *Plane's Reclination* is the *Latitude*, where it becomes an *Horizontal* one in the same *Longitude*.

If it be a *Declining Recliner*, Rectify the *Globe* according to the *Latitude given*, bring the *Place* to the *Meridian*, and the *Quadrant* to the *Zenith*, which turn to the *Declination* on the *Horizon*, and on the *Quadrant* count upwards the *Reclination*

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clination, by which Degree make a Prick on the Globe, which find both the Latitude and Longitude for the true Place where such a Plane becomes an Horizontal one, the Difference of Longitude change into Time, for the Difference the Sun makes betwixt the two Meridians.

**P R O B. VII.** *To make a Dial on the Globe, that shall shew the Hour of the Day, without a Gnomon.*

Divide the Equinoctial or Middle Circle into 24 equal Parts with two twelves, as we count the Hours, then elevate it according to the Latitude, and place one 12 due North, and the other 12 due South, when the Sun shines on it the Globe will be divided into two Halves, the one enlightened with Sun-shine, the other Shadow'd, and where they part on the Equinox, is the Hour of the Day in two Places on the Ball.

**P R O B. VIII.** *To make an Erect South Dial at Latitude 51 Degrees 30 Minutes.*

### The Operation by the Globe.

We may reduce all Verticals to Horizontals, if we elevate the Pole to the Complement of the Latitude, which in this Case is 38 Degrees 30 Minutes, and bring the Vernal Colure to the Meridian, and the Index to 12, then turn the Globe Westwards, and as each 15th Degree is at the Meridian (or as the Index points out the several Hours on the Hour-Circle) the Colure shews in the Horizon the Distance of the several Hour Lines, from the Meridian, as in the following Table.

Comp. Latitude $38^{\circ} 30'$ .			
Hours.		Distances from the Meridian.	
12		00°	00'
11 1		09	28
10 2		19	45
9 3		31	54
8 4		47	09
7 5		66	42
6		90	00

## the Geometrical Construction, Plate 2. Figure 5.

I. Draw a Meridian-Line, as EM, for the Hour-Line of 12; cross it at Right-Angles with the Line NP for the Hour-Line 6, and 6, and where these Lines cross each other (as at O) the Center of the Dial.

II. With the Chord of 60 Deg. draw a Semicircle N P Q, and from the Line of Chords take the Hour-Distances (as in the foregoing Table) from the Meridian, and lay on the Semicircle, one Foot of the Compass being in the Meridian; to which Distances, from the Center, draw the Hour-Lines.

III. For the Style, take 38 Deg. 30 Min. (the Complement of the Latitude) from the Line of Chords; set it from Q to R, and draw the Line OR for the Cock or Style of our Dial, which must stand over 12, and point downwards towards the South Pole.

N. B. The North Vertical Dial is the same with the South, only the Style must point upwards, towards the North Pole, and Hours 9, 10, 11, 12 at Night, and 1, 2, 3 in the Morning must be left out, and 4, 5 in the Morning, and 7, 8 at Night, be drawn through the Center, so is our North Dial finished.

## PROB. IX. To make an Erect, Direct East or West-Dial.

These Sorts of Dials may be better demonstrated than made on the Globe, for the Pole being rectified to the Latitude, Index to 12; and the Quadrant of Altitude in the Zenith; the Quadrant be brought about till the graduated Edge thereof exactly East or West, and turning the Globe about, the Equinoctial Colure will not cut the Quadrant of Altitude in any particular Degree, but a Part of the Colure will coincide with all the Degr̄ees of the Quadrant at the same Time; therefore the Hour-Lines of these Planes will make no Angles with the Pole, and consequently must be parallel to one another, which the Globe plainly represents, but will not conveniently give the Parallel Distance of each from the other, they being nearer or farther off, according as the Style is proportioned to the Plane.

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### The Geometrical Construction.

Let the Plate, upon which we would make an *East* or *West* *Dial*, be ABCD, Plate 2. Fig. 6.

1. Upon D, if it be an *East-Dial-Plane*; or upon the Point if it be a *West-Dial*, with the Radius of the Line of Chords describe an Arch of a Circle GE, then from the Line of Chords take 38 Deg. 30 Min. and draw the Line DGE quite through the Plane for the Equinoctial, towards the upper Part of this Line, as at P; assume any Point, and through it draw the Line 6 P 6, perpendicular to the Equinoctial for the Hour-Line of Six, also towards the lower Part of the same Line, assume another Point as L, and through it draw the Line 11 C 11, for the Hour of Eleven.

2. With 60 Deg. from the Chords, upon the Point C, describe a small Arch of a Circle as HK, and upon it set 15 Degrees, or one Hour's Distance from H to K, and draw the Line CKM cutting the Hour-Line of 6 in M.

Upon M as a Center, with 60 Deg. from the Chords, describe an Arch of a Circle NO, which divide into five equal Parts in the Points OOO. &c. Lay a Ruler upon M, and of these Points, and the Ruler will cut the Equinoctial Line DE in the Points \*\*\*\*, through which Points, if we draw Right Lines parallel to the Hour-Line of 6, they will be Hour-Lines of 7, 8, 9 and 10, the Hour-Lines of 6 and 11 being drawn before.

For the Hour-Lines of 4 and 5 in the Morning, they require the same Distance from six, as do the Hours 8 and 7.

The Stile must stand upon the Hour-Line of 6, and be of Height equal to the Length of the Line MP, and may be either a Pin or Wire, or a Plate of Brass, or Iron.

An Erect, Direct *West-Dial* is the same in all respects with Erect, Direct *East-Dial*, only as the *East* shews the Forenoon Hours, the *West* shews the Afternoon Hours, for that which in the *East-Dial* is 10, the *West-Dial* must be 2; and 9 in the *East-Dial* must be 3 in *West*.

### PROB. X. Of Erect Declining Planes.

The Upright or Erect Planes that we have hitherto treated of, are such as do directly behold the four Cardinal Points of the Horizon, all other Upright Planes are said to decline,

their Declination is counted from the *North* or *South*, towards the *East* or *West*; thus to make an *Erect Dial* for 51 Deg. 30 in. *North*, the Plane declining from the *North* towards the *East*, Degrees: Elevate the Pole to the given Latitude, fix the Quadrant of Altitude to the Zenith, and number the Declination of the Plane upon the Horizon from the *North*, (or *South* Point thereof according as the Plane declines) namely, Deg. and to that Point of the Horizon bring the Quadrant of Altitude, and there fix it, then bring the Vernal Colure the Meridian, and the Index of the Hour-Circle to the uppermost Figure of 12, in the Hour-Circle; then turn the Globe Eastwards, till the Index points to all the Hours before noon; and examine in what Number of Degrees from the Zenith the Colure cuts the Quadrant of Altitude, when the Index points to each Hour, or when each 15 Degrees of the Equator passes the Meridian, for the Degrees of the Quadrant, numbered from the Zenith, cut off by the Colure, are the Distances of the Forenoon Hour-Lines, as are expressed in the following Table.

Hours from noon.	Hours dist. on the Plane
	0 1
II	9 43
10	19 00
9	25 57
8	35 10
7	45 56
6	60 15
5	79 43

There is this Difference between *Direct* and *Declining Dials*, that the Hour-Distances for the Afternoon on *Declining Dials*, are not the same with the Hour-Distances for the Forenoon, because the Sun remains longer on that Side of the Plane, which it declines to, than it doth on the contrary Side; therefore, there will be a greater Number of Hour-Lines upon it, and by Consequence the Distances of the Hour-Lines less than on the contrary Side of the Plane; therefore, for finding the Afternoon Hour-Distances, turn about the Quadrant of Altitude upon the Zenith-Point, till the lower End of it comes to the Degree of the Horizon, opposite to that Degree of

Declination, the Quadrant of Altitude was placed at, when the Distance of the Forenoon Hour-Lines was found, viz. to Degrees, counted from the *South* towards the *West*, and bring the Vernal Colure again to the Meridian, and the Index to 12; then turning the Globe Westwards, as the Index points to the several Hours, or at each 15 Degrees of the Equator passing the Meridian, the Colure will cut the Quadrant of Altitude the Afternoon Hour-Distances, numbered from the Zenith, are expressed in the following Table.

Hours

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Hours from Noon.	Hours dist. on the Plane
1	11 20
2	26 47
3	49 20
4	75 52

It is to be observed, that this Plane is capable of receiving no more Hour-Lines, after Noon, than 4, for when the Colure goes off the Quadrant of Altitude, the Sun goes off these Kind of Planes.

And to find the Distance of the Substilar-Line from the 12 a-Clock-Line, and the Elevation of the Stile about the Plane, which are two Requisites always to be found in upright declining Planes, bring the Colure to the Number of Degrees of the Plane's Declination, counted in the *Horizon*, from the South Point towards the *East*, and the Quadrant of Altitude to the Degrees of the Plane's Declination on the *Horizon*, from the North towards the *East*, so shall the Quadrant of Altitude and the Colure, cut each other at Right-Angles, and the Number of Degrees comprehended between the Colure and Zenith in the Quadrant of Altitude, shall be the Number of Degrees between the Substilar-Line and the 12 a-Clock-Line, which, in this Example, is 19 Deg. 45 Min. and the Number of Degrees comprehended between the Quadrant of Altitude and the Pole, counted on the Colure, shall be the Number of Degrees that the Stile is to be elevated above the Plane, which in this Example, is 33 Deg. 40 Min.

*The Geometrical Construction, as in Plate 2  
Fig. 7.*

Draw on our Plane an Horizontal Line, as CD, and with the Chord of 60 Degrees describe a Semicircle DBC, which divide into two equal Parts, and draw the Line AB, which will be the Hour of 12, then, from a Line of Chords, take several Hour-Distances from the Meridian, and lay on the Semicircle from B to C and D, drawing Lines from the Center A, through those Divisions, so shall all the Hour-Lines be presented on the Plane; then to represent the Substilar-Line on that Plane, from the Line of Chords, take 19 Degrees 45 Minutes, the Distance of the Substilar-Line from the 12 a-Clock-Line, and on the Semicircle from the 12 a-Clock-Line at B, set it off to x, on the contrary Side to the Declination of the Plane, which, in this Case, must be in the West Side, and from the Center A draw Ax, which shall represent the Substilar-Line; and from the Substilar-Line, lay off

3 Deg: 40 Min. the Elevation of the Stile above the Plane, in the Circle from x to y, then draw the Line Ay for the stile, or *Gnomon*; and let fall the Perpendicular ab upon the substile, so we have a Triangle, which erected perpendicular upon the Substile Ax, the Stile Ay shall be parallel to the axis of the World, and cast a Shadow upon the Hour of the day.

Here we may observe, that in *Declining Dials*, the Stile doth not stand at the same Elevation above the Plane, that it doth in *Erect Direct Dials*, neither doth it stand over the 12 a-Clock-line, but on some Part of that Quarter towards which the Declination of the Plane is.

Thus we have finish'd our Dial, and in so doing, we have,  
this one, made four Dials, viz.

A	{	North declining East	{	Deg.	Min.
		North declining West			
		South declining East			
		South declining West		{	63 00

Only placing the Number of the Hours, and the Stile respectively upon each Plane: For in the *South-West* Plane, the Stile stands upon the Hour-Line of 2 in the Afternoon; in the *East*, declining as much, it will stand upon the Hour-line of 10 before Noon. And so all the Morning-Hours of *West-Decliner*, will be the Afternoon-Hours of the *East-Decliner*, and the Afternoon-Hours of the *West-Decliner* will be the Morning-Hours of the *East-Decliner*; and the *South-East-Decliner* produce the *North-West-Decliner*, and the *South-West Decliner*, *North-East-Decliner*, by only extending the Hour-Lines, Stile Subfile, quite thro' the Center.

## o B. XI. Of Direct South Reclining DIALS.

Declining Planes are those that cut the Horizon at Oblique angles, reclining from the Zenith, or inclining to the Horizon, and are either direct North, South, East, or West reclining, reclining from the North, West, &c. and so are call'd Declining Planes.

*South-Plane* may so recline, that the Reclination thereof  
be either

than } the Complement of the Latitude.

Now,

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Now, to reduce any of these Planes to a new Latitude, where they may become Horizontal-Planes.

1. If the Reclination of the Plane be less than the Complement of the known Latitude, subtract the Plane's Reclination from the Coimplement of the Latitude, and the Remainder shall be a new Latitude, where the Reclining Plane shall be an Horizontal Plane; and, in this Case, the *South-Pole*, in *North Latitude*, is always elevated.

2. If the Reclination be equal to the Complement of the Latitude: In that Case the Plane lies in the Axis of the World, and hath no *Pole* elevated above it.

3. If the Reclination of the Plane be more than the Complement of the Latitude, subtract the Complement of Latitude from the Plane's Reclination, and the Remainder shall be the new Latitude; and in this Case the *North-Pole*, in *South Latitudes*, is always elevated.

In the first of these three Varieties: If a *South-Plane* in Latitude of 51 Deg. 30 Min. recline 20 Degrees, which is less than the Complement of the given Latitude; therefore Reclination being subtracted from it, leaves 18 Deg. 30 Min. for the new Latitude: Wherefore, if we rectify the Globe to 18 Deg. 30 Min. of Latitude, and find the Distances of Hour-Lines from the Meridian, for a Horizontal-Dial in that Latitude, that Dial shall serve for a *South-Reclining* 20 Deg. in Latitude of 51 Deg. 30 Min. and the Height of the Stile above the 12 Hour-Line, or Substile, will be equal to the new Latitude, namely 18 Degrees 30 Minutes.

In the second Case, when the *South-Reclination* and Complement of the *North-Latitude* are equal, the Dial is to be made in all Respects like an *East* or *West-Dial*; only that which in *East* or *West-Dial* is the Six o'Clock Hour-Line, must in these *Dials* be the Hour-Line of 12, &c.

In the third Case, suppose a *South-Plane* to recline from Zenith 60 Deg. in the Latitude of 51 Deg. 30 Min. the Complement of which subtracted from 60 Deg. leaves 21 Deg. 30 Min. for the new Latitude, and find the Hour-Distances of the Horizontal-Dial in that Latitude, which Hour-Distance will serve for a *South-Dial* reclining from the Zenith 60 Deg. in the Latitude of 51 Deg. 30 Min. and the Stile of the Dial must be elevated above the Substile, or Hour-Line of 21 Deg. 30 Min. equal to the new Latitude, and pointing upwards towards the *North-Pole*, as the Stiles of all *South-Planes* do, which recline more than the Complement of the Latitude; thus the Hour-Distance of all *South-Reclining-Dials*,

be found by the Globe, by referring such reclining Planes to a Latitude, where they may become Horizontal-Planes.

### P R O B. XII. Of North-Reclining DIALS.

There are three Varieties of North-Decliners, as there are of South-Recliners, for the Reclination may be either

Less than }  
Equal to } the Latitude of the Place.  
More than }

And to refer these to a new Latitude, where they will be Horizontal-Planes, we must observe,

I. If the Reclination of the Plane be less than the Latitude, add the Complement of the Latitude to the Plane's Reclination, and the Sum will be the new Latitude. Thus, let a North-plane in the Latitude of 51 Deg. 30 Min. recline from the Zenith 20 Deg. add 20 Degrees, the Plane's Reclination, to 38 Deg. 30 Min. the Complement of the Latitude, the Sum will be 58 Deg. 30 Min. which is the new Latitude. Wherefore, if we rectify the Globe to 58 Deg. 30 Min. and find the Hour-Distances of a Horizontal-Dial in that Latitude, those Distances will serve for a North-Plane reclining 20 Deg. in the Latitude of 51 Deg. 30 Min. North, and the Stile must be elevated above the Substile, or Hour-Line of 12, 58 Deg. 30 Min. equal to the new Latitude.

In the Secord of these Varieties, where the Plane of the Meridian declines, so as to cut the Meridian, just at the Intersection of the Meridian with the Equator, the Plane it self lying in the Equinoctial-Circle, and the Poles thereof in the Poles of the World; it is call'd a Polar-Plane. Wherefore rectify the Globe to 90 Deg. of Latitude, so shall the Poles be in the Zenith and Nadir, and the Equator in the Horizon, then turn the Globe about till 15 Degrees of the Equinoctial-Colure have pass'd the Meridian, and it will rest at 15 Deg. of the Horizon, which is the first Hour's Distance from 12. and in these Planes the Degrees of the Equator and Horizon being the same, the Hour-Lines are equally removed from one another; wherefore, if a Circle be described and divided into 24 equal Parts, lines being drawn from the Center to each Division, and a Wire perpendicularly placed in the Center, the Dial is finished. In the third Case, when the Plane declines more than the Latitude, and cuts the Meridian between the Equator and the

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Horizon; add the Reclination to the Complement of the Latitude, which Sum (if it don't exceed 90 Deg.) is a new Latitude, but if it exceeds 90 Deg. subtract that Sum from 180 Deg. and the Remainder will be a new Latitude; for which new Latitude rectify the Globe, and make an Horizontal-Dial, elevate the Stile above the 12 a-Clock Hour-Line equal to the new Latitude, and the Dial is finished.

### PROB. XIII. Of Declining Reclining or Inclining PLANES.

Such Planes as do not behold the *East*, *West*, *North*, or *South* Points of the Horizon directly, are called *Decliners*, and if they are not perpendicular to the Horizon, they both decline and incline, therefore they are called *Declining Inclining Planes*; for the making of these kind of Dials, let us suppose a Plane in the Latitude of 51 Deg. 30 Min. to decline from the *North* Part of the Meridian towards the *West* 72 Degrees, and also to recline from the Zenith 26 Deg. 34 Min.

1. Elevate the Globe to the given Latitude 51 Deg. 30 Min. fix the Quadrant of Altitude in the Zenith, the Hour-Index to 12, and the Equinoctial-Colure to the Meridian.
2. The Declination of the Plane being 72 Deg. Westward count upon the Horizon 20 Deg. the Complement of the Declination, from the *South* Part of the Meridian Westward, and from the *North* Part of the Meridian Eastward, and to these two Points on the Horizon bring the Ends of a narrow Plate of thin Brass, containing a complete Semicircle, divided into Degrees, beginning the Divisions at the Middle, and number them both Ways, and there fix it; then bring the Quadrant of Altitude to 20 Degrees on the Horizon, counted from the *East-Southward*. Now because the Plane reclines 26 Deg. 34 Min. count those Degrees downwards from the Zenith and to that Point bring the thin Plate of Brass representing the Plane, and there fix it; so is the Globe prepared for the making of this Dial; and for the Hour-distances, turn the Globe Eastward, till 15 Degrees of the Equator have passed the Meridian, and upon the Plane, or Plate of Brass, we shall find the Colure cut the Semicircle, counted from the Middle of it at 26 Deg. 3 Min. and by turning still Eastward, and observing where the Colure cuts the Semicircle at each 15 Degrees of the Equator, passing the Meridian, we shall find the Forenoon Hour-Distances, as in the following Table; and the Colure being again brought to the Meridian, and the Globe turned

the Lat. new Lat. from 180 for which ntal-Dial, al to the turned to the West, at each 15 Degrees of the Equator, crossing the Meridian, the Colure will cut the Semicircle in the Afternoon Hour-Distances, as in the following Table.

	Hours past the Meridian		Deg.	Min.
	Subtill.	Subtill.		
Forenoon	2 10	1 52	26	33
	3 2	2 57	57	47
	4 8	3 67	67	53
	5 7	4 76	76	12
Afternoon	6 6	5 84	84	15
	7 4	6 87	87	38
	8 3	7 78	78	25
	9 2	8 66	66	48
	10 1	9 50	50	46
	11	10 28	28	4

Now besides these Hour-Distances, we must find four Things more, preparatory to the Geometrical Construction of these Dials.

1. *The Arch of the Plane, or the Distance between the Meridian and Horizon, which may be found thus :*

Take, with the Compasses, the Distance upon the Plane, from the Intersection of the Plane with the Horizon, to the Intersection of the Plane with the Meridian, which Number of Degrees, namely, 36, is the Distance required.

2. *The Arch of the Meridian between the Plane and Zenith, thus : The Degrees of the Meridian intercepted between the Plane and Zenith, viz. 58 Deg. is the Arch required.*

3. *The Height of the Pole and Stile above the Plane.*

To find which, continue the Quadrant of Altitude from the Zenith, below the Horizon, so much as is the Reclination of the Plane, 26 Deg. 34 Min. and mark that Point. Then, a thin Plate of Brass (if the Quadrant of Altitude be too short) divided, and extended from the North-Pole towards the South-Pole, and passing through the Pole of the Plane, which is the Point before found, mark where the Plate cutteth the Plane, and the Number of Degrees upon the Plate contain'd between the

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Pole and the Plane, which in this Case will be 31 Deg. Min. is the Height of the Pole above the Plane or Substile.

### 4. The Distance of the Substile from the Meridian.

And that is, the Number of Degrees of the Plate representing the Plane, which are contained between the Plate, which came from the Pole of the World to the Pole of the Plane and the Intersection of the Plane with the Meridian, which in this Example will be 82<sup>1</sup>Deg. 4 Min. as appears by the following Table:

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466	467	468	469	470	471	472	473	474	475	476	477	478	479	480	481	482	483	484	485	486	487	488	489	490	491	492	493	494	495	496	497	498	499	500	501	502	503	504	505	506	507	508	509	510	511	512	513	514	515	516	517	518	519	520	521	522	523	524	525	526	527	528	529	530	531	532	533	534	535	536	537	538	539	540	541	542	543	544	545	546	547	548	549	550	551	552	553	554	555	556	557	558	559	560	561	562	563	564	565	566	567	568	569	570	571	572	573	574	575	576	577	578	579	580	581	582	583	584	585	586	587	588	589	590	591	592	593	594	595	596	597	598	599	600	601	602	603	604	605	606	607	608	609	610	611	612	613	614	615	616	617	618	619	620	621	622	623	624	625	626	627	628	629	630	631	632	633	634	635	636	637	638	639	640	641	642	643	644	645	646	647	648	649	650	651	652	653	654	655	656	657	658	659	660	661	662	663	664	665	666	667	668	669	670	671	672	673	674	675	676	677	678	679	680	681	682	683	684	685	686	687	688	689	690	691	692	693	694	695	696	697	698	699	700	701	702	703	704	705	706	707	708	709	710	711	712	713	714	715	716	717	718	719	720	721	722	723	724	725	726	727	728	729	730	731	732	733	734	735	736	737	738	739	740	741	742	743	744	745	746	747	748	749	750	751	752	753	754	755	756	757	758	759	760	761	762	763	764	765	766	767	768	769	770	771	772	773	774	775	776	777	778	779	780	781	782	783	784	785	786	787	788	789	790	791	792	793	794	795	796	797	798	799	800	801	802	803	804	805	806	807	808	809	810	811	812	813	814	815	816	817	818	819	820	821	822	823	824	825	826	827	828	829	830	831	832	833	834	835	836	837	838	839	840	841	842	843	844	845	846	847	848	849	850	851	852	853	854	855	856	857	858	859	860	861	862	863	864	865	866	867	868	869	870

ect. 4. Solved by the Globes. 93

31 Deg. 28 Min. set those Degrees from G to H, both above and below, and draw the Line HCH quite thro' the center for the Axis or Stiles of both Dials.

8. In the Table of Hour-Distances aforesaid, find the first Hour's Distance from 12 which is 26 Deg. 3 Min. set that Distance upon the Circle from 12 upwards to 1, and from 12 (on the other Side) downwards to 11, and draw the Lines G I, and C II; for the Hour-Lines of III and I a-Clock, which will both make one strait Line.

Do thus with all the Hours in the Table, till we come up to the Substile, and then (beginning at the Bottom of the Table.)

Take 28 Deg. 28 Min. and set from 12 on the Right-Hand downwards to 11, and from 12 on the Left-Hand upwards to draw the Line C II in the North-Reclining-Plane, for the Sun will never shine upon the South-Reclining-Plane at 1, otherways should have drawn it thro' the Center as we did before.

Lastly, Erect the Stile perpendicular to the Substile, making an angle therewith equal to the Elevation thereof; namely, 31 Deg. 28 Min. and the Dials are finished. And in making of these we have made two others also; viz. A North-Declining 72 Deg. Eastward, and Inclining 26 Deg. 34 Min. and a South-Declining Westward 72 Deg. and Inclining, as the other; all which are one, and may easily be apprehended by any Person that understands the former Problems.

I ALL O B. XIV. *A General Rule to know which Pole, whether the North or the South, is to be elevated over any Plane.*

The Stile of every Dial respecteth (or rather lieth parallel to) the Axis of the World, and always pointeth upwards or downwards, to one of the Poles. Now, when we have drawn our (though truly) we may be to seek, whether it be the North or South-Pole that must be elevated; wherefore to avoid any trouble, and to know which Pole is to be elevated, observe the General Rule.

Upon

## 94 Gnomonical or Dialling Problems

Upon all Upright-Planes, { South } Side the { South } Pole,  
whether Direct or Declining, upon the { North } Side to the { North } Pole.

Upon all Recliners { North } Pole,  
East and { the } Pole, whether Direct or Declining, upon the { South } Side to the { South } Pole.

Upon all South Incliners { South } Pole,

all { South Re-cliners } whether Direct or Declining. If Nadir be the { North } Pole, { South } Pole,  
North In-passed between the { Horizon } the { South } Pole.

This Rule being duly observed, there will be no Difficultie to find which is elevated.

A T A

ect. 4. Solv'd by the Globes.

95

A T A B L E of Meridional-Angles: Or,  
Angles which the Hour-Lines make  
with the Meridian, both in Horizontal  
and Erect South-Dials in all Latitudes.

Hor. Dial. Lat.	XI.	X.	IX.	VIII.	VII.	VI.	South Dial La.
	I.	II.	III.	IV.	V.		
d.	m.	d.	m.	d.	m.		
0	0	0	0	0	0	0	90
1	0	16	0	34	1	0	89
2	0	32	1	9	2	0	88
3	0	48	1	44	3	0	87
4	1	5	2	19	4	0	86
5	1	20	2	52	4	58	85
6	1	36	3	27	5	58	84
7	1	52	4	3	6	57	83
8	2	8	4	37	7	55	82
9	2	23	5	9	8	54	81
10	2	40	5	43	9	55	80
11	2	55	6	17	10	48	18
12	3	11	6	5	11	45	19
13	3	27	7	24	12	41	21
14	3	43	7	57	13	36	22
15	3	58	8	30	14	31	24
16	4	13	9	2	15	25	25
17	4	29	9	35	16	16	26
18	4	44	10	8	17	10	28
19	4	59	10	39	18	22	29
20	5	14	11	10	18	53	30
21	5	29	11	41	19	44	31
22	5	44	12	12	20	32	32
23	5	59	12	43	21	20	34
24	6	13	13	13	22	8	35
25	6	28	13	43	22	55	36
26	6	42	14	12	23	40	37

90 Degrees throughout.

A

96 Gnomonical or Dialling Problems,

A T A B L E of Meridional-Angles, &c.

F. Dial La	XI.		X.		IX.		VIII.		VII.		VI.		S. Dial La.
	I.	II.	I.	II.	III.	IV.	V.	VI.	VII.	VIII.	VII.	VIII.	
	d.	m.	d.	m.	d.	m.	d.	m.	d.	m.	d.	m.	
27	6	56	14	41	24	25	38	11	59	27	9	63	
28	7	10	15	10	25	9	39	7	60	17	61	61	
29	7	24	15	40	25	52	40	2	61	4	61	61	
30	7	38	16	6	26	33	40	5	46	1	49	60	
31	7	50	16	34	27	15	41	44	62	30	59	59	
32	8	5	17	12	27	55	42	30	63	11	58	58	
33	8	19	17	27	28	34	43	20	63	49	57	57	
34	8	31	17	54	29	13	44	5	64	24	56	56	
35	8	44	18	20	29	50	44	49	64	58	55	55	
36	8	57	18	49	30	27	45	31	65	30	54	54	
37	9	10	19	9	31	2	46	12	66	10	53	53	
38	9	22	19	34	31	37	46	50	56	29	52	52	
39	9	34	19	58	32	11	47	28	56	56	51	51	
40	9	45	20	21	32	44	48	7	57	21	50	50	
41	9	57	20	44	33	16	48	39	67	47	49	49	
42	10	10	21	7	33	46	49	12	68	11	48	48	
43	10	22	21	29	34	18	49	44	68	33	47	47	
44	10	32	21	51	34	47	50	10	68	54	46	46	
45	10	44	22	12	35	17	50	46	69	15	45	45	
46	10	54	22	33	35	44	51	15	69	35	44	44	
47	11	52	22	53	36	11	51	42	69	53	43	43	
48	11	17	23	13	36	37	52	9	70	11	42	42	
49	11	25	23	33	37	3	52	35	70	28	41	41	
50	11	35	23	52	37	28	53	0	70	43	40	40	
51	11	45	24	9	37	52	53	24	70	59	39	39	
52	11	55	24	27	38	15	53	46	71	12	38	38	
53	12	52	4	43	38	37	54	12	71	28	37	37	
54	12	13	25	2	38	58	54	29	71	41	36	36	
55	12	22	25	18	39	19	54	49	71	54	35	35	
56	12	32	25	34	39	40	55	9	72	5	34	34	
57	12	40	25	50	39	50	55	28	72	17	33	33	
58	12	48	26	5	40	1	55	45	72	28	32	32	

Degrees throughout.

A

## A T : B L E of Meridional-Angles, &amp;c.

Sc. S. Dial Lat.	Hor. Dial Lat.	VI.						South Dial Lat.
		XI. I.	X. II.	IX. III.	VIII. IV.	VII. V.		
63								
62								
61								
60	59	12 56 26	20 40	36 56	3 72	38		31
	60	13 4 26	34 40	54 56	15 72	48		30
	61	13 11 26	47 +I	10 56	34 72	58		29
	62	13 19 27	1 4 I	31 56	45 73	7		28
	63	13 26 27	13 4 I	42 57	373	15		27
	64	13 32 27	25 +I	57 57	17 73	24		26
	65	13 36 27	37 42	15 57	30 73	32		25
	66	13 46 27	49 42	25 57	43 73	39		24
	67	13 51 27	59 42	38 57	54 73	46		23
	68	13 57 27	9 42	50 58	573	53		22
	69	14 3 28	19 43	2 58	16 73	59		21
	70	14 7 28	29 43	13 58	26 74	5		20
	71	14 13 28	37 43	18 58	35 74	11		19
	72	14 18 28	46 43	24 58	44 74	16		18
	73	14 22 28	54 43	36 58	52 74	20		17
	74	14 27 29	2 43	52 59	0 74	25		16
	75	14 30 29	7 44	0 59	7 74	30		15
	76	14 33 29	15 44	8 59	15 74	34		14
	77	14 37 29	21 44	14 59	22 74	37		13
	78	14 41 29	27 44	22 59	27 74	40		12
	79	14 44 29	32 44	28 59	32 74	44		11
	80	14 47 29	37 44	34 59	37 74	47		10
	81	14 49 29	41 44	37 59	40 74	45		9
	82	14 51 29	45 44	40 59	44 74	51		8
	83	14 53 29	49 44	44 59	47 74	53		7
	84	14 55 29	22 44	48 59	51 74	55		6
	85	14 56 29	54 44	53 59	54 74	57		5
	86	14 57 29	55 44	55 59	55 74	58		4
	87	14 58 29	56 44	56 59	56 74	58		3
	88	14 59 29	57 44	57 59	58 74	59		2
	89	14 55 29	58 44	58 59	59 74	59		1
	90	15 0 30	0 45	0 60	0 75	0		0

## 98 Gnomonical or Dialling Problems,

PROB. XV. *The Day of the Month, and Hour of the Day, according to our Way of reckoning in England, being given, to find thereby the Babylonian, Italic, and the Planetary or Judaical Hours.*

1. To find the *Babylonian Hour* (which is the Number of Hours from Sun-rising.) Having found the Time of Sun-rising in the given Place, the Difference betwixt this and the Hour given is the *Babylonian Hour*.

2. To find the *Italic Hour*, which is the Number of Hours from Sun-setting.) Subtract the Hour of Sun-setting, from the given Hour, and the Remainder will be the *Italic Hour* required.

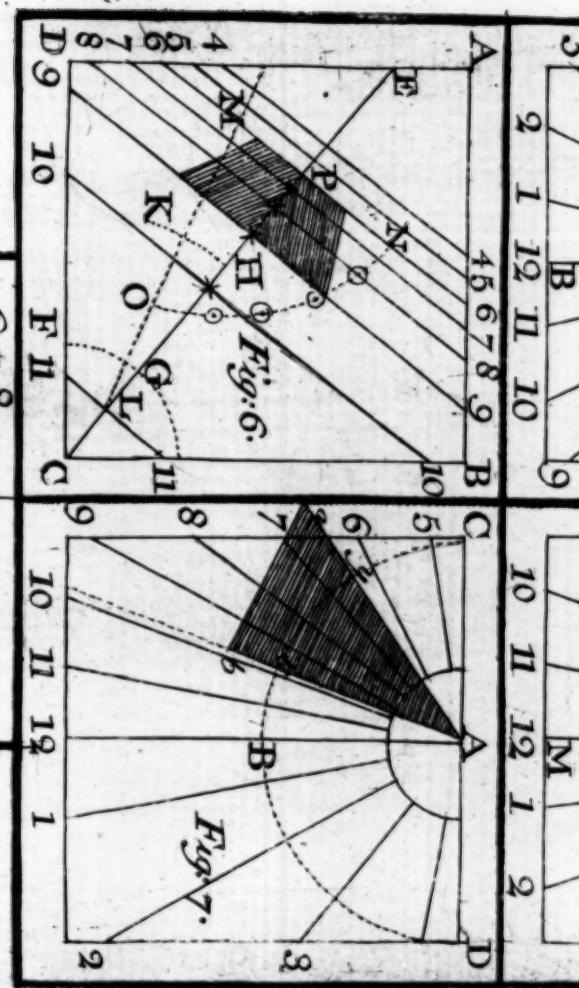
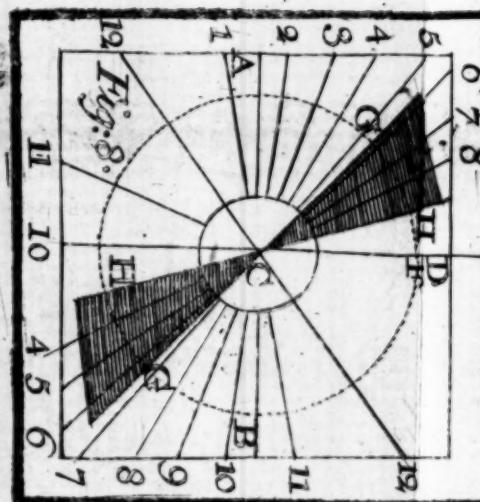
3. To find the *Planetary or Jewish Hour*, (which is  $\frac{1}{12}$  Part of the Artificial Day.) Find how many Hours the Day consists of; as say, as the Number of Hours the Day consists of, is to 12 Hours, so is the Hour since Sun-rising, to the *Planetary or Jewish Hour* required.

Thus, If the Sun rises at 4 o'Clock, (consequently it sets at 8) and the Hour given be 5 in the Evening, the *Babylonian Hour* will be the 13th; the *Italic* the 21st; and the *Planetary or Jewish Hour* will be Nine and three Quarters.

The Converse being given, the Hour of the Day, according to our Way of reckoning in England may be easily found.

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TRIGON



J. C. Smith Sc.

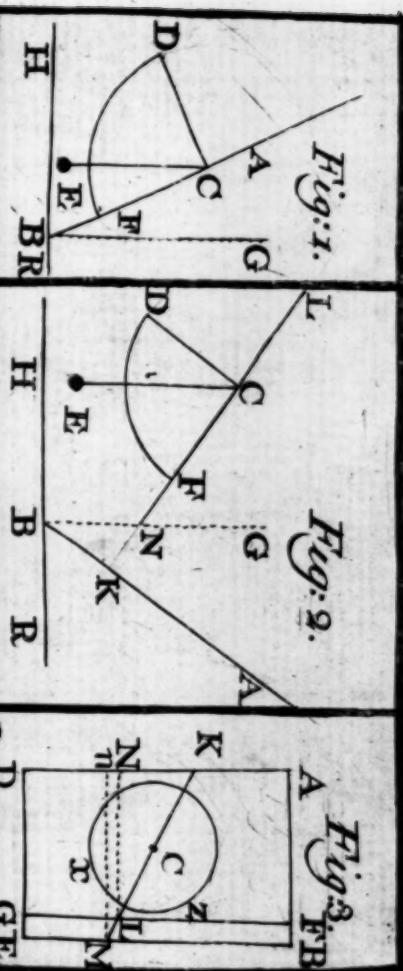
Plate II.

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*Fig: 1.*

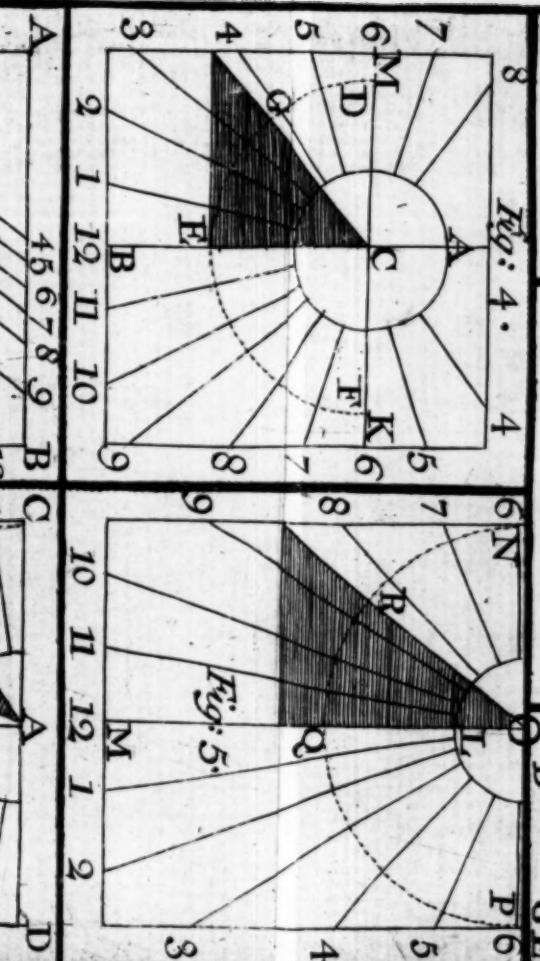
*Fig: 2.*

*Fig: 3.*



*Fig: 4.*

*Fig: 5.*



# TRIGONOMETRICAL PROBLEMS.

Solv'd by the

# GLOBES.

## SECT. V.

### *of the Solution of, SPHERICAL-TRIANGLES upon the GLOBE.*

**S**PHERICAL-TRIANGLES are best represented by the Circles on, and those appendant to the Globes: The Globe being the Original from whence all Spherical-Trigonometry proceeds, and upon which the Sides and Angles of all Spherical-triangles are most naturally represented and most expeditiously measured.

**Definition I.** A Spheric-Triangle is bounded by the Arks of three great Circles of the Sphere, or Globe, each Ark being less than a semicircle, or 180-Degrees.

**Def. II.** A Spheric-Angle is the same with the Inclination of the Planes of those two Circles which constitute the Angle; and

if from the Point of any *Spheric-Angle* as a *Pole*, we describe a *Circle* at the Distance of  $90^{\circ}$  Degrees from that Point, the Arc of this *Circle* intercepted between the Legs of the Angle is the Measure of it.

*Def. III.* When a *Spherical-Angle* has one or more Right-Angles; that is, contains  $90^{\circ}$  Degrees, it is call'd a *Right-angle Spherical-Triangle*: If all its Angles be acute, that is, each of them less than  $90^{\circ}$  Degrees, it is call'd an *Acute-Angled Triangle*; and if all its Angles be *Obtuse*, each exceeding  $90^{\circ}$  Degrees, or some of them be *Obtuse* and some *Acute*, it is called an *Obtuse-Angled Spherical-Triangle*.

*Def. IV.* The Complement of a Side or Angle to a Quadrant or  $90^{\circ}$  Degrees, is so much as that Side or Angle wants of  $90^{\circ}$  Degrees; and their Complement to a Semicircle, is so much as that Side or Angle wants of  $180^{\circ}$  Degrees.

*Def. V.* If two great *Circles* of the *Sphere* pass through each other's *Poles*, those two great *Circles* intersect each other at Right-Angles; but if they intersect each other, and do not pass through each other's *Poles*, those two *Circles* shall intersect each other at Oblique-Angles.

*Def. VI.* If a *Spherical-Triangle* hath three Right-Angles, the three Sides of that Triangle shall be all Quadrants, as in a Parallel-Sphere, the Brass-Meridian cutting the Horizon in North and South at Right-Angles, the Equinoctial Colure cutting the Horizon in the East and West-Points at Right-Angles; and the Meridian and Colure intersecting each other in the Poles of the World at Right-Angles; do constitute a *Spherical-Triangle* with three Right-Angles; and the three Sides of this Triangle for this Reason, shall be all of them Quadrants.

*Def. VII.* The Sides of *Spherical-Triangles* are of the same Affection or Kind with their opposite Angles.

*Def. VIII.* All great *Circles* must cut each other in two equal Parts, because their common Intersection is a Diameter of the Sphere, and consequently the two Points of Intersection are at the Distance of a Semicircle from each other.

*Def. IX.* The opposite Angles at the Intersection of two *Circles*, are always equal, because the same Plane constitutes both Angles.

PROB. I. To Project the Sphere for the Latitude 51 Degrees 30 Minutes North, Geometrically.

Quarter the Circle, which represents the Solstitial-Colure or Meridian, with Z N the Prime-Vertical, and H O the Horizon : then set the Chord of the Latitude 51 Deg. 30 Min. from H P, the Pole : from Z the Zenith to A the Equinoctial from S, and from N to Q, and draw AQ the Equinoctial, PS the Equinoctial-Colure, from A and Q on both Sides, off the Chord of  $23\frac{1}{2}$  Degrees for the Tropics S and V, draw SXV the Ecliptic; lay a Rule from A to S, which cuts PS in L, then thro' the three Points S L V, draw the Tropic of S, which suppose the apparent Course of Sun for that Day, which cuts the Horizon at O, thro' the three Points P O S draw the Meridian P O S, which forms first and third Triangles shaded, and at 6 a Clock. the Sun appears at L, thro' ZLN three Points, draw the Vertical EN, which forms the fourth shaded Triangle XLE. Again, suppose the O at M, thro' the three Points ZMN, draw the Sun's Distance ZMN, and draw thro' PMS the Meridian PMS, which is formed both the second and fifth shaded Triangles V, and PZM.

### PROB. II.

In the Right-Angled Spherical-Triangle HOP, Plate 3.

Figure I. Right-angled at H are

$\angle PH$ , the Latitude 51 Deg. 30 Min.

$\angle PO$ , the Sun's Distance from the Pole 69 Deg. 30 Min.

Required  $\begin{cases} \angle HO, \text{ the Complement of the Sun's Amplitude.} \\ \angle HP, \text{ the Hour of the Sun's Rising, accounted from Midnight.} \\ \angle PHO, \text{ the Angle of the Sun's Position, which the Horizon makes with the Meridian.} \end{cases}$

To represent this Triangle on the Globe.

Elevate the Pole to the given Latitude, and turn the Globe about till  $69\frac{1}{2}$  Degrees of the Equinoctial-Colure counted from the Pole, be at the Horizon, so will the Triangle be perfectly described

## 1021 Trigonometrical Problems,

described by an Arch of the Brass Meridian, an Arch of the Horizon, and an Arch of the Colure.

The Complement of the Sun's Amplitude,  $H\odot$ , is numbered on the Horizon, from the Colure to the North-Point of the Horizon, and in this Case is 57 Deg. 34 Min.

For the Angle  $H\odot O$ , count the Degrees of the Equinoctial, which are contained between the Colure and the North-Side of the Brass Meridian, which Degrees, reduced to Time, i.e. Degrees 45 Minutes are equal to 4 Hours 15 Minutes, the Hours from Midnight, the Time of Sun-rise, and half the Length of the Night, which subduct from 12, leaves 7 Hours 45 Minutes, the Time of Sun-set, and half the Length of the Day.

For the Angle  $P\odot H$ , number on the Colure, and also on the Horizon, the Sides that include the Angle 90 Degrees from the Angular-Point, and the Distance between those two Points where Reckoning ends, measured by the Quadrant of Altitude or by Compasses, contains 56 Degrees 39 Minutes, the Angle of the Sun's Position.

### PROB. III.

In the Right-angled Spherical-Triangle,  $Xyz$  Right-angled at  $y$ , Plate 3. Figure 2.

Given  $\{ Xz$ , the Sun's Distance from  $V$  72 Degrees.  
 $\{ yXz$ , the Sun's greatest Declination 23 Deg. 29 Min.

Required  $\{ zy$ , the Sun's present Declination.  
 $\{ Xy$ , the Sun's Right-Ascension.  
 $\{ yzX$ , the Sun's Position, or the Angle that the Sun makes with the Ecliptic.

To represent this Triangle on the Globe.

Bring the Sun's Place, which is  $II 12$  Deg. to the East Meridian, and fix the Globe in that Position, and the Triangle will be represented by an Arch of the Equinoctial, an Arch of the Ecliptic, and an Arch of the Brazen Meridian.

The Sun's present Declination  $Xy$  22 Deg. 16 Min. is measured on the Brazen Meridian, from the Equinoctial to the Sun's Place, and is North, because betwixt the Equinoctial and the North-Pole.

The Sun's Right-Ascension  $Xy$ , is measured on the Equinoctial 70 $\frac{1}{2}$  Deg. from  $V$ , to the Brass Meridian.

And for the Measure of the Angle  $y z X$ , number 90 Deg. the Meridian from the Sun's Place, and 90 Deg. on the Ecliptic from the Sun's Place, so shall the Distance between these two Points, measured by the Quadrant of Altitude, contain for the Angle  $y z X$ , 82 Deg. 20 Min.

## PROB. IV.

In the Right-angled Spherical-Triangle  $A \odot B$ , Right-angled at  $B \odot$ , Plate 3. Fig. 3.

Given  $\odot A B$ , the Complement of Latitude 38 Deg. 30 Min.  $\odot B \odot$ , the Sun's Declination 20 Deg. 30 Min. North.

Required  $\begin{cases} A \odot, \text{ the Sun's Amplitude.} \\ A B, \text{ the Ascensional-Difference.} \\ A \odot B, \text{ the Sun's Position at Rising.} \end{cases}$

To represent this Triangle on the Globe.

Express the Equinoctial below the North-Point of the Horizon 38 Degrees 30 Minutes, the Complement of the Latitude, and number 90 Deg. the Sun's Declination on the Equinoctial-Colure, and bring that to the East-Side of the Horizon, where the Triangle will be formed, and appear below the Horizon by  $A \odot$ , an Arch of the Horizon.  $A B$ , an Arch of the Equinoctial. And  $B \odot$ , an Arch of the Colure.

$\odot A \odot$ , the Sun's Amplitude from the East, is numbered on the Horizon to the Colure, and is 32 Degrees 26 Minutes.  $A B$ , the Ascensional-Difference, is numbered on the Equinoctial from the East-Point of the Horizon to the Colure, and is 2 Deg. 15 Min. which reduced into Time, is 1 Hour 49 Min. more 6, for Sun-rise, i. e. 4 Hours 11 Minutes.

And the Angle of the Sun's Position  $A \odot B$ , is found by continuing the Sides  $\odot A$  and  $\odot B$  to Quadrants, and then Trisecting the Angles lying betwixt those two Points, as in the second and third Problems.

## PROB. V.

In the Right-angled Spherical-Triangle  $A E L$ , Right-angled at  $E L$ , Plate 3. Figure 4.

Given

Given  $\begin{cases} AL, \text{ the Sun's Declination equal to } 20 \text{ Deg. } 30 \text{ Min. N.} \\ LAE, \text{ the Latitude equal to } 51 \text{ Deg. } 30 \text{ Min. North.} \end{cases}$

Required  $\begin{cases} SLE, \text{ the Sun's Altitude at Six.} \\ A E, \text{ the Sun's Azimuth from East.} \end{cases}$

$\begin{cases} ALE, \text{ the Sun's Position or Angle, which the Colure makes with the Vertical at Six.} \end{cases}$

To represent this Triangle on the Globe.

Elevate the Pole to the given Latitude, fix the Quadrant Altitude in the Zenith, and number the Sun's Declination  $20\frac{1}{2}$  Degrees on the Equinoctial-Colure, the Colure being brought to the East-Point of the Horizon, bring the graduated Edge of the Quadrant, over the Sun's Declination on Colure, so will the Triangle be form'd by,

AL an Arch of the Colure equal to the Declination.

AE an Arch of the Horizon equal to the Azimuth, from the East.

LE an Arch of the Quadrant equal to the Sun's Altitude.

( AE, the Sun's Azimuth from East is  $13 \text{ Deg. } 6 \text{ Min.}$   
LE, the Sun's Altitude at Six, is  $15 \text{ Deg. } 54 \text{ Min.}$   
the Angle of the Sun's Position ALE, is found by combining the Sides LA and LE to Quadrants, and then measuring betwixt those two Points, as in the second and third Part.

### Of Oblique-angled Spherical-Triangles.

#### P R O B. VI.

In the Oblique-angled Spherical-Triangle P Z M, Plate 5. Oblique-angled at Z.

Given  $\begin{cases} ZP, \text{ the Complement of the Latitude equal to } 38 \\ 30 \text{ Min.} \\ MP, \text{ the Sun's Distance from the Pole equal to } 69 \\ 30 \text{ Min.} \\ MZ, \text{ the Complement of the Sun's Altitude equal to } 47 \text{ Deg. } 20 \text{ Min.} \end{cases}$

Required  $\begin{cases} PZM, \text{ the Sun's Azimuth from the North,} \\ ZPM, \text{ the Hour of the Day from Noon.} \\ ZMP, \text{ the Sun's Angle of Position.} \end{cases}$

*To represent this Triangle on the Globe.*

Elevate the Pole to the Latitude, then count Z P 38 Deg. 35 Min. the Complement of the Latitude from the Pole, on the South-Side of the Brazen Meridian, and where the Reckoning ends, screw the Quadrant of Altitude, i. e. on the Zenith, which is markt 51 Deg. 30 Min. on the Brass-Meridian this done, count the Side M P 69½ Deg. upon the Equinoctial-Colure from the Pole, and the Side M Z equal to 47 Deg. 20 Min. on the Quadrant of Altitude, from the Zenith downwards, and so move the Globe and Quadrant of Altitude together, till the Numbers counted on the Colure and Quadrant of Altitude, meet in one Point, so will the Triangle be exactly delineated upon the Globe.

*Now to find the several Angles.*

For the Angle Z, count the Number of Degrees of the Horizon, which are contained between the North-Point of the Meridian, and the Quadrant of Altitude 115 Deg. 35 Min. the Sun's Azimuth from the North.

For the Angle Z P M, the Degrees of the Equinoctial, contain'd between the South-Side of the Brass Meridian, and the Colure 45 Deg. reduced into Time, is 3 Hours from Noon, & 9 in the Morning, or 3 Afternoon.

For the Angle Z M P, the Angle of Position, reckon 90 Deg. from the Point M, on the Circles M Z and M P, the Distance betwixt those Points measured by the Quadrant of Altitude, applied to both, give 36 Deg. 52 Min. the Angle sought, made by the Meridian and Vertical concurring in M. Also by having three Parts of any Oblique-Triangle given, the other three may be found, which afford no less Variety, than 60 Cases in an Oblique, and 30 in a Right.

As will appear, if we call the Latitude 1. the Sun's Declination 2. Azimuth 3. Altitude 4. Position 5. Hour 6. Then may each of these be found from 10 different Data's

# 106 Trigonometrical Problems,

1	2	3	4	5	6
may be found from the Ten different Data's, directly underneath.					

1 2.3.4	1.5.6	1.5.6	1.5.6	2.3.4	2.3.4
2 2.3.5	1.4.6	1.4.6	2.3.5	1.4.6	2.3.5
3 2.3.6	1.4.5	1.4.5	2.3.6	2.3.6	1.4.5
4 2.4.5	1.3.6	2.4.5	1.3.6	1.3.6	2.4.5
5 2.4.6	1.3.5	2.4.6	1.3.5	2.4.6	1.3.5
6 2.5.6	1.3.4	2.5.6	2.5.6	1.3.4	1.3.4
7 3.4.5	3.4.5	1.2.6	1.2.6	1.2.6	3.4.5
8 3.4.6	3.4.6	1.2.5	1.2.5	3.4.6	1.2.5
9 3.5.6	3.5.6	1.2.4	3.5.6	1.2.4	1.2.4
10 4.5.6	4.5.6	4.5.6	1.2.3	1.2.3	1.2.3

the Stars-Longitude from  $\odot$ , and PMZ the Angle of the Stars Position.

The same Triangle may be applied to sundry other Uses in *Geography, Navigation, and Dialling.*

Thus may we serve the five Parts of a Right-angled Spherical-Triangle.

Moreover, in the same Triangle, call the Side ZP, the Distance of the Pole of the Equinoctial, from the Pole of the Ecliptic, then PM will be the Co-declination of a Star at M, ZM will be the Complement of the North-Latitude of that Star, the Angle MPZ, will be the Complement of the Stars Right-Ascension; the Angle PZM,

NAUTICAL

NAUTICAL PROBLEMS,  
OR,  
PROBLEMS  
In NAVIGATION,  
Solv'd by the  
GLOBES.

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S E C T. VI.

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*P RÆCOGNIT A.*

HERE are four Fundamentals whereon the *Art of Navigation* depends. 1. The *Course* found by the *Compass*, regarding the *Variation*. 2. The *Distance* measured by the *Log* and *Half-Minute-Glass*, allowing for *Lee-way*. 3. The *Latitude* found by *Celestial Observation* of the *Sun* or *Stars*. The *Longitude* found by Help of two of the foregoing: no instrumental Way at Sea of immediately finding being discovered, that hath been certain and practicable: That of *Mulum Watches*, and the *Eclipses* of the *Satellites* of *Jupiter* bid Fairest of any I know.

Before I begin any *Problem*, I shall premise a few Words of *use* and *Distance*, as describ'd on the *Globe*.

- AL 1. Rhumb-Lines make equal Angles with all Meridians on the Globe.
- 2. An equal Part of the Rhumb altereth the Latitude equal in all Places,

P 2

3. They

3. They are represented by Spiral-Lines winding about the Globe, and continue inclining towards the Pole; where they seem confused, never passing thro' the Poles.

4. The Bearing found by help of the Quadrant, is not the true Rhumb leading from one to the other, which may be thus proved by finding the Bearing of the Second from First, which will not be the opposite Point, but 'tis the Angle of Position (i. e.) the Angle which the Arch of a great Circle passing vertically over the two Places makes with the Meridian of the first Place.

5. A Great Circle inclining to the Meridian, maketh greater Angles with all other Meridians, than with that from whence it was drawn.

6. By the Distance is to be understood the shortest Distance or their Distance in the Arch of a great Circle, which is less than their Distance in the Rhumb leading from one to the other, except both Places lye under one Meridian, or under the Equator in as much as a great Circle on the Globe, like a straight Line on a Plane is the shortest of all Lines or Circles possible to be drawn.

7. Wherefore the Distance in the Rhumb must be thus less than or measured: Take a Degree or two of the Equator, and turn it over upon the Rhumb, for if it be measured all at once Extent on the Rhumb then would it be the distance in the Arch of a great Circle.

### P R O B L E M I.

*To find the Difference of Latitude betwixt any two Places.*

1. BRING both Places, either at once to the Meridian, or in the same Longitude, or one after the other, if of different Longitudes. 2. The Degrees intercepted by the Sun on the Meridian is the Difference of Latitude sought.

P R O B. II. *To find the Latitude, Hour, Sun's Altitude and Azimuth, the Globe, Sun-shine, and the Day of the Month.*

1. Fix the Globe Horizontally. 2. Set a Spheric Gnomon exactly on the Sun's Place (found against the Day of the Month on the Horizon) in the Ecliptic, which bring to the Meridian, and the Index to 12 at Noon. 3. Move the Globe upward and downward Eastward and Westward, till it cast a

Shado

adow on any Side. 4. Then the Degree of the Meridian cut by the Horizon is the Latitude sought.

*Note.* The Index points at the Hour. Then apply the Quadrant to the Zenith, and over the Sun's Place on the Quadrant is the Altitude. And where the Quadrant cuts the Horizon is the Azimuth on the Horizon.

otherwise, By the Meridian-Altitude of Sun or Stars.

Bring the Sun's Place or Star to the Meridian. 2. And when it count on the Meridian the Number of Degrees equal to the Meridian-Altitude given where the Count ends, bring to the South-Point of the Horizon, if observed on the South, but to the North, if observed on the North off the Zenith. 3. So will the Elevation of the Pole shew the Latitude.

### SYNOPSIS of all the possible Varieties, that can happen in working an Observation at Sea.

Sun or Stars Declination.	Situ- ation.	Sun's Sha- dow.	Rule.	What Latitude
N°	S°d.	N°d.	Add the Declination and Zenith Distance, the Sum is the Latitude.	N°
S°	N°d.	S°d.		S°
N°	N°d.	S°d.	The Difference of them is the Latitude, when the Zenith-distance is greater.	S°
S°	S°d.	N°d.		N°
N°	N°d.	S°d.	But when the Zenith- Distance is less than the Declination. the Differ- ence is the Latitude.	N°
S°	S°d.	N°d.		S°
neat all	Zenith	No Shad.	The Zenith-Distance is the Latitude.	S° O N°
N°	N°d.	S°d.		
S°	S°d.	N°d.		
On the Zenith	No Sha- dow.	No Sha- dow.	The Declination is the Latitude.	N° S°

*Note.*

*Note.* { N° S° N°d. S°d. } stands for { North South Northward Southward }

Betwixt the 10th of March and the 12th of September  
Declination of the Sun is North, and betwixt the 12th of September and 10th of March the Declination is South.

But if the Sun or Star do not Rise or Set in 24 Hours observe this General Rule.

If the Object observed be above the Pole the Sum of the Meridional Difference

**an-Altitude and Complement of Declination, is the Latitude of the same Name with the Declination.**

Or without the Declination, observe the Meridian-Altitude when above the Pole, and when below : Half their Sum is Latitude.

**P R O B. III.** *To find the Difference of Longitude of two Places.*

1. Bring both Places to the Meridian, one after another, diligently marking what Degree of the Equator is cut by the Meridian, when each Place is under the Meridian. 2. The Degree on the Equator so intercepted is the Difference of Longitude.

*Note.* The Degree of Longitude of one and the same Place by different Authors, may vastly differ in Number, yet this is true; because of the Variety of first Meridians, or Beginnings of Longitude, which breed Confusion; and the more, because each Author doth not keep always the same, nor tell whence he begins Longitude, and if some do, perhaps they tell not whether the *East*, *West*, or Middle of the Island, it were 3, 4, or 5 Degrees broad.

TABLE of the several first Meridians, by whom used, and their Difference in Longitude from *Pico de Teneriffa*.

used by	the Spanish Mercator	and differs from <i>Pico de Teneriffa</i>	Deg.	Min.
	<i>Moxon</i>		15	55
	<i>Dutch</i>		13	25
	<i>English</i>		10	25
	<i>French</i>		9	
			8	5
			2	20

of which seem to me to have the chief Properties of a chosen first Meridian, which, with due Respect, I propose the Judgment of the Learned.

That it be on the Equator, because thereon Longitude is known.

That it be some small Island not above half a Degree distant, to prevent Errors, whether Side of it soever Longitude makes.

That it stand by it self, not confounded with other.

If it divided the two Continents, *America* from *Europe*, and *Africa*, it would be more conspicuous.

On Search, in the Dutch Maps, such a Place appears, called *Teneriffa*, having all the above Properties West from *Pico de Teneriffa*, distant about 9 Degrees of Longitude, tho' to speak the Truth, I found it not elsewhere.

Noting before in the *Præcognita* two instrumental of detecting Longitude, something further concerning Manner follows.

#### B. IV. To find the Longitude by Pendulum-Watches.

Take at least two Watches, that if one should stop by Misshap or Neglect, the other may keep going.

Keep them close, free from Moisture or Dust.

Let them be well adjusted by an Equation-Table, before they are taken to Sea, and kept going while at Sea.

Set them to the exact Moment of Time observed by the Sun at the Place left, regarding the Equation-Number.

When arriving at the Place whose Longitude is sought, observe exactly the Time by the Sun in that Place, and also by

by the Watch, allowing for the Equation; if they both agree exactly, there is no Difference of Longitude. But if the Time of the Day there be greater than that shewn by the Watch, then the Difference of Longitude is Easterly: but if less, Westerly.

6. Convert the Difference of Time into Degrees, which will be the Difference of Longitude in Degrees with greater Exactness than those Ways that depend upon Tables, so various among themselves, such as Calculations of Lunar-Eclipses, which are as laborious as uncertain, and their true Beginning or Ending are scarce to be distinguished for some Minutes by Reason of the Penumbra: tho' four Minutes in Time will alter the Longitude a whole Degree.

7. To convert Time into Degrees, or Degrees into Time.

Remember	Time.			{	Deg.	Min.	Sec.	Deg.	Min.	Sec.	Deg.	Min.	Sec.	
	Hours.	Min.	Sec.											
	1	0	0					15	0					
	0	4	0					1	0					
	0	1	0					0	15					
	0	0	4	{	is equal to			0	0					
Thus	Hours.	Min.	Sec.					Deg.	Min.					
	3	42	32	=				55	32					
For	3	0	0	=				45	0					
	0	40	0	=				10	40					
	0	2	0	=				0	30					
	0	0	32	=				0	0					

8. Wherefore, considering the vast Improvement in Work by the Learned Dr. Hook, the Ingenious Hugenot, whose very first Work, being try'd by Major Holms, proved both Satisfactory and Useful in a great Streight, and met with Commendation, and the Approbation of the States of Holland, insomuch that he obtain'd a Patent for them; this seems to shew its Readiness, and to be done by one alone, no despatching Way, tho' not infallible.

PROB. V. To find the Longitude by the Satellites of Jupiter.

1. This above all claims the first Place by Geographers, principally by their Eclipses, both because they are frequent, being almost Momentaneous.

2. This (as before) requires the exact Time of their appearing in both Places, either their Immersion or Emergence.

which may be obtained by taking exactly the Altitude of a  
fixed Star at the same Instant.

the Time 3. Reduce this Difference of Time into Degrees of Longitude  
Watch-side, as before taught.

4. 'Tis true, as this is less fallible than the Former, so 'tis less  
inconvenient at Sea, as requiring a long Telescope not to be managed  
well a Ship-board, also the joint Assistance of some able  
Observators at both Places, tho' it may be of extraordinary  
service to rectify the Longitude of Sea-ports, when they are on  
various Islands.

### R O B. VI. Betwixt two Places to find the Course.

1. Observe the Rhumb that passeth thro' them, which is it :  
if none runs thro' them, that Rhumb which runs most parallel to them is the Course.

### R O B. VII. To find how many Miles are in a Degree of Longitude in any Latitude.

1. In the given Parallel take 20 Degrees, and measure them  
on the Equator. 2. The Number whereof there tripled will  
give the Number of Geographical Miles (60 of which make a  
Degree of Latitude.)

### R O B. VIII. A Place given of a certain Distance from us; to find all the Places of like Distance.

1. Rectify the Globe to our Latitude. 2. Bring that Place  
to the Meridian. 3. To the Zenith affix the Quadrant. 4.  
Mark what Degree of the Quadrant the other given Place  
occupies. 5. All the Places passing under that Degree, while the  
Globe is turned round, are of the like Distance.

### R O B. IX. Course and Distance given; to find the Latitude and Longitude arrived at, supposing the Place left be known.

1. Make a small Mark on the Rhumb given in the Latitude  
of the Place left. 2. Bring that Mark to the Meridian, which  
then

then cuts the Equator in its Longitude, which we will call the Longitude left. 3. Reduce the Distance sail'd into Degrees. 4. Take one Degree from the Equator, and turn it over to the Rhumb, as oft as there be Degrees in the Distance given. 5. At the End of the Distance make a Mark, which bringeth the Meridian, whereon is the Latitude arrived at. 6. The Meridian cuts then also the Equator in the Longitude of the Point, which compared with the Longitude left, we get the Difference of Longitude, and consequently the Longitude arrived at, if we add it to, or subtract it from the Longitude left, according as the Course hath been East or West.

**P R O B. X.** *Both Latitudes and Course given; to find their Distance, and Difference of Longitude.*

1. Turn the Globe till the given Rhumb cuts the Meridian in the Latitude left. 2. There mark the Rhumb, and observe then the Degree of the Equator cut by the Meridian, call it the Longitude of Departure. 3. Turn the Globe till the same Rhumb cut the Meridian in the Latitude arrived at, under which on the Rhumb make a Mark, and find the Longitude of this second Mark, which compared with the Longitude of Departure gives the Difference of Longitude. 4. Turn over a Degree of the Equator as oft as is possible betwixt two Marks on the Rhumb, for the Number of Degrees the Places are distant on the Rhumb.

**P R O B. XI.** *The Latitude and Longitude of Places given; to find their Course and Distance.*

1. Find the Places themselves, then their Course and Distance, by the Sixth Problem foregoing.

*Note.* 'Tis best working these Questions on the Globe, where fewest Places are painted.

*Note.* By some of the foregoing Problems, the Mariner can find the Way the Ship hath made, and make Pricks on the Globe in their proper Places for every Day's Voyage, and so consequently know where they are, how far from their known Port or desired Haven, thus truly representing their Voyage with less Trouble and more naturally than by any Verse or Journal whatever.

PROB. XII. The Distance of two Places situate on the same Meridian, with their Angles of Position they make with a third Place; to find that Place with its nearest Distance from each of the other two.

1. Rectify the Globe to the Latitude of the first, and fix the Quadrant to the Zenith. 2. To the Zenith bring the first given Place. 3. Extend the Quadrant to the Point of the Horizon in which it bears off the Third. 4. By the Side of the Quadrant make a small Trace with Chalk. 5. Elevate the Pole to the Latitude of the second Place. Bring it to the Meridian and the Quadrant to the Zenith. 6. Bring the Quadrant to the Point of the Compass on which it beareth from the Third. Where the Quadrant crosseth the chalk'd Line is the third Place whose Distance from the other two, find by the Degrees of the Quadrant of Altitude.

Note, By this one may plot any new Land, observing its Bearing from two known Points. the Bearing and Angle of Position not differing much in the narrow Compass of the semi-Horizon.

### PROB. XIII. To take the Altitude of a Star.

1. Fix the Globe Horizontal. 2. Move it up and down thro' the South Pole along the Axis the Star be directly over. 3. Then the Degree of the Meridian intercepted by the Horizon is the Stars Altitude.

### PROB. XIV. To learn the Names of the most noted Stars.

Rectify the Globe to the Latitude Day, and Hour of the Day; then if every Star on the Globe had a Hole, and the Eye was placed in the very Center of the Globe, and looking thro' the Hole, a direct Ray from the Eye thro' the Center of the Star if extended to the Firmament, would cut the same Star in the Heavens which that Star on the Globe represented; if the Globe was duly rectified and set exactly level, and the Meridian to the North, then would the Stars that be,

Rising		Rising	
On the Meridian	on the	on the Meridian	in the
On the Zenith	Globe be	on the Zenith	Heavens
Setting		Setting	
On any Azimuth		on the same Azimuth	
On any Almicanter		on the same Almican.	

Wherefore, take the Azimuth or Amplitude by a Compass or Altitude by a Quadrant of any Star whose Name is desired and find what Star hath the same Altitude and Azimuth by its either its Name, or what Part of the Constellation it possesses, as also its Magnitude, &c. It may be objected, that the Planets ♀, ♂, and ☽ especially, may cause the young Beginner to mistake; wherefore this shall be the next Problem.

### PROB. XV. To distinguish the Planets from the fixed Stars.

1. Planets don't twinkle commonly. 2. They are bigger than ordinary, ♀ and ☽ especially. 3. They are of differing Colors, ♂ of a leaden Color, and of third Magnitude, ♀ bigger than the First, of a Silver-Color, ♂ of the second Magnitude, of a Copper-Color, ☽ bigger than ♀, of a Glistering Color like new-coind Silver, ☽ of the third Size, Pale, White, like Quick-silver, never aboye 30 Degrees from the Sun, seldom seen but when he rises before the Sun or sets just after the Sun. 4. they shift their Places in a Week or two observably from some known fixed Stars. 5. Consult an Ephemeris to see in what Sign the Planets are, and if they are not in the Sign observ'd; know 'tis a fixed Star.

### PROB. XVI. To steer in the Night by the fixed Stars.

1. Rectify the Globe to the Latitude and Hour of the Day. Then turn the Globe till the Difference of Longitude passed thro' the Meridian, that is betwixt the Place left and the Place sail'd to. 3. If any Star in the Latitude and Longitude aim'd at, come to or near the Meridian, that Star then in or near the Zenith of the Port desired. Then

the Ship towards the same Star in the Heavens without  
still observing what Star is in or near the Zenith of the  
place sail'd to.

XVII. By the Globe to find the Variation of the Compass.

Observe by the Compass on what Point the Sun rises or sets; by the Globe find the Sun's true Amplitude, if they agree, then is there no Variation, if not, their Difference is the Variation sought. Which is Easterly, If the Sun rises on the Compass nearer the North, than on the Globe, sets on the Compass further from the North than on the Globe. But Westerly, if the Sun rises on the Compass further from the North, than on the Globe, or sets on the Compass nearer to the North than on the Globe. The like may be found at any Time, by comparing the Azimuth by the Compass, and the Azimuth by the Globe instead of Amplitude.

XVIII. Seeing two known Points or Capes of Land as we sail along; to find the Ship's Distance from them, by knowing their Bearing.

Pitch one Foot of a Pair of Compasses upon one Cape, the other Foot upon the Rhumb which points towards the other Cape; do the like by the other Cape with another Foot of Compasses, then move the Compasses so open'd by these two Rhumbs off from the Land, the very same Point where the two Feet which came from the two Capes do meet, is the Point where the Ship is, whole Distance measured by the Quadrant of Altitude.

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E R R A T A.

Line 29 and 38 for Miles read Geographical Miles. p. 75. l. 33. for Depression of a Star, &c. read Depression of the Sun when a Star of the Magnitude rises Heliacally.

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# PARADOXES

To be Resolved by the

# GLOBES

WHEREAS PATRICK GORDON the ingenious Author of the Geographical Grammar hath publish'd therein 41 verting and surprizing Paradoxes, of which, in my Mutual-Miscellany, I have attempted a probable Solution, and th<sup>t</sup>o have subjoined 55 more, with their certain Solution; which, when perused, will render the following Paradoxes proposed to the World by G. GORDON an easy and delighful Entertainment, with which I conclude this Treatise of both Globes.

I. THERE is on the Terraqueous Globe a certain Paral<sup>e</sup> of Latitude, to which a Ship may be supposed to sail, and have Sea-room, to depart from that Parallel; but such is the Situation of every Point of that Parallel of Latitude, that no Ship can sail the said Latitude, but upon one particular Point of the Compass; and Wind tho' it veer round all the 32 Points, will always blow ag<sup>t</sup> that Point upon which the Ship must sail from that Latitude, and Wind tho' blowing against the Point upon which the Ship must sail, the Ship may go directly before the Wind.

II. There are two Places on the Terraqueous Globe so situated respect to one another, that from each of those Places a Ship may sail, and tho' they have Sea-room to all the 32 Points, yet it is impossible for them to sail from those Places but upon opposite Points of the Compass; and tho' they sail upon opposite Points, yet they may, upon those Points be either following or meeting one another.

ect. 6. Resolv'd by the Globes. 119

I. There is a certain Place of the Terraqueous Globe to which the sun and Moon rise always in the South, and set in the South.

II. There are two Places of the Earth which bear directly North and south of one another, and their Distance from each other is 100 Miles, but the true Course from one of those Places to the other is to sail 50 Miles due North, and 50 Miles due South.

III. There is a certain Place on the Terraqueous Globe to which a Ship may sail directly upon one Point of the Compass; but there are other fourteen Points on which a Ship may sail towards that Place, but if she continue to sail upon e'er a one of the Fourteen, she will always approach nearer to the aforesaid Place, but will never be able to come to it.

IV. There is a certain Parallel of Latitude upon which a Ship may sail round the Globe, and may all that Time observe the Body of the Sun, without his being above the Horizon.

V. There is a certain Place of the Earth from which two Ships may depart on one and the same Day yea, and on the same Hour and Minute of that Day, and upon one and the same Point of the Compass, may continue to sail with the same Velocity for the Space of 24 Hours, and tho' they depart from the same Place, and at the same Time, and both sail upon the same Point of the Compass, with the same Velocity, yet in 24 Hours, they will be distant from one another above 1000 Italian Miles.

VI. There is a certain Parallel of Latitude upon which a Ship may sail at the Rate of 12 Italian Miles an Hour and in 24 Hours her Velocity measured in Degrees of the Equator, shall be equal to the Velocity of the Sun on the 10th of June.

VII. There is a certain Place of the Earth, from which a Stone of about 10000 Weight could not fall, tho' a Pit were digged all round it, and that which is the Cause of other Bodies falling from other Places, would be the only Pillar to support a Body in that Place.

VIII. There are two Parallels of Latitude, in one of which less Gold will make a Pound Weight than in the other.

IX. There are two Places of the Earth where one and same Vessel will hold more Wine or Water in the one Place than in the other.

X. There is a certain Parallel of Latitude from which two Ships may sail at one and the same Moment of Time, with respect of real Time, and with respect of apparent Time, will differ one entire natural Day; but there is another Parallel of Latitude, to which, if those two Ships sail upon one and the same Point of the Compass, with the same Velocity, they shall arrive at that certain Parallel of Latitude at one and the same Moment, both with respect to real and apparent Time.

XIII. There is a certain Place of the Earth, where all the fixed Stars still the same Altitude; and notwithstanding of the Diurnal Revolution of the Earth, they always bear upon the same Point of the Compass.

XIV. There are several Places at a considerable Distance from one another, lie all directly East of London, but London does not lie directly from any of the said Places.

XV. The Christians observe the first Day of the Week for their Sunday, Jews the Seventh for their Sabbath, and the Turks the sixth Day of the Week for the Time of their Worship; but there is a particular Place on the Terraqueous Globe to which, if a Christian, Jew, and Turk sail in one and the same Ship, they shall keep the Time for their Worship on different Days, and not all the Time they are sailing to that particular Place; but when they arrive at that Place, and during the Time they remain at it, they shall all keep their Sabbath on one and the same Day; but when they part from that Place, they shall all differ as before.

XVI. There is a certain Port, from which, if three Ships depart at the same Time, and sail on three particular different Courses, till they arrive to the Port they departed from, and if in one of these Ships be Christians, in the second Jews, and in the third Turks, when they return to the Port they departed from, they shall differ so with respect to real and apparent Time, that they all shall keep their Sabbath on one and the same Day of the Week and yet each of them, separately, shall believe that he keeps his Sabbath on the Day of the Week his Religion requires.

XVII. There is a certain Country in the North-Temperate-Zone, where the Inhabitants the Bodies of the three Superior Planets, Saturn, Jupiter, and Mars appear to be most enlighten'd, when they are actually least enlightened.

XVIII. There is a Continent all lying in the North-Side of the Equator, whose Inhabitants the Body of the Sun seems to be nearest to them, and farthest removed from them.

XIX. There is a certain Parallel of Latitude, on which Parallel the Star, called the North-Polar-Star, appears, by Observation, to be 47 Deg. above the Horizon, and at another Time, the said Polar-Star will appear by an Observer on the same Parallel of Latitude, to be at the Horizon.

XX. There are two Places lying in the Torrid-Zone that are not above 10 Miles distant from one another, but if a Ship sail from one to the other, through one particular Point of the Compass, the Difference of Time between those two Places will actually be found to be above 23 Hours.

XXI. There are 24 Places on the Terraqueous Globe, in which all the Hours of the natural Day do always exist at the same Time and the Distance of any two of those Places does not exceed 60 Miles.

The GREAT ORRERY  
Four Feet in Diameter. Made by  
Tho: WRIGHT Mathematical Instru-  
ment maker TO HIS MAJES TY



Who makes Orrery's of differ  
as may be seen at his Shop  
**FLEET-STREET**



THE  
DESCRIPTION  
OF THE  
ORRERY,

*newly made by THO. WRIGHT, Ma-  
hematical Instrument-Maker to His  
MAJESTY.*

**T**HE ORRERY is an Astronomical Machine, made to represent the Motions of the Planets, as they really are in Nature: These Machines are made of various Sizes, some having more Planets than others; but I shall here confine myself to the Description of those mentioned.

The Frame which contains the Wheel-Work, &c. regulates the whole Machine, is made of fine Ebony and is near four Feet in Diameter; the outside of it is adorned with twelve Pilasters, curiously wrought and gilt: Between these Pilasters, the twelve Signs of the Zodiac are neatly painted, within gilded Frames. Above this is a broad Ring, supported with twelve small pillars: This Ring represents the Plane of the Ecliptic, in which there are two Scales of Degrees, and before those the Names and Characters of the twelve Signs.

Near the Outside is a Scale of Months and Days, exactly corresponding

*Orrery.*

*The Description  
of the Orrery.*

*Vide Orrery  
p. 121.*

corresponding to the Sun's Place at Noon, each Day throughout the Year.

Above the Ecliptic stand some of the principal Circles of the Sphere, according to their respective Situation in the Heavens, viz N° 10, are the two *Colures*, divided into Degrees, and Half Degrees: N° 11, is one Half of the Equinoctial Circle, making an Angle with the Ecliptic of  $23\frac{1}{2}$  Degrees: The *Ecliptic of Cancer* and the *Arctic Circle* are each fixed parallel, and at their proper Distance from the Equinoctial. On the Northern Half of the Ecliptic, is a brass Semicircle, moveable upon two Points fixed in  $\gamma$  and  $\Delta$ : This Semicircle serves as a moveable Horizon, to be put to any Degree of Latitude upon the North Part of the Meridian. The whole Machine is also contrived, as to be set to any Latitude, without affecting the least any of the inside Motions: For this purpose there are two strong Hinges (N° 13.) fixed to the bottom Frame, upon which the Instrument moves, and a strong Brass Arch, having Holes at every Degree, thro' which a strong Pin is to be passed according to the Elevation. This Arch, and the two Hinges support the whole Machine, when it is lifted up according to any Latitude; and the Arch at other times lies convenient under the bottom Frame.

When the Machine is set to any Latitude (which is easily done, by two Men, each taking hold of two Handies, conveniently fixed for that purpose) set the moveable Horizon to the same Degree upon the Meridian, and you may form an Idea of the respective Altitudes, or Depressions of the Planets, above or below the Horizon, according to their respective Positions with regard to the Meridian.

Within the Ecliptic, and nearly in the same Plane there stand the Sun, and all the Planets both Primary and Secondary. The Sun (N° 1.) stands in the middle of the whole System, on a Wire, making an Angle with the Plane of the Ecliptic, of about 82 Degrees, which is the Inclination of the Sun's Axis, to the Axis of the Ecliptic. Next the Sun is a small Ball, (N° 2.) representing Mercury: Next to Mercury is Venus (N° 3.) represented by a larger Ball, (and both these stand upon Wires, so that the Balls themselves may be more visibly perceived by the Eye.) The Earth is represented (N° 4.) by an Ivory Ball having some of the principal Meridians and Parallels and a little Sketch of a Map described upon it. The Wire which supports the Earth makes an Angle with the Plane of the Ecliptic of  $66\frac{1}{2}$  Degrees, which is the Inclination of the Earth's Axis to that of the Ecliptic. Near the Bottom of the Earth's Axis is a Dial-Plate, (N° 9.) having an Index pointing to the Hours of the Day, as the Earth turns round its Axis.

Ro

Round the Earth is a Ring supported by two small Pillars; which Ring represents the Orbit of the Moon, and the Divisions upon it answer to the Moon's Latitude; the Motion of this Ring represents the Motion of the Moon's Orbit according to that of the Nodes. Within this Ring is the Moon (N° 5.) having a black Cap or Case, which by its Motion represents the Phases of the Moon according to her Age. Without the Orbits of the Earth and Moon is Mars (N° 6.) The next in Order after Mars is Jupiter and his four Moons, (N° 7.) each of these Moons is supported by a crooked Wire, fixed in a Socket which turns about the Pillar that supports Jupiter: these Satellites may be turned by the Hand to any Position; and yet when the Machine is put in motion, they'll all move in their proper Times. The outermost of all is Saturn and his five Moons, (N° 8.) these Moons are supported and contrived after the same manner with those of Jupiter. The whole Machine is put into Motion by turning a small Winch, (like the Key of a Clock, N° 14); and the inside Work is so truly wrought, that notwithstanding the vast Number of Wheels that are to be turned, it does not require above the Strength of a fine Hair to put the whole in motion.

Above the Handle, there is a Cylindrical Pin, which may be drawn a little out, or pushed in at pleasure: When it is pushed in, all the Planets both Primary and Secondary will move according to their respective Periods, by turning the Handle: when it is drawn out, the Motions of the Satellites of Jupiter and Saturn will be stopped, while all the rest move without interruption. This is a very good Contrivance to preserve the Instrument from being clogged by the swift Motions of the wheels belonging to the Satellites of Jupiter and Saturn, when the Motions of the rest of the Planets are only considered. There is also a brass Lamp, having two convex Glasses, to be set in the room of the Sun; and also a smaller Earth and Moon, made somewhat in Proportion to their Distance from each other, which may be put on at pleasure.

The Lamp turns round in the same time with the Earth, and by means of the Glasses casts a strong Light upon her: and when the smaller Earth and Moon are placed on, it will be easy to shew when either of them may be eclipsed.

Having thus given a brief Description of the outward Parts of this Machine. I shall next give an Account of the Phenomena explained by it, when it is put into Motion.

*I. Of the Motions of the Planets in general.*

Having put on the Handle, push in the Pin which is just above it, and place a small black Patch (or bit of Wafer) upon the middle of the Sun (for Instance) right against the first Degree of  $\Upsilon$ ; we may also place Patches upon *Venus*, *Mars* and *Jupiter*, right against some noted Point in the Ecliptic. If we lay a Thread from the Sun to the first Degree of  $\Upsilon$ , we may set a Mark where it intersects the Orbit of each Planet; and that will be a help to note the Time of their Revolutions.

One entire Turn of the Handle answers to the Diurnal Motion of the Earth round her Axis; as may be seen by the Motion of the Hour-Index which is placed at the Foot of the Wire upon which the Terella is fixed. When the Index has moved the space of ten Hours, we may observe that *Jupiter* has made one Revolution complete round its Axis; the Handle being turned until the Hour-Index has passed over 23 Hours, will bring the Patch upon *Venus* to its former Situation with respect to the Ecliptic, which shews that  $\oplus$  has made one entire Revolution round her Axis. *Mars* makes one complete Revolution round his Axis in 24 Hours and about 40 Minutes. When the Handle is turned 27 times round, the Spot upon the Sun will point to the same Degree of the Ecliptic, as it did when the Instrument was first put into Motion. By observing the Motions of the Spots upon the Surface of the Sun, and of the Planets in the Heavens, their Diurnal Motion was discovered; after the same manner as we do here observe the Motions of their Representatives, by that of the Marks placed upon them.

If while we turn the Handle we observe the Planets, we will see them perform their Motions in the same relative Time as they really do in the Heavens; each making its Period in the Times mentioned in the Tables of their Periodic Revolutions 27 $\frac{1}{2}$  Turns of the Handle will bring the Moon round the Earth, which is called a *Periodic Month*. and all the while she keeps the same Face towards the Earth: for the Moon's Annual and Diurnal Motion are performed both in the same Time nearly, so that we always see the same Face or Side of the Moon.

If before the Instrument is put into Motion, the Satellites of *Jupiter* and *Saturn* be brought into the same right Line from their respective Primaries, we'll see them as we turn the Handle immediately dispers'd from one another, according to the different Celerities. Thus, one turn of the Handle will bring the first of *Jupiter's* Moon's about  $\frac{2}{3}$  parts round *Jupiter*; whi-

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The second has described but  $\frac{2}{3}$  parts; the third but about  $\frac{1}{2}$ ; and the fourth not quite  $\frac{1}{8}$  part; each of its respective Orbit. If we turn the Handle until the Hour-Index has moved  $18\frac{1}{4}$  hours more; the first Satellit will be then brought into its former Position, and so has made one entire Revolution; the second at the same time will be almost diametrically opposite to the first; and so has made a little more than Half of one evolution: the others will be in different Aspects, according to the Length of their Periods, as will be plainly exhibited by the Instrument. The same Observations may be made with respect to the Satellites of *Saturn*.

The Machine is so contrived, that the Handle may be turned either way; and if before we put it into motion, we observe the Aspects (or Situation with respect to each other) of the Planets, and then turn the Handle round any Number of times; the same number of Revolutions being made backwards, will bring all the Planets to their former Situations. I shall next proceed to Particulars.

### *Of the Stations and Retrogradations of the Planets.*

The Primary Planets, as they all turn round the Sun, at different Distances and in different Times, appear to us from the Earth to have different Motions; as sometimes they appear to move from *West* to *East* according to the Order of the Signs, which is called their *direct* Motion; then by degrees they slacken their pace, until at last they lose all their Motion and become *Stationary*, or not to move at all; that is, they appear in the same place with respect to the *fixed Stars* for some time together: After which they again begin to move, but with a contrary Direction, as from *East* to *West*; which is called their *retrograde* Motion: when again they become *Stationary*, and afterwards assume their *direct* Motion. The Reason of all these Appearances is very evidently shewn by the *Orrery*.

*Stationary.*  
*Retrograde*  
*Motion of*  
*the Planets.*

### I. *Of the Stations, &c. of the inferior Planets.*

We shall instance in the Planet *Mercury*, because his Motion round the Sun differs more from the Earth's than that of *Venus* does.

When *Mercury* is in his superior Conjunction (or when he is in a direct Line from the Earth beyond the Sun) fasten a String about the Axis of the Earth, and extend it over *Mercury* to the Ecliptic;

Ecliptic; then turning the Handle, keep the Thread all the while extended over ♀, and we'll find it move with a direct Motion in the Ecliptic, but continually slower, until *Mercury* has the greatest Elongation from the Earth. Near this Position, the Thread for some time will lay over *Mercury* without being moved in the Ecliptic, tho' the Earth and *Mercury* both continue their progressive Motion in their respective Orbits. When *Mercury* has got a little past this Place, we'll find the Thread must be moved backward in the Ecliptic, beginning first with a slow Motion, and then faster by degrees, until *Mercury* is in his inferior Conjunction, or directly betwixt the Earth and the Sun. Near this Position of ♀, his retrograde Motion will be the swiftest; but he still moves the same way, tho' continually slower, till he has again come to his greatest Elongation, where he will appear the second time to be Stationary, after which, he begins to move forward, and that faster by degrees, until he is come to the same Position, with respect to the Earth, that he was in at first. The same Observations may be made relating to the Motions of *Venus*. In like manner the different Motions observed in the superior Planets, may be also explained by the Orrery. If we extend the Thread over *Jupiter* and proceed after the same manner as before we did in regard to *Mercury*; we'll find that from the time *Jupiter* is in Conjunction with the Sun, his Motion is direct, but continually slower, until the Earth is nearly in a Quadrat Aspect with *Jupiter*, near which Position *Jupiter* seems to be Stationary: after which he begins to move, and so continually mends his Pace until he comes in Opposition to the Sun, at which time his retrograde Motion is swiftest. He still seems to go backward, but with slower Pace, till the Earth and he are again in a Quadrat Aspect, where *Jupiter* seems to have lost all his Motion; after which he again resumes his direct Motion and so proceeds faster by degrees, till the Earth and he are again in Opposition to each other.

These different Motions observed in the Planets, *Plate 5. Fig 1.* are easily illustrated, as followeth: The lesser Circle round the Sun is the Orbit of *Mercury*, in which he performs his Revolution round the Sun in about three Months, or while the Earth is going through  $\frac{1}{2}$  part of her Orbit or from A to N. The Numbers 1, 2, 3 &c. in the Orbit of *Mercury* shew the Spaces he describes in a Week nearly; and the Distances AB, BC, CD, &c. in the Earth's Orbit do likewise shew her Motion in the same Time. The Letters A, B, C, &c. in the great Orb, are the Motions of *Mercury* in the Heavens, as they appear from the Earth. Now if the Earth be supposed in A, and *Mercury* in 12, near his superior Conjunction with the Sun,

the Sun, a Spectator on the Earth will see ♀, as if he were in the Point of the Heavens A; and while ♀ is moving from 12 to 1, and from 1 to 2, &c. the Earth in the same time also moves from A to B, and from B to C, &c. All which time ♀ appears in the Heavens to move in a direct Motion from A to B, and from B to C, &c. but gradually slower until he arrives near the Point G, near which place he appears Stationary, or to stand still: and afterwards (tho' he still continues to move uniformly in his own Orbit with a progressive Motion) yet in the sphere of the fixed Stars he'll appear to be retrograde, or to go backwards, as from G to H, from H to I, &c. until he has arrived near the Point L, where again he'll appear to be Stationary, and afterwards to move in a direct Motion from L to M, and from M to N, &c.

What has been here shewn concerning the Motions of *Mercury*, is also to be understood of the Motions of *Venus*; but the Conjunctions of *Venus* with the Sun, do not happen so often as in *Mercury*: for *Venus* moving in a larger Orbit, and much lower than *Mercury*, does not so often overtake the Earth. But the Retrogradations are much greater in *Venus* than they are in *Mercury*, for the same Reasons.

The innermost Circle represents the Earth's Orbit, Fig. 2.  
divided into 12 Parts, answering to her Monthly Motion: the greatest Circle is the Orbit of *Jupiter*, which he describes in about 12 Years; and therefore the  $\frac{1}{12}$  thereof, from A to N, defines his Motion in one of our Years nearly; and the intermediate Divisions, A, B, C, &c. his monthly Motion. Let us suppose the Earth to be in the Point of her Orbit 12, and *Jupiter* in A, in his Conjunction with the Sun: It is evident that from the Earth, *Jupiter* will be seen in the Great Orb, or in the Point of the Heavens A; and while the Earth is moving from 12 to 1, 2, &c. ♀ also moves from A to B C &c. all which Time he appears in the Heavens to move with a direct Motion from A to B, C, &c. until he comes in Opposition to the Earth near the Point of the Heavens E, where he appears to be Stationary: After which, ♀ again begins to move (tho' at first with a slow Pace) from E thro' F, H, I. to K; where again he appears to stand still; but afterwards he resumes his direct Motion from I thro' K, to M, &c.

From the Construction of the preceding Figure, it appears that when the Superior Planets are in Conjunction with the Sun, their direct Motion is much quicker than at other times; and that because they really move from *West* to *East*, while the Earth in the opposite Part of the Heavens is carried the same Way, and round the same Center. This Motion afterwards continually slackens until the Planet comes almost in Opposition

tion to the Sun, when the Line joining the Earth and the Planet will continue for some time nearly parallel to it self, and the Planet seems from the Earth to stand still; after which it begins to move with a slow Motion backward, until it comes into a Quattuor Aspect with the Sun, when again it will seem to be Stationary for the above Reasons. After that, it resumes its direct Motion until it comes into a Conjunction with the Sun, then it will proceed as above explained. Now it also appears that the Retrogradations of the superior Planets are much slower than their direct Motions, and their consonance much shorter; for the Planet, from its last Quadrature till it comes in Opposition to the Sun, appears to move the same way with the Earth, by whom it is then overtaken; at which it begins to go backwards, but with a slow Motion, because the Earth being in the same part of the Heavens, and moving the same way, that the Planet really does, the apparent Motion of the Planet backwards must thereby be lessened.

What has been here said concerning the Motions of Jupiter is also to be understood of Mars and Saturn. But the Retrogradations of *Saturn* do oftner happen than those of *Jupiter*, because the Earth oftner overtakes *Saturn*; and for the same Reason, the Regressions of *Jupiter* do oftner happen than those of *Mars*. But the Retrogradations of *Mars* are much greater than those of *Jupiter*; whose are also much greater than those of *Saturn*.

In either of the Satellites of *Jupiter* or *Saturn*, these different Appearances in the neighbouring Worlds, are much oftner than we do in the Primary Planets.

We never observe these different Motions in the Moon, because she turns round the Earth as her Center; neither do we observe them in the Sun, because he is the Center of the Earth's Motion, whence the apparent Motion of the Sun always appears the same way round the Earth.

### *Of the Annual and Diurnal Motion of the Earth, and of the Increase and Decrease of Days and Nights.*

The Earth in her Annual Motion round the Sun, has her Axis always in the same Direction, or parallel to it self; that is, if a Line be drawn parallel to the Axis while the Earth is in any point of her Orbit, the Axis in all other Positions of the Earth, will be parallel to the said Line. This Parallelism of the Axis, and the simple Motion of the Earth in the Eccentric, solves all the Phænomena of different Seasons. These things are very well illustrated by the Orrery.

Plate V.

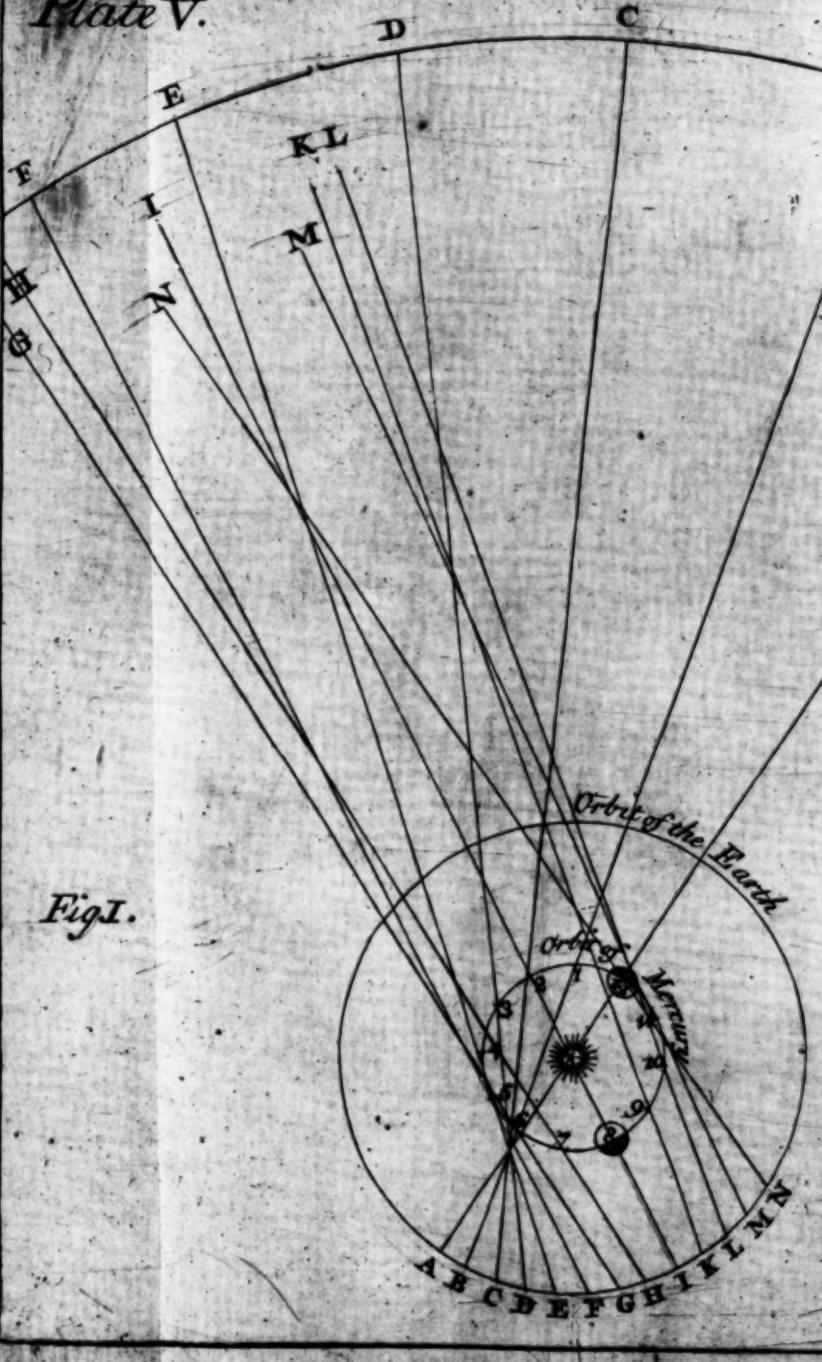


Fig I.

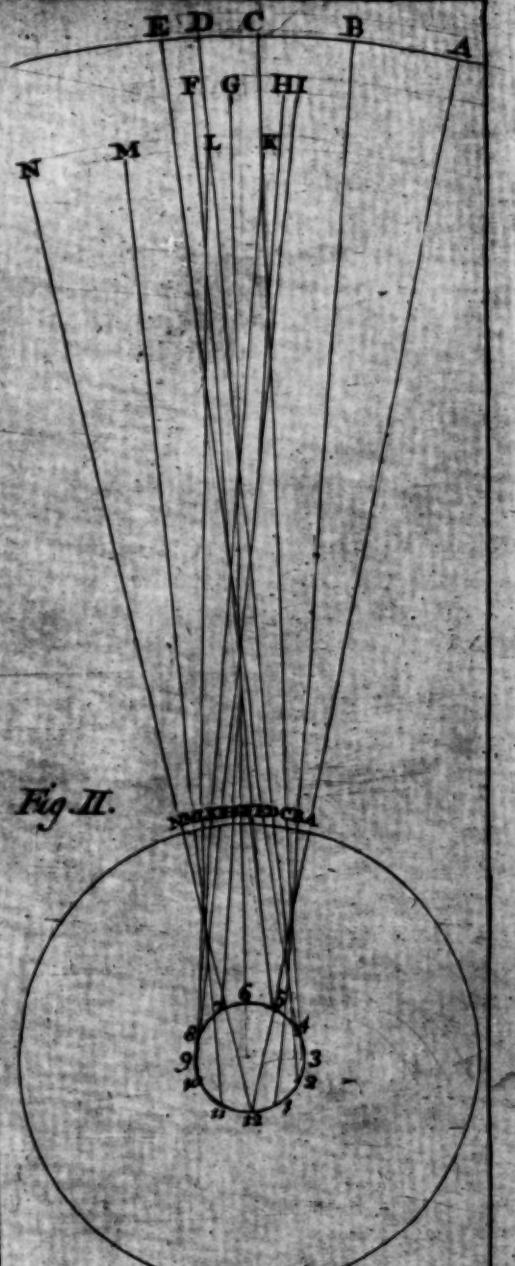


Fig. II.

J. Smith.

we put on the Lamp in the place of the Sun, we will see one half of our Globe is always illuminated by the Sun, the other Hemisphere remains in Darkness; how Day and Night are formed by the Revolution of the Earth round her, so as she turns from *West* to *East*, the Sun appears to move from *East* to *West*. And while the Earth turns in her Orbit, we may observe that her Axis always points the same way, and the several Seasons of the Year continually change. To make these things plainer, we will take a View of the Earth in different parts of her Orbit.

When the Earth is in the first Point of *Libra* (which is found by suspending a Thread from the Sun, and over the Earth to the horizon) we have the *Vernal Equinox*, and the Sun at that Time is in the first Point of *Aries*. In this Position of the Earth, the two Poles of the World are in the Line separating Light and Darkness; and as the Earth turns round her Axis, just one half of the Equator, and all its Parallels, will be in the Light, and the other Half in the Dark; and therefore the Days and Nights must be every where equal.

As the Earth moves along in her Orbit, we'll perceive the North Pole advances by degrees into the illuminated Hemisphere, and at the same Time, the South Pole recedes into Darkness; and in all Places to the Northward of the Equator, the Days continually lengthen, while the contrary happens in the Southern Parts; until at length the Earth is arrived in *Capricorn*. In this Position of the Earth, all the Space included within the Arctic Circle falls wholly within the Light; and all the opposite Part lying within the Antarctic Circle, is quite involved in Darkness. In all Places between the Equator and the Arctic Circle, the Days are now at the longest, and are continually longer as the Places are more remote from the Equator; in the Southern Hemisphere there is the contrary Effect. While the Earth is travelling from *Capricorn* towards *Aries*, the North Pole gradually recedes from the Light, and the South Pole approaches nearer to it: the Days in the Northern Hemisphere gradually decrease, and in the Southern Hemisphere increase in the same proportion, until the Earth being arrived in *Aries*, then the two Poles of the World lie exactly in the Line separating Light and Darkness, and the Days are equal to Nights in all Places of the World. As the Earth advances towards *Cancer*, the North Pole gradually recedes from the Light, and the Southern one advances into it, at the same rate; in the Northern Hemisphere the Days decrease, and in the Southern they gradually lengthen, until the Earth being arrived in *Cancer*, the North Frigid Zone is all involved in Darkness, and the South Frigid Zone falls entirely within the Light; the Days

every where in the Northern Hemisphere are now at the sh  
est, and to the Southward they are at the longest. As the Earth  
moves from hence towards *Libra*, the North Pole gradually ap  
proaches the Light, and the other recedes from it; and in  
Places to the Northward of the Equator, the Days now lengthen,  
while in the opposite Hemisphere they gradually shorten, un  
til the Earth has got into  $\text{Aries}$ ; in which Position, the Days and  
Nights will again be of equal Length in all Parts of the  
World.

We might have observed, that in all Positions of the Earth, one half of the Equator was in the Light, and the other in Darkness; whence under the Equator, the Days and Nights are always of the same Length: And all the while the Earth was going from  $\text{Aries}$  towards  $\text{Venus}$ , the North Pole was constantly illuminated, and the South Pole all the while in Darkness; so that for the other Half Year the contrary. Sometimes there is a Semicircle exactly facing the Sun, fixed over the Middle of the Earth, which may be called the Horizon of the Disk: This we do instead of the Lamp, if that Half of the Earth which is next the Sun be consider'd as being the illuminated Hemisphere, and the other Half, to be that which lies in Darkness.

*Plate 6.* The Great Circle  $\text{V}$ ,  $\text{S}$ ,  $\text{II}$ , &c. represents

Earth's annual Orbit; and the four lesser Circles E S Q C, the Ecliptic upon the Surface of the Earth, coinciding with the great Ecliptic in the Heavens. These four Figures represent the Earth in the four Cardinal Points of the Ecliptic; P being the North Pole of the Equator, and P' the North Pole of the Ecliptic; S P' C the Solstitial Colure, which is always parallel to the great Solstitial Colure  $\odot \text{VS}$  in the Heavens; E P' Q the Equinoctial Colure. The other Circles passing thro' P, are Meridians at two Hours distance from another; the Semicircle E A E Q is in the Northern Half of the Equator; the parallel Circle touching the Ecliptic in S, is the Tropic of Cancer; the dotted Circle the Parallel of London; the small Circle, touching the Pole of the Ecliptic, is the Arctic Circle. The shaded Part, which is always opposite to the Sun, is the obscure Hemisphere, or that which lies in Darkness; and that which is next the Sun, is the illuminated Hemisphere.

If we suppose the Earth in  $\text{Aries}$ , she'll then see the Sun in  $\text{Pisces}$  (which makes our Vernal Equinox) and in this Position, the Circle, bounding Light and Darkness, which here is S C, passes thro' the Poles of the World, and bisects all the Parallels of the Equator; and therefore the Diurnal and Nocturnal Arces, or the Lengths of the Days and Nights are equal in all Places of the World.

but while the Earth, in her annual Course, moves thro'  $\textcircled{z}$  to  $\textcircled{y}$ ; the Line SC, keeping still parallel to it self, or the Place where it was at first; the Pole P, will by this Motion gradually advance into the illuminated Hemisphere; and so the Diurnal Arches of the Parallels gradually increase, and consequently the Nocturnal ones decrease in the same proportion, until the Earth has arrived into  $\textcircled{y}$ : in which Position the Pole P, and all the Space within the Arctic Circle, fall wholly within the illuminated Hemisphere; and the Diurnal Arches of all the Parallels that are without this Circle, will exceed the Nocturnal Arches more or less, as the Places are nearer to, or farther off from it; until the Distance from the Pole is as far as the Equator, where both these Arches are always equal.

Again, while the Earth is moving from  $\textcircled{y}$ , through  $\textcircled{x}$ ,  $\textcircled{v}$ ,  $\textcircled{w}$ ; the Pole P begins to incline to the Line, distinguishing Light and Darkness, in the same proportion that before it rec'd from  $\textcircled{z}$ ; and consequently the Diurnal Arches gradually shorten, until the Earth has arrived into  $\textcircled{v}$ ; where the Pole P will again fall in the Horizon, and so cause the Days and Nights to be every where equal. But when the Earth has past  $\textcircled{v}$ , while she is going thro',  $\textcircled{s}$  and  $\textcircled{u}$  &c. the Pole P will begin to fall in the obscure Hemisphere, and so recede gradually from the Light, until the Earth is arrived in  $\textcircled{u}$ ; in which Position, not only the Pole, but all the Space within the Arctic Circle, are involved in Darkness; and the Diurnal Arches of all the Parallels, without the Arctic Circle, are equal to the Nocturnal Arches of the same Parallels, when the Earth is in the opposite Point  $\textcircled{w}$ ; and it is evident, that the Days are now at the shortest, and the Nights the longest. But when the Earth has past this Point, while she is going through  $\textcircled{s}$ ,  $\textcircled{u}$ , the Pole P will again gradually approach the Light, and so the diurnal Arches of the Parallels gradually lengthen, until the Earth is arrived in  $\textcircled{z}$ ; at which Time the Days and Nights will be equal in all Places of the World, and the Pole it self see the Sun.

Here we only considered the Phænomena belonging to the Northern Parallels; but if the Pole P be made the South Pole, then all the Parallels of Latitude will be Parallels of South Latitude; and the Days every where, in any Position of the Earth, will be equal to the Nights of those who lived in the opposite Hemisphere, under the same Parallels.

*Of the Phases of the Moon, and of her Motion in her Orbit.*

The Orbit of the Moon makes an Angle with the Plane of the Ecliptic, of above  $5\frac{1}{2}$  Degrees, and cuts it into two Points diametrically opposite, (after the same manner as the Equator and the Ecliptic cut each other upon the Globe)

*Nodes.*

*Line of the  
Nodes.*

*Dragon's Head.*

*Dragon's Tail.*

*Retrograde  
Motion of the  
Nodes.*

$\vee$  and  $\wedge$ ) which Points are called the *Nodes*; a right Line joining these Points, and passing through the Center of the Earth, is called the *Line of the Nodes*. That Node where the Moon begins to ascend Northward above the Plane of the Ecliptic, is called the *Ascending Node*, and the *Head of the Dragon*, and is thus commonly marked  $\vee$ . The other Node, from whence the Moon descends to the Southward of the Ecliptic, is called the *Descending Node*, and the *Dragon's Tail*, and is marked  $\wedge$ . The Line of the Nodes continually shifts it self from *East* to *West*, contrary to the Order of the Signs; and with this *Retrograde Motion* makes one Revolution round the Earth, in the Space of about 19 Years.

The Moon describes its Orbit round the Earth in the Space of 27 Days, and 7 Hours, which Space of Time is called a *Periodical Month*; yet from one Conjunction to the next, the Moon spends 29 Days and a Half, which is called a *Synodical Month*; because while the Moon in its proper Orbit finishes its Course, the Earth advances near a whole Sign in the Ecliptic, which Space the Moon has still to describe before she will be seen in Conjunction with the Sun.

When the Moon is in Conjunction with the Sun, note her Place in the Ecliptic; then turning the Handle, we'll find that 27 Days and 7 Hours will bring the Moon to the same Place, and after we have made  $2\frac{1}{4}$  Revolutions more, the Moon will be exactly betwixt the Sun and the Earth.

The Moon all the while keeps in her Orbit, and so the Way that supports her continually rises or falls in a Socket as she changes her Latitude; the black Cap shifts it self, and so shews the Phases of the Moon, according to her Age, or how much of her enlighten'd Part is seen from the Earth. In one Synodical Month, the Line of the Nodes moves about  $1\frac{1}{2}$  Degree from *West* to *East*, and so makes one entire Revolution in 19 Years.

in b

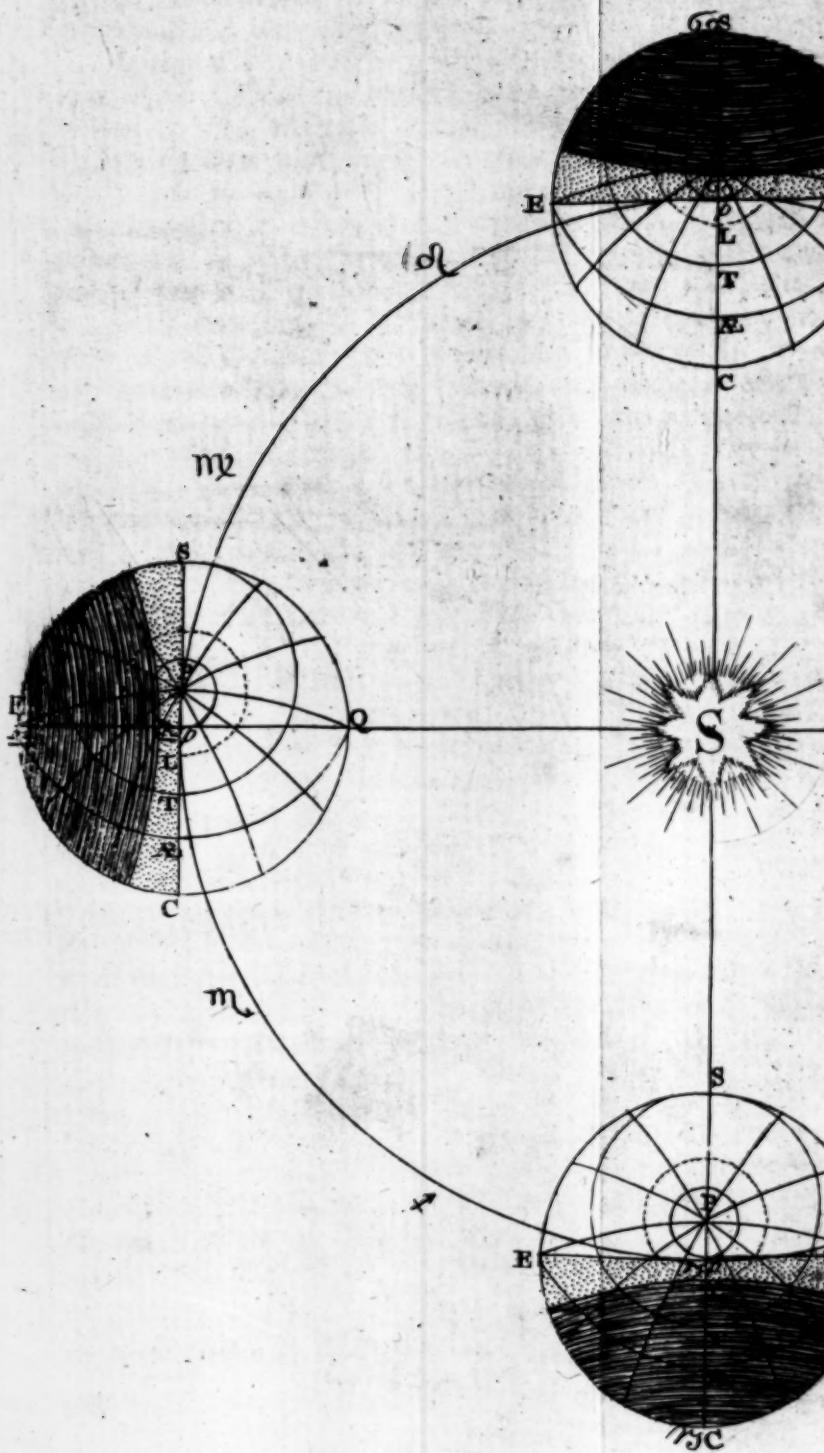
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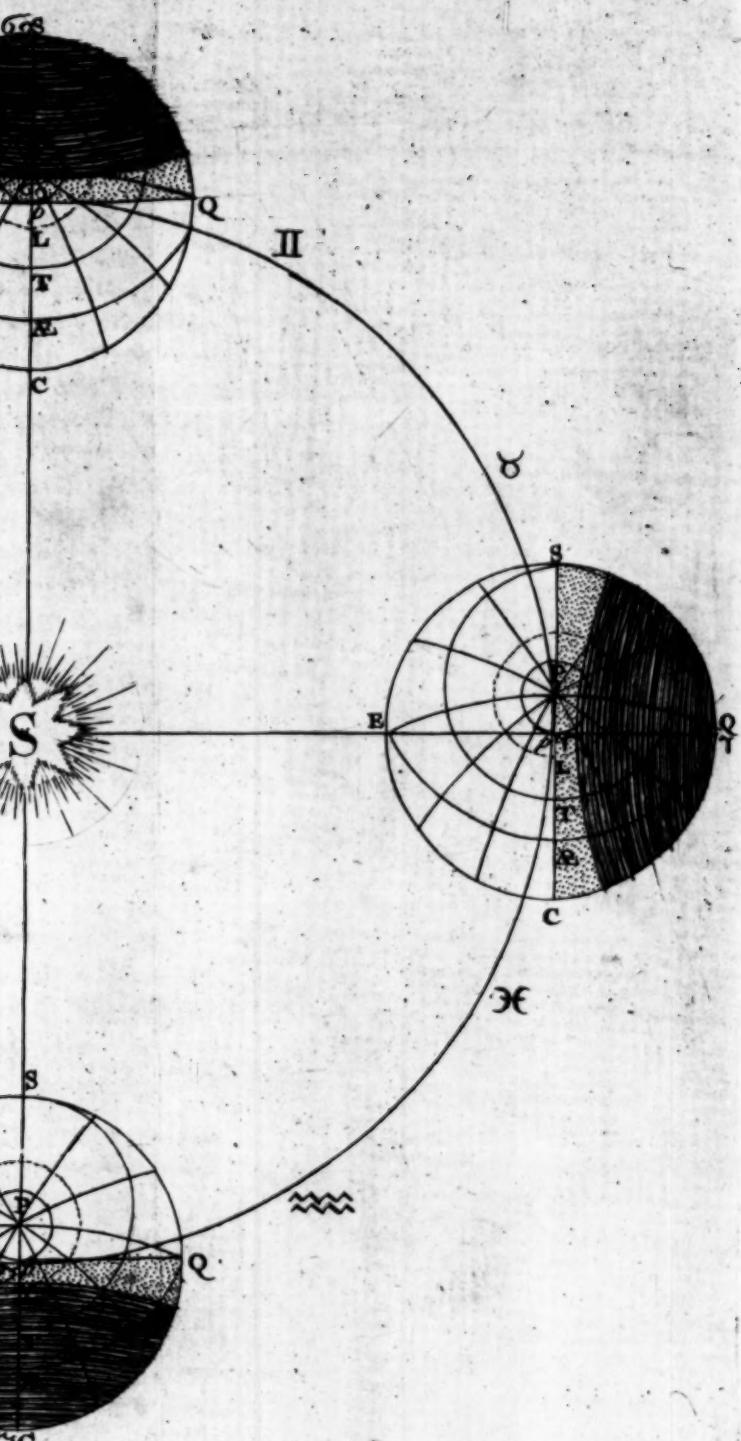
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Plate VI.



*fronting Page 132.*



*J. Gravim Sc.*

A B be an Arch of the Earth's Orbit, and *Plate 7. Fig. 1.* the Earth is in T, let the Moon be in N, in Conjunction with the Sun in S; while the Moon is describing Orbit N A F D, the Earth will describe the Arch of her Orbit T z; and when the Earth has got into the Point z, the Moon will be in the Point of her Orbit n, having made one complete Revolution round the Earth. But the Moon, before she comes in Conjunction with the Sun, must again describe the Arch n o; which Arch is similar to T z, because the Lines of n, are parallel; and because, while the Moon describes the Arch n o, the Earth advances forward in the Ecliptic; the Arch described by the Moon, after she has finished her period of a Month, before she makes a Synodical Month, must be somewhat greater than n o. To determine the mean Length of a Synodical Month; find the Diurnal Motion of the Moon, (or Space she describes round the Earth in one Day) and likewise the Diurnal Motion of the Earth; then the Difference between these two Motions, is the apparent Motion of the Moon over the Earth in one Day; then it will be, As this differential Motion is to a whole Circle; so is one Day, to that Space of Time in which the Moon appears to describe a complete Circle round the Earth; which is about 29½ Days: But this is not always a uniform Motion; for the Motion of the Moon is sometimes faster, sometimes slower, according to the Position of the Earth in her Orbit.

In one Synodical Month, the Moon has all manner of Aspects with the Sun and Earth; and because she is opaque, that Part of hers will only appear bright which is towards the Sun, the opposite remains in Darkness. But the Inhabitants of the Earth can only see that Face of the Moon, which is turned towards the Earth; and therefore, according to the various Aspects of the Moon, in respect of the Sun and Earth, we see different Portions of her illuminated Face, and so a continual Change in her \* Phases.

S be the Sun, R T V an Arch of the Earth's Orbit *Plate 7. Fig. 2.* T the Earth, and the Circle A B C D, &c. the Earth's Orbit, in which she turns round the Earth, in the Space of a Month; and let A, B, C, &c. be the Centers of the Moon's different Parts of her Orbit.

Now if with the Lines S A, S B, &c. we joyn the Centers of the Sun and Moon, and at right Angles to these, draw the Lines H O; the said Lines H O. will be the Circles that separate

the different Appearances we observe in her, according to her Position in respect of the Sun and Earth.

the

the illuminated Part of the Moon, from the dark and obscure. Again, if we conceive another Line I L, to be drawn at right Angles to the Lines T A, T B, &c. passing from the Center of the Earth to the Moon, the said Line I L will divide the visible Hemisphere of the Moon, or that which is turned toward us, from the invisible, or that which is turned from us; and this Circle may be called the *Circle of Vision*.

*Full Moon.* Now it is manifest, that whenever the Moon is in the Position A, or in that Point of her Orbit which is opposite to the Sun, the Circle of Vision, and the Circle bounding Light and Darkness do coincide, and all the illuminated Face of the Moon is turned towards the Earth, and is visible to us; and in this Position the Moon is said to be full. But when the Moon arrives to B, all her illuminated Face is then not towards the Earth, there being a Part of it, H B, not to be seen by us; and then her visible Face is deficient from a Circle, and appears of a gibbous Form, as in B, Fig. 3. Again, when she arrives to C, the two forementioned Circles cut each other at right Angles, and then we observe a

*Half Moon.* serve a Half Moon, as in C, Fig. 3. And again, the illuminated Face of the Moon is more and more turned from the Earth, until she comes to the Point E where the Circle of Vision, and that bounding Light and Darkness do again coincide. Here the Moon disappears, the illuminated Part being wholly turned from the Earth; and she is now said to be in *Conjunction* with the Sun, because she is in the same Direction from the Earth, that the Sun is in, which

*New Moon.* Position we call a *New Moon*. When the Moon has arrived to F, she again resumes a horned Figure; but her Horns (which before the Change were turned Westward) have now changed their Position, and look Eastward. When she has arrived to a Quadrat Aspect at G, she'll appear bisected like a Half-Moon; afterwards she'll still grow bigger, until last she comes to A, where again she'll appear in her full Splendor.

The same Appearances which we observe in the Moon, are likewise observed by the *Lunarians* in the Earth; our Earth being a Moon to them as their Moon is to us; and we are observed by them, to be carried round in the same space of Time, that they are really carried round the Earth. But the same Phases of the Earth and Moon happen when they are in a contrary Position; for when the Moon is in *Conjunction* to the Earth is then in *Opposition* to the Moon, and the *Lunarians* have then a full Earth, as we in a similar Position have a full Moon. When the Moon comes in *Opposition* to the Sun, the Earth seen from the Moon, will appear in *Conjunction*.

ith her, and in that Position the Earth will disappear; af-  
wards she'll assume a horned Figure, and so shew the same  
as to the Inhabitants of the Moon, as she does to us.

### *Of the Eclipses of the Sun and Moon.*

An *Eclipse* is that Deprivation of Light in a Pla-  
et, when another is interposed betwixt it and the  
Sun. Thus, an Eclipse of the Sun is made by the Interpositi-  
on of the Moon at her Conjunction; and an Eclipse of the  
Sun is occasioned by the Shadow of the Earth falling upon the  
Sun, when she is in Opposition to the Sun.

Let S be the Sun, T the Earth, and A B C its Sha-  
dow; now if the Moon, when she is in Opposition  
to the Sun, should come into the conical Space A B C,  
she'll then be deprived of the Solar Light, and so  
undergo an Eclipse.

*Eclipse.**Fig. 4.**Lunar  
Eclipse.*

In the same manner when the Shadow of the Moon falls up-  
on the Earth (which can never happen but when the Moon is  
Conjunction with the Sun) that part upon which the Sha-  
dow falls, will be involved in Darkness, and the Sun  
eclipsed. But because the Moon is much less than  
the Earth, the Shadow of the D cannot cover the  
whole Earth, but only a part of it. Let S be the  
Sun, T the Earth, A B C the Moon's Orbit, and L

*Solar  
Eclipse.**Fig. 5.*

the Moon in Conjunction with the Sun: Here the Shadow of  
the Moon falls only upon the part D E of the Earth's Surface,  
and there only the Sun is entirely hid; but there are other  
parts E F, D G, on each side of the Shadow, where the Inha-  
bitants are deprived of part of the Solar Rays, and that more  
or less according to their Distance from the Shadow. Those  
that live at H and I, will see Half of the Sun Eclipsed: but  
in the Spaces F M, G N, all the Sun's Body will be visible without  
any Eclipse. From the preceding Figure, it appears, that  
an Eclipse of the Sun does not reach a great way upon the Su-  
rfaces of the Earth: but the whole Body of the Moon may  
sometimes be involved in the Earth's Shadow.

The D also being an opaque Body, and enlightened by the ☽  
consequently casts a Shadow towards those parts that are turn-  
ed from the ☽, and if the Earth should be deprived of the ☽'s  
light, by being immers'd in the shadow of D this Phænomena  
ought to be call'd an Eclipse of the Earth; but the Observer of  
being on the Earth, and the D (which more or less covers  
the ☽) not being easily perceiv'd by us: the Defect of Light ap-  
pears to us as in the ☽ it self, and is therefore call'd an Eclipse  
of

of  $\odot$ , which is distinguish'd into a Total Eclipse, wherein  $\Delta$  covers the whole body of the  $\odot$  from us, or a partial Eclipse wherein the  $\Delta$  covers only a part of the  $\odot$ .

But it is to be observed, that altho' an Eclipse  $\odot$  be in reality an Eclipse of the Earth, yet what is call'd a total Eclipse of the  $\odot$  is not to be conceiv'd in reality as a total Eclipse of the Earth, or that the whole upper and opposite Hemisphere of the Earth is then deprived of the Sun's Light, as in a total Eclipse of  $\Delta$  its whole opposite Hemisphere is darkned; (the reason of which difference is this) the Earth being bigger than the  $\Delta$ , the Cone of its Shadow is big enough to involve the whole opposite Hemisphere of  $\Delta$  in its darkness; whereas  $\Delta$ , being less than the Earth the Cone of her Shadow will involve at once only a small tract.

Although the Moon seen from the Earth, and the Earth seen from the Moon, are each alternately once a Month in Conjunction with the Sun; yet by Reason of the Inclination

the Moon's Orbit to the Ecliptic, the Sun is never Eclipsed every New Moon, nor the Moon at every Full. Let  $T$  be the Earth,  $DTE$  an Arch of the Ecliptic,  $ALBF$  the Moon's Orbit, having the Earth  $T$  in Center; and let  $AGBC$  be another Circle coinciding with the Ecliptic, and  $A, B$ , the Nodes, or the two Points where the Moon's Orbit, and the Ecliptic cut each other.  $A$  the ascending Node, and  $B$  the descending Node. The Angle  $GAL$  equal to  $GBL$  is the Inclination of the Moon's Orbit to the Ecliptic, being about  $5\frac{1}{2}$  Degrees. Now a Spectator from Earth at  $T$ , will observe the Sun to move in the Circle  $AGBC$ , and the Moon in her Orbit  $ALBF$ ; whence it is evident, that the Sun and Moon can never be seen in a direct Line from the Center of the Earth, but when the Moon is in one of the Nodes  $A$  or  $B$ ; and then only will the Sun appear centrally Eclipsed. But if the Conjunction of the Moon happens when she is any where within the Distance  $AB$  of the Nodes either North or South, the Sun will be then Eclipsed, more or less according to the Distance from the Node  $A$ , or  $B$ . The Conjunction happens when the Moon is in  $b$ , the Sun will be then one half Eclipsed; and if it happens when she is in  $a$ , the Moon's Limb will just touch the Sun's Disk, without covering any part of it.

If the *Lunar* Orbit coincided with the Ecliptic, every Month would exhibit two Eclipses one of the  $\odot$ , the other of  $\Delta$  the former at the New  $\Delta$  the other at the full  $\Delta$ ; so there would be no New  $\Delta$  nor full without an Eclipse; not only so, but these Eclipses would be both of them Total and Central. Nay the same Numbers which would have shewn

true Conjunctions, and Oppositions would have shew'd Eclipses also. But from considering the Annual Motion of the ☽ and the Angle which the Moon's Orbit makes with the Ecliptic 'tis manifeste cannot be an Eclipse at every Change or Full; because Earth and the Earth's Shadow always falls in the plane of Ecliptic; since both ☽ and Earth are always there, these effects or Eclipses only can happen when the true Conjunctions or Oppositions are found in or about the Nodes, that is, when the Conjunctions are within  $16^{\circ}.26'$  and the Oppositions within  $12^{\circ}.34'$  of either Node before or after.

The Shadow of the Earth at the Place where the Moon's Orbit intersects it, is three times as large as the Moon's Diameter, in Fig. 4. and therefore it often happens that Eclipses of Moon are Total; when they are not Central: and for the Reason the Moon may sometimes be totally eclipsed for three Hours together; whereas Total Eclipses of the Sun can scarcely ever exceed four Minutes.

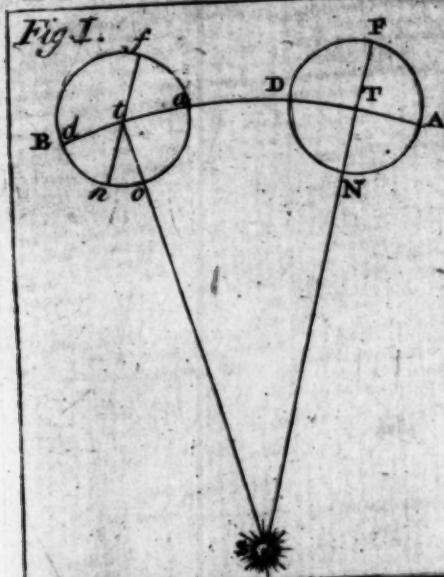
In Total and Central Eclipses of the ☽ the Duration is found to be so long, as to let the ☽ go the Length of three of its Diameters in the Shadow totally eclipsed; which stay in the Earth's Shadow is computed to be about four Hours whereof the ☽ takes one Hour from its beginning to enter the Shadow quite immersed therein; two Hours more she continues wholly Dark, and the fourth Hour is taken up from her first entering to come out of the Shadow, till she is quite out of it but the Eclipse of the ☽ lasts not so long, its seldom in one place exceeds  $2\frac{1}{2}$  Hours, and in total Darkness, never above 5 Minutes, scarce 1 or 3 such will happen in the Course of an Age; because the point of the ☽'s Shadow reaches a little beyond the Earth, and sometimes does not reach the Earth at all; also the apparent Diameter of the ☽ does very little exceed the apparent Diameter of the ☽, that is it be in central Eclipses, which are rare and unusual, the ☽ cannot wholly cover and hide the Body of ☽ from us.

The Eclipses of the Sun and Moon are very well explained by the *Orrery*: thus, Having put the Lamp in the Place of the ☽, and the little Earth and the little Moon in their proper Places, instead of the larger ones; let the Room wherein the Instrument stands be darkned; then turning the Handle about, you will see when the Conjunction of the Moon happens. When the ☽ is in or near one of the Nodes, her Shadow will fall upon the Earth, and so deprive that part upon which it falls of Light of the Sun: If the Conjunction happens when the ☽ is not near one of the Nodes, the Light of the Lamp will fall upon the Earth, either above or below the Moon, according

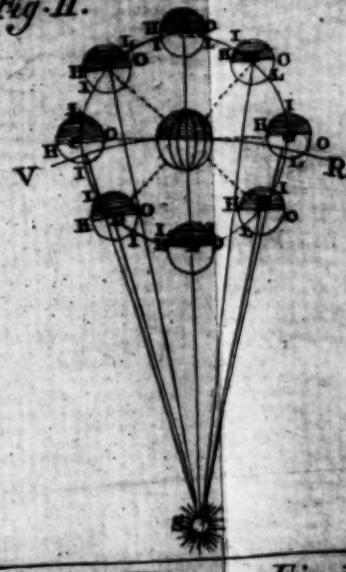
ing to her Latitude at that Time. In like manner, when full Moon happens near one of the Nodes, the Shadow of the Earth will fall upon the Moon; and if the Moon's Latitude be but small, her whole Face will be involved in Darkness. At other times, when the full Moon happens when she is near one of her Nodes, the Shadow of the Earth will pass either above or below the Moon, and so by that means the Moon will escape being eclipsed.



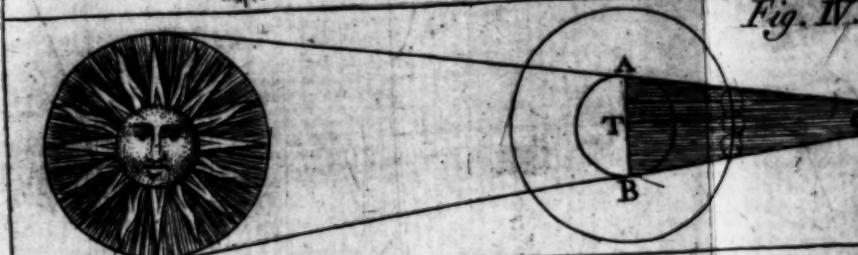
*Plate VII.*



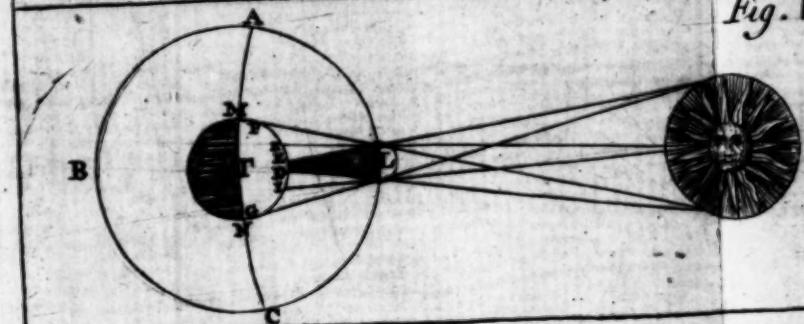
*Fig. II.*



*Fig. IV.*



*Fig. V.*



*Fig. VII.*

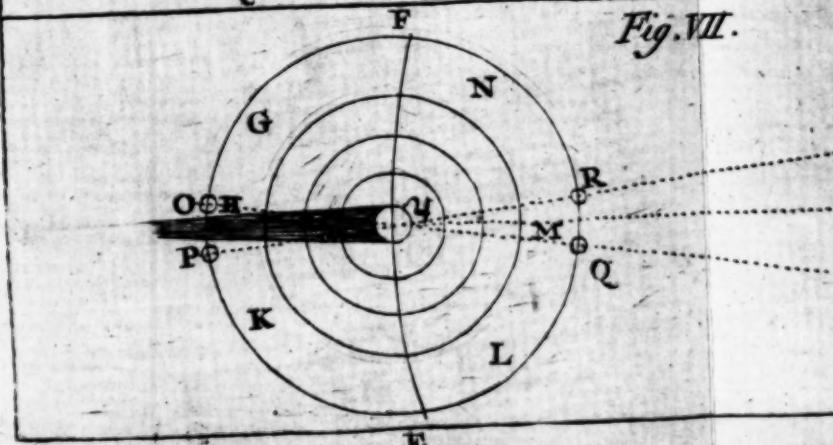


Fig. III.

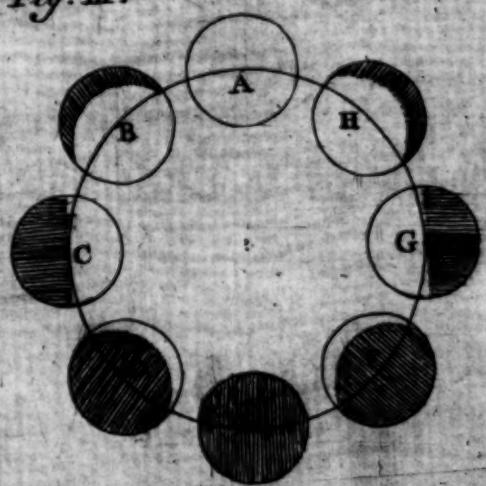
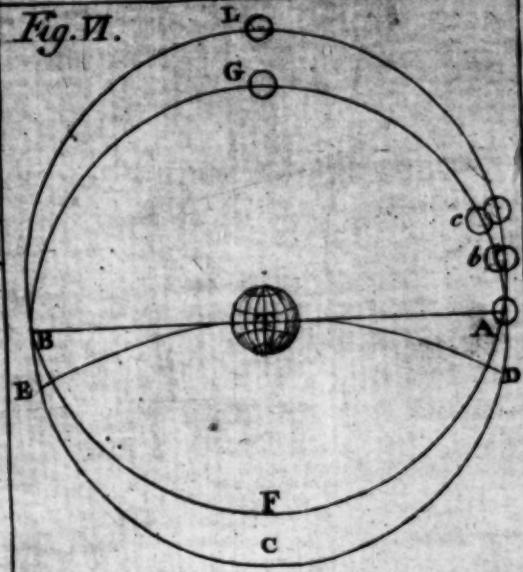
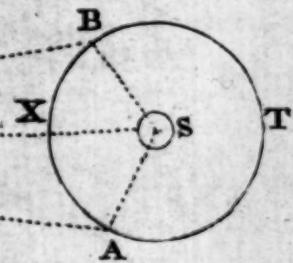


Fig. IV.

Fig. VI.



III.



Tirrini 1.

**T H E  
E S C R I P T I O N and U S E**

**O F  
E L E S C O P E S :**

**S E C T . I .**

THE Sight of Man is of it self confined to narrow Views, and tho' it takes in a great Part of the Creation at once, yet all is represented in Miniature and imperfectly. The naked Eye sees only so much of external Objects, as is sufficient to move the principal Passions, and give notice more immediately concerns the Safety and Happiness Animal. What is more than this, was left as a Subject for Curiosity, upon which we might exercise those Faculties which are bestowed by our bountiful Benefactor, for this end, of searching into the astonishing Mechanism of all Works, and from thence enlarging our Idea of his Great-Objects placed at a great Distance whether upon the Surface of the Earth, or in the Heavens are seen under so small a Angle, that their parts are not to be distinguished one from another; and by this means those distant charming Scenes were hid from us, which the Study of Catoptrics and Dioptrics have laid open to our View. This noble part of Knowledge teaches us how by a due Position of Glasses ground into Figures, we may enlarge the Diameter of the Heavenly and all such Objects, to which we are allow'd no nearer approach, in what Proportion we please, and view them as perfectly.

fectly and distinctly as if we could summon them before us, and command them to the End of our Telescope : This brought us into a perfect Acquaintance with these surprizing Parts of the Creation, which are far separate from this Globe of ours, and with which we are allow'd no Commerce, by Looking. We can now perceive the Sun to be a vast Globe of Fire, and by the different Phases of all the Planets, that he is the Fountain of all their Light. The Surfaces of most of them appear like so many Maps of Land and Water, and there are now but allow both them and the fixed Stars : some nobler than to twinkle upon us in the Night. By fixing upon some markable Spots upon their Surfaces, and observing how they shift their Position, and in what time they again return to the same Place, we determine the Motion of these Bodies round their Axis, and the time in which that Revolution is performed. Several Secondary Planets or Satellites, which were too small for the naked Eye, are now discern'd to move round Jupiter and Saturn as the Moon round our Earth ; and about the last of them seen the particular Phenomenon of an Annulus or Ring : Now is the Discovery of these Satellites, merely Speculative, but the prodigious Use and Advantage for their Eclipses have determined the Velocity of Light and are so frequent, as to be the most constant Appearance the Heavens afford us at present for the Solution of the Great, and Valuable Problem of the Longitude. The Distances, Magnitudes and Motions of all the Heavenly Bodies, and even the Irregularities of the Sun, have by this means been so nicely observ'd, and by the Power of Numbers, reduced within some few Tables for common and easy Use that the Places for any determinate instant of Time to come, are now to be predicted as easily, and almost as exactly as we could wish.

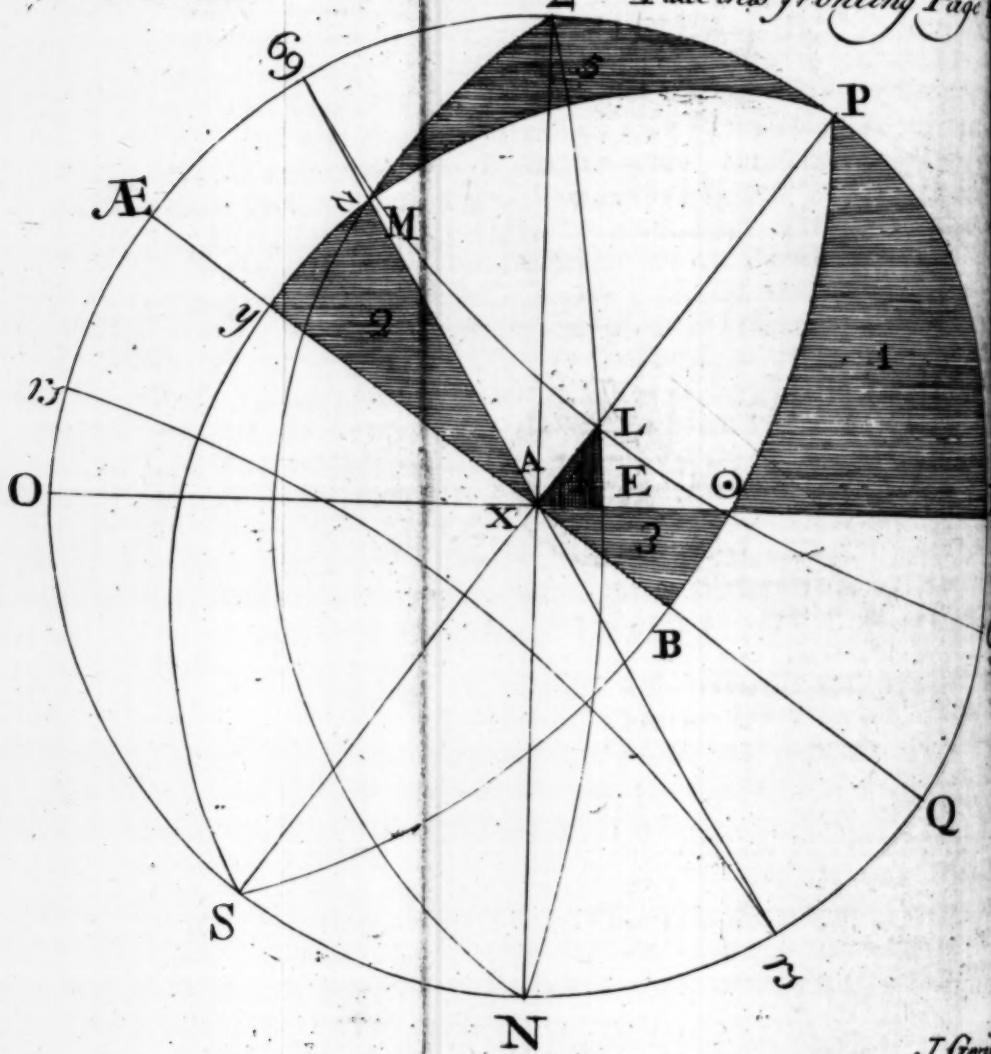
Galileus a Florentine, about 1615, first invented and applied his Telescope, to the Discovery of Celestial Objects; by which he beheld the 4 Moons or Satellites of Jovis, the different Phases of Venus, and the increase and decrease of the Sun, that the Sun's Disk was like our Earth rising with Mountains, and deprest into Valleys and Seas ; that the Sun had his Spots whereby he evinced its Rotation upon its own Axis, and that the Via Lactea was nothing but a multitude of small Stars all of the same sort or kind, as since his time both Astronomy and Geography have from the Glasses received many particular Advantages, and Discoveries unknown to the Antients.

For by the means of Telescopes, especially such as magnify the Diameters of Objects 100 or 200 times we will see the Sun in the same Manner Figure and Bigness, as it would appear in a Distance 100 or 200 times less than ours ; by the same we may



*Plate III.*

*Place this fronting Page*



scend yet higher, and approach the Planets, Comets, and fixed Stars, so near, that of such immense Distances, there remains only the hundredth, or two hundredth part to have the whole Journey finished, and from thence we can behold the Converſion of the Planets about their proper Axes. The Moons of  $\pi$  and  $\eta$  their Eclipses the Belts of  $\mu$  the wonderful Ring of  $\delta$ , and all the various Appearances and shapes it takes. This is the chief Instrument, by which we obſerve the Magnitude and apparent Motions of the Heavenly Bodies, and hence their proportional Distances are calculated.

Tis now reckon'd no absurd Notion to conceive the *fixed Stars*, as so many Suns; probably at as great Distances one from another, as they are from us and every one their System of inhabited Planets circling round them. And perhaps the Number of those we see may bear little or no Proportion to those others that may be dispersed thro' the vast Regions of the *Univerſe* at such Distances from our little *Ball*, that no Assistance can ever help us to a sight of them. A Notion that gives, surely the most just and noble Sentiments, that the Mind of Man can entertain of an Almighty Author. That the *Milky-Way* in the Heavens, which we behold in a clear Star-light Night, is nothing else, but a continued Cluster of such *fixed Stars* (as aforesaid,) is a truth of which we are assured by the Telescope; and to the same Help it is we owe all we know of these Heavenly bodies call'd *Comets*; their Distance, Magnitude and Motion round the *Sun*, in such *eccentrical Orbits*, as some of them come very near to right Lines. To what a surprizing heighth this *Cometical Astronomy* has been carried by the present Age, notwithstanding the Observations we have been able to make upon these Bodies are so few, and those made by our Predecessors so imperfect, may be seen in the Writings of those incomparable Astronomers, Sir *Isaac Newton*, Doctor *Gregory*, and Doctor *Halley*: That in every clear Morning and Evening, we see the *Sun* for some time before he rises, and after he sets is a *Paradox* only to be unriddled by Diphysics; and if we would know the true Place of any Heavenly Body, elevated not many degrees above the *Horizon*, the same Science tells us, that here, *Seeing is not Believing*, but that we must correct our *Eye-Sight* by a Table of *Refractions*. It is true, the *Ratio* of *Refraction* of the *Atmosphere* very near the *Horizon*: does not observe a constant Rule; because there happens a very great Variety in the Accumulations of Vapours about these Parts: But then this Variation depends pretty regularly upon the Position of the *Sun*, above or below the *Horizon*, and the different State of the Weather, and if in the Morning or Evening we see the lower parts of a distant Tower or Mountain, thro' a Telescope fixed in Position, we shall find the upper parts of the

the same Tower or Mountain in the same Place, if our Observations be made nearer Noon, and just at Noon, the same Object will be seen lowest of all, as the accurate Huyghens has observed; and this Difference is greater in cold, and moist than in hot and dry Weather, and tho' not in a Proportion always certain, yet constant enough for Physical Purposes. In short, without the Assistance of Telescopes, Astronomy could have comet nothing, and our Observations on the Heavens, had gone little further than foretelling a fine Morning from the setting of the Sun; or a Shower of Rain from the Course of the Clouds.

## *II. Of the Construction of the Astronomical Telescope.*

### S C O P E.

A Telescope is an Optic Instrument which serves to discover Objects at a Distance; the Invention of which is one of the noblest and most useful these Ages have to boast of: By Means hereof the Wonders of the Heavens are discover'd to us, and Astronomy brought to a Degree of Perfection, which former Ages could have no Idea of. The Optic Principles, whereon Telescopes are founded, are contain'd in Euclid, and it is for want of Attention thereto, that the World was so long without that admirable Invention; as no doubt there are great many others lying hid in the same Principles, only waiting for Reflection or Accident to bring them forth.

Telescopes are either Refracting or Reflecting. Refracting Telescopes are of several Kinds, and are distinguished by the Number and Form of their Lens's or Glasses, and denominated from the particular Uses, &c. Such are the Terrestrial or Land Telescope, and Cœlestial or Astronomical Telescope.

If a Telescope consists only of a Convex Object Lens, and an Eye-Glass of a much greater Convexity than the Object-Glass is, then will the apparent Magnitude of the Object seen through that Telescope, be to the Object seen by the naked Eye at the Station of the Object-Glass, as the Focal Length of the Object-Glass to the Focal Length of the Eye-Glass. Thus in Plate 8. Fig. 1. let A B represent the Object-Glass, and suppose its Focal Length H d 12 Foot or 144 Inches, and the Eye-Glass represented by c D, its Focal Length 3 Inches; then the apparent Diameter of the Object, seen through such a Telescope to that seen through the naked Eye, will be as 144 to 3, or as 48 to 1, wherefore such a Telescope will be said to magnify 48 times, and its Surface 2304 times (i. e. the Square of 48). Wherefore

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Wherefore if the same Object-Glass be combined with an Eye-Glass whose Focal Distance is 1, and at another time with an Eye-Glass whose Focal Distance is 2, the former Telescope will magnify twice as much as the latter. Also, if two Telescopes have different Lengths, and the Focus of the Eye-Glass of the shorter be in the same Proportion to the Focus of its Object-Glass, as the Focus of the Eye-Glass of the longer bears to its Object-Glass; then those two Telescopes will *magnify alike*. But long Telescopes are of very great Use, and it is impossible to make short ones perform as well: For,

1. Object-Glasses of a shorter Focus will not bear Eye-Glasses proportionably short without colouring the Object, or rendering it dark and obscure.

For Instance: Suppose a very good 12 Foot Object-Glass will receive an Eye-Glass of no shorter Focus than 3 Inches, with *sharpness* and *distinctness*, yet, however, an Object-Glass of 24 Foot Focus, equally good, will bear an Eye-Glass of less than 6 Inches Focus, (perhaps of 4 or 5 Inches Focus) with equal *clearness* and *distinctness*; and then, tho' an Object-Glass of 12 Foot, with an Eye-Glass of 3 Inches, will magnify but 48 times, as above proved, yet an Object-Glass of 24 Foot, with an Eye-Glass of 4 Inches, will magnify 72 times, which is above one third more than the former.

2. The Image of the Moon, or any other Object, in the distinct Base of an Object-Glass of 24 Foot, is twice as long as the Image of the distinct Base of an Object-Glass of 12 Foot; and consequently the Image in the former will be much more plain and distinct. Hence may be concluded also, that if the Object-Glass be formed on a less Sphere than an Eye-Glass, the appearance of Objects will be diminished in the aforesaid Proportion; as is plain by the Case, when a Telescope is inverted. But for a more particular Construction of the same Telescope, let A B as before (Plate 8. Fig. 1.) represent the Convex Glass next the Object C D, the other Glass more Convex near the Eye. Suppose the Object-Glass A B to form the Image of the Object at E F, so that if a Sheet of White Paper were to be held in this Place, the Object would appear. Now suppose the Rays, which pass the Glass A B, and are united about E F, to proceed to the Eye-Glass C D, and be there refracted: Three only of these Rays are drawn in the Figure; those which pass by the Extremities of the Glass A B, and that which passes its Middle. If the Glass C D be placed at such a Distance from the Image E F, that the Rays, which pass by the Point F, after having proceeded through the Glass diverge so much,

much, as the Rays do that come from the Object, which is such a Distance from the Eye as to be seen distinctly; these being received by the Eye, will make on the Bottom of the Eye a distinct Representation of the Point F. In like manner the Rays, which pass through the Object-Glass A B to the Point E, after proceeding through the Eye-Glass C D, will, on the Bottom of the Eye, make a distinct Representation of the Point E; but if the Eye be placed where these Rays, which proceed from F, cross those which proceed from E, the Eye will receive a distinct Impression of both these Points at the same time, and consequently will also receive a distinct Impression from the intermediate Parts of the Image E F; that is, the Eye will see the Object, to which the Telescope is directed, distinctly. The Place of the Eye is about the Point G, where the Rays H E, H F cross, which pass through the Middle of the Object-Glass A B to the Points E and F, or at the Place where the Focus would be formed by Rays coming from the Point H, refracted by the Glass C D. To judge how much the Instrument magnifies any Object, we must first observe, that the Angle under E H F, in which the Eye, at the Point H, would see the Image E F, is nearly the same as the Angle, under which the Object appears by direct Vision; but when the Eye is at G, and views the Object through the Telescope, it sees the same under a greater Angle; for, the Rays, which coming from E and F cross in G, make a greater Angle than the Rays which proceed from the Point H to these Points E and F. The Angle at G is greater than that at H in the Proportion, as the Distance between the Glasses A B and C D is greater than the Distance of the Point G from the Glass.

This Telescope inverts the Object; for the Rays, which come from the Right Hand Side of the Object, go to the Point E, the Left Side of the Image; and the Rays, which come from the Left Side of the Object, go to F, the Right Side of the Image. These Rays cross again in G, so that the Rays, which come from the Right Side of the Object, go to the Right Side of the Eye; and the Rays from the Left Side of the Object go to the Left Side of the Eye; therefore, in this Telescope, the Image in the Eye has the same Situation as the Object; and seeing that in direct Vision the Image in the Eye has an inverted Situation, here, where the Situation is not inverted, the Object must appear so. This is no Inconvenience to Astronomers in Celestial Observations, but for Objects here on the Earth it is usual to add two other Convex-Glasses, which may turn the Object again, as is represented in Plate 8. Fig. 2. or else to use the other kind of Telescope, with a concave Eye-Glass.

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## II. Of the Construction of a Land or Day TELESCOPE.

A Land or Day Telescope consists of more than two Lens's, commonly of a Convex Object Glass, and three Convex Eye-Glasses, by which it exhibits Objects erect: The Construction of it, thus.

Having provided a Tube, fit in an Object-Glass, which is either Convex on both Sides, or Plano-Convex, and a Segment of a large Sphere: To this add three Eye-Glasses, all Convex on both Sides, and Segments of equal Spheres, disposing them in such manner as that the Distance of any Two may be the Sum of the Distances of their Foci: Then will an Eye, applied to the least Lens, at the Distance of its Focus, see Objects very distinctly erect and magnified in the Ratio of the Distance of the Focus of one Eye-Glass, Plate 8. Fig. 1. to the Distance of the Focus of the Object-Glass.

For 1. The Rays falling upon the Object-Glass parallel, the image of the Object will be represented inverted at the Distance of the principal Focus; wherefore, since this Image is in the focus of the first Eye-Glass, the Rays, after a second Refraction, will become parallel, and thus falling on the third Lens, after a third Refraction, they exhibit the inverted Image invertedly, that is, a direct Image of the Object: Since then this Image is in the Focus of the third Eye-Glass, the Ray, after a fourth Refraction, will become Parallel, and in this Disposition the Eye will receive them, and consequently there will be distinct Vision, and the Object will appear erect.

Or as Molineux observes, p. 206 *Dioptrics*. That one Convex-Glass, that is the Object-Glass as posited in this Telescope inverts: The 2d, that is the first Eye-Glass does nothing towards erecting or reversing; but represents the Image, as it is in the *distinct Base* of the Object-Glass before it, that is *inverted*. The 3d, Glass erects, or rather restores what was before inverted. The 4th, represents the Image as it receives it from the *distinct Base* of the 3d, that is erect; because it inverts in the 3d, what was inverted in the first.

The Rays of Vision meeting in a Point before they reach the Retina in the Bottom of the Eye cause a confused Vision, the Fault of such, as are *Purblind*, which is help'd by Concave-Glasses, or by holding the Object very near.

On the contrary, the Eyes of Old Men, have their Chrystal-line too flat, and cannot correct the Divergence of the Rays to make them meet on the Retina; but beyond the Eye, where,

fore, for their help, 'tis requisite they add the adventitious Convexity of a Glass, that both it, and the Chrystalline together may be sufficient to make the Rays meet just at the Retina; and from thence it appears, that Spectacles help Old Men, notwithstanding magnifying an Object; but by making its Appearance distinct: for Old Persons cannot read the largest Print without Spectacles; and yet with Spectacles they read the smallest, tho' the Objects with Spectacles do not appear so large, as those without Spectacles.

#### *IV. To Know whether Glasses be Plane or Spherical.*

Shake them somewhat nimblly, between the Eye and Object; and if the Object seem to move by the Motion of the Glass, the Glass is not plane, the reason hereof is this, that towards the Extremities of a Glass, it refracts more than towards the Middle, and that Glass, which makes the Objects seem the most to move is form'd on the Less Sphere, whether Convex or Concave.

#### *V. To Combine, or put together a TELESCOPE of four Glasses.*

Take the 2 First Eye-Glasses, and Combine them by Tryals so as to make a distinct inverting Telescope.

Then take the Object-Glass, and first Eye-Glass, and by Tryals combine them likewise.

Lastly, take both these Telescopes, and without altering the Distances of their Glasses in either of them singly by Tryals, combine both these Telescopes, till the Appearance be clear and distinct.

What is here done by Tryals, may be effected by actual Measurement or designing out the Distances of the Glasses from each other by knowing their Focal Lengths.

#### *VI. To find the Foci of Glasses.*

If of pretty deep Convexities, apply them to the End of a Scale of Inches and Parts, and expose them before the Sun, and upon the Scale we shall find the bright Intersection of the Rayes exactly measur'd out. Or expose them in the Hole of a dark Chamber, and where a white Paper receives the distinct Representation of distant Objects, there is the Focus of this Glass. This is an universal and certain way for all Convexes.

## VII. The Wonderful Painting by means of an Object-Glass.

Make choice of a Room with a North Window so darkn'd, as to admit no Light to come in, save at the Hole, wherein fix the Object-Glass of a seven Foot Telescope, behind which let no Glass be, then in the dark Room move a Sheet to and fro, till you find the Out-Object appear distinct, there fasten it to the Cieling, then will whatever is without the Hole be represented on that sheet, with such exquisite Exactness, as far surpasses the utmost Skill of any Painter to express; for if the Sun shine brightly upon the Objects, we'll have the Color of all things there in their natural Paint, and such an admirable Proportion of Light, and Shadow, as is impossible to be imitated by Art.

N.B. Let not the Sun Shine near the Hole, else all will appear confused. Hereby their Motion is represented, as well as Color and Proportion, Postures, Gestures, as lively on the Cloth, as to any ones Eye without, only they will be all inverted, which to rectify, Hold a Looking-Glass over against the Sheet, with an acute Angle to your Breasts, and look down into it, and all things appear Natural and Erect, like so many Walking and Magical glaring Spectres.

## VIII. That Light is a Body.

First appears, by this Affection of being Refracted, and that in its passage thro' this, and 'tother Diaphanous body, it does and a different Resistance, now 'tis unconceivable, how any thing but Body, should suffer Resistance; because Resistance must proceed from contact of two Bodies, and contact either Active or Passive, belongs only to Body according to that of the Philosophic Poet, (*Lucretius*) *Tangere enim & tangi nisi Corpus nulla potest resisti.* It requires Time to move from one place to another, and does not in an Instant; but is only of all Motions, the quickest, requiring about 7 min. to pass from the Sun to us. 3dly, Light cannot by any Art, or Contrivance whatsoever, be increased or diminished, (that is to say) we cannot Magnify, for Instance, the Light of the Sun, or a Candle, no more than we can magnify a Cubic Inch of Gold, or make it more than Cubic Inch. But whenever we see Light increased 'tis by robbing of some other part of the Medium of its Light, or by bringing the Light that naturally should have been diffused thro' some other part to the more enlightened Place.

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The Focal Distance of the Object Lens, or the Length of the Telescope.	The Diameter of the Aperture of the Object Lens.	The Focal Distance of the Ocular Lens.	The Proportion of Magnifying, consider'd as to Diameter.
Rhinland Feet.	Inches, & Decimals.	Inches, & Decimals.	
1.	0,55.	0,61.	20.
2.	0,77.	0,85.	28.
3.	0,95.	1,05.	34.
4.	1,09.	1,20.	40.
5.	1,23.	1,35.	44.
6.	1,34.	1,47.	49.
7.	1,45.	1,60.	53.
8.	1,55.	1,71.	56.
9.	1,64.	1,80.	60.
10.	1,73.	1,90.	63.
13.	1,97.	2,17.	72.
15.	2,12.	2,33.	77.
20.	2,45.	2,70.	89.
25.	2,74.	3,01.	100.
30.	3,00.	3,30.	109.
35.	3,24.	3,56.	118.
40.	3,46.	3,81.	126.
45.	3,67.	4,04.	133.
50.	3,87.	4,26.	141.
55.	4,06.	4,47.	148.
60.	4,24.	4,66.	154.
65.	4,42.	4,86.	161.
70.	4,58.	5,04.	166.
75.	4,74.	5,21.	172.
80.	4,90.	5,39.	178.
85.	5,05.	5,56.	183.
90.	5,20.	5,72.	189.
95.	5,34.	5,87.	194.
100.	5,48.	6,03.	199.

*X. To find in what Proportion the Planets are enlightened by the Sun.*

The Famous M. Azout, used to enlighten an Object in what proportion he pleased, by applying a great Object-Glass by him call'd a *Planetary* one; because that by it he shew'd the Difference of Light, which all the Planets receive from the  $\odot$ , by taking use of several Apertures, Proportionate to their Distances from the  $\odot$ , provided that for every 9 Foot Draught, thereabout one Inch of Aperture be given for the Earth. Whence he observ'd, that the Light which *Mercury* receives is enough from being able to burn Bottles, and yet the same Light is great enough in  $\text{h}$  to see clear there; seeing that it appears greater in  $\text{h}$ , than it doth upon our Earth, when it is overcast with Clouds; which would scarce be believed, if by means of this Glass it did not sensibly appear so.

*. To make the Picture of any Thing appear in a Light Room.*

Opposite to the Place or Wall, where the Apparition is to let a Hole be made of about a Foot in Diameter, or bigger, there be an high Window, that hath a Casement in it, 'twill so much the better.

Without this Hole or Casement open'd, at a convenient Distance, (that it may not be perceived by the Company in the Room) place the Picture or Object to be represented, in an inverted Order, if possible, and by means of Looking-Glasses placed behind, if the Picture be transparent, reflect the Rays of the Sun so as that they may pass thro' it, towards the Place where it is to be represented, and to the End, that no Rays may pass before it, let the Picture be encompass'd on every Side, with a broad Cloth.

If the Object be a Statue, or some living Creature; then it will be very much enlightened by casting the Sun-beams on it, by Refraction, Reflexion, or both.

Between this Object, and the Place where it is to be represented, there is to be placed a broad Convex-Glass ground of a Convexity, as that it may represent the Object distinct in the said Place, which any one that hath Insight in Optics, may easily direct.

The nearer it is placed to the Object, the more is the magnified on the Wall, and the further off, the less, which verity is effected by Glasses of several Spheres.

If the Object cannot be inverted (as 'tis difficult to do Living Animals, Candles, &c.) then there must be two large Glasses of convenient Spheres, and they placed at their appropriate Distances (which are easily found by Tryals) so as to make Representation erect, as the Object.

These Objects Reflecting and Refracting Glasses, and the whole Apparatus, as also the Persons employ'd to Order, Change, and make Use of them must be placed without the said high Window or Hole; so that they may not be perceived by the Spectators in the Room, and the whole Operation will be easily perform'd.

Whatsoever may be done by means of the Sun-beams in the Day-Time, the same may be done with much more easily in the Night, by the help of Torches, about the Lamps, or other bright Lights placed about the Objects according to the several Sorts of them.

### *XI. Concerning Telescopes, where the Eye-Glass is Concave.*

2. When the Eye-Glass is concave, the Effect is founded on the same Principles, as in the Convex. The Distinctness of Appearance is procured in the same Manner; But here the Glass CD (in Fig. 2.) is placed between the Image EF, and the Object Glass AB: By this means the Rays, which come from the Right Hand Side of the Object, and proceed toward E the Left Side of the Image, being intercepted by the Eye-Glass, are carried to the Left Side of the Eye; and the Rays, which come from the Left Side of the Object, go to the Right Side of the Eye; so that the Impression in the Eye being inverted, the Object appears in the same Situation, as when viewed by the naked Eye. The Eye must here be placed close to the Glass. The Degree of magnifying, in this Instrument, is difficult to be found: Let the Rays, which pass through the Glass AB at H, after the Refraction of the Eye-Glass CD diverge, as if they came from the Point G; then the Rays, which come from the Extremities of the Object, enter the Eye under a small Angle at G, so that here also the Object will be magnified in the Proportion of the Distance between the Glasses, to the Distance of G from the Eye-Glass.

The Space, that can be taken in at one View in the Telescope, depends on the Breadth of the Pupil of the Eye; for as the Rays, which go from the Points EF of the Image, are soon

distant from each other, when they come out of the Glass, if they are wider asunder than the Pupil, it is evident they cannot both enter the Eye at once. In the other scope the Eye is placed in the Point G, where the Rays come from the Points E or F cross each other, and therefore must enter the Eye together. On this Account the Telescope with Convex Glasses takes in a larger View than those Concave; but in these also the Extent of the View is limited, because the Eye-Glass does not, by the Refraction towards its Edges, form so distinct a Representation of the Object near the Middle.

Hence an Astronomical Telescope is easily converted into a Land Telescope, by using three Eye-Glasses instead of one; and the Land Telescope, on the contrary, into an Astronomical one, by taking away two Eye-Glasses, the Faculty of magnifying remaining the same: Since the Distance of the Eye-Glass is very small, the Length of the Telescope is much the same as if only used one.

From the Construction it is evident that the Length of the Telescope is had, by adding five times the Semidiameter of the Eye-Glasses to the Diameters of the Object-Glass, the Plane Convex, or its Diameter if a Convex on both

edges first observed, both in the Astronomical and Land Telescope, that it contributes considerably to the Perfection of the Instrument, to have a Ring of Wood or Metal, with an Aperture, a little less than the Breadth of the Eye-Glass, fixed in the Plane where the Image is found to radicate upon the Object next the Eye; by means hereof the Colors which are apt to disturb the Clearness and Distinctness of the Object are prevented, and the whole Compass taken in at a View perfectly de-

monstrates, That the Perfection of Telescopes is impeded by the different Refrangibility of the Rays of Light, and not, as has been vulgarly supposed, by the spherical Figures of Glasses, and consequently they cannot be perfected by Glasses of Figures of the Conic Section, i. e. by Parabolic, Hyperbolic Glasses, &c. for having shewed the Ratio between the lesser and greater Refractions of the different Rays to be very nearly 7 to 28. he saith, Those that are skill'd in Optics will easily understand that the least circular Space, into which the Object-Glasses of Telescopes can collect all Sorts of parallel Rays, is about the  $\frac{27}{2}$  Part of half the Aperture of the Glass, or the  $\frac{55}{2}$  Part of the whole Aperture; and that the Focus of the most refrangible Rays is nearer to the Object-Glass than

the

the Focus of the less refrangible ones, by about  $\frac{1}{27}$  Part of the Distance between the Object-Glass, and the Focus of mean refrangible ones.

And if Rays of all Sorts flowing from any one lucid Point in the Axis of any Convex Lens, be made by the Refraction of the Lens to converge to Points not too remote from the Lens, the Focus of the most refrangible Rays shall be nearer to the Lens than the Focus of the least refrangible Ray, a Distance which is to the  $\frac{1}{27}$  Part of the Distance of the Focus of the mean refrangible Rays from the Lens, as the Distance between that Focus and the lucid Point from whence the Rays flow, is to the Distance between the lucid Point and the Lens very nearly.

After this he shews, by Experiments made with very great Accuracy, that the Rays of Light, which differ in Refractivity, do not all converge to the same Focus; but if they flow from a lucid Point, as from the Lens on the one Side, as the Foci are on the other, the Focus of the most refrangible shall be nearer to the Lens than that of the least refrangible, by above the  $\frac{1}{14}$  Part of the whole Distance: And if they flow from a lucid Point so very remote from the Glass, before their Incidence, they may be accounted parallel, the Focus of the most refrangible Rays shall be nearer to the Lens than the Focus of the least refrangible, by the  $\frac{1}{27}$ th or  $\frac{1}{28}$ th Part of their whole Distance from it: And the Diameter of the Circle in the Middle Space between these two Foci, which will illuminate when they fall there on any Plane perpendicular to the Axis, (which Circle is the least into which they can be gather'd) is about the  $\frac{1}{55}$ th Part of the Diameter of the Aperture of the Glass; so that 'tis a Wonder the Telescopes represent Objects so distinctly. But were all the Rays of Light equally refrangible, the Error arising only from the Sphericity of Figures of Glasses, would be many hundred times greater. And by Calculation, Page 70. he proves, That the Error arising from the Spherical Figure of Glasses, to that arising from the different Refrangibility of the Rays, is as 1 to 8151, and consequently is so little, as deserves not to be consider'd.

There is another Argument (saith our excellent Author, p. 73.) which proves, that the different Refrangibility of Rays is the true Cause of the Imperfection of Telescopes; the Errors of the Rays arising from the Spherical Figure of Object-Glasses, are as the Cubes of the Apertures of such Object-Glasses; and thence to make Telescopes, of various Lenses, magnify with equal Distinctness, the Apertures of the Object-Glasses, and the Charges, or magnifying Powers, ought to be as the Cubes of the Square Roots of their Lengths, which

not answer to Experience : But the Errors of the Rays arising from the different Refrangibility, are as the Apertures of the Object-Glasses; and thence to make Telescopes of various Lengths magnify with equal Distinctness, their Apertures and Charges ought to be as the Square Root of their Lengths; and this answers to Experience, as is well known : For Instance ; a Telescope of 64 Feet in Length, with an Aperture of  $2\frac{1}{3}$  Inches, magnifies about 120 times with as much Distinctness as one of 1 Foot in Length, with  $\frac{1}{2}$  of an Inch Aperture, magnifies 15 times.

By Reason of this different Refrangibility, he concludes : that there can scarce be any other Means of improving Telescopes by Refractions alone, besides that of increasing their Lengths ; for which End the late Contrivance of *Hugenius* seems well accommodated, (see *Philosophical Transactions*, N° 161.) for in his Aerial Telescope, the Glasses are readily manageable, and the Object-Glass being upon a strong upright Pole, becomes more steady.

## II. Of the Construction of a Reflecting TELESCOPE.

The Catoptric, or Reflecting Telescope, is a Telescope which instead of Lens's consists chiefly of Mirrors, and exhibits remote Objects by Reflection, as the other Telescope before describ'd does by Refraction.

The great Sir *Isaac Newton*, considering the different Refrangibility, which in his new Doctrine of Light and Colors he made appear the Light to consist of.

In Effect, as he found the Ratio between the greatest and least Refractions of the different Rays, to be nearly as 28 is to 1, it easily followed, that the Rays could never be all refracted parallel from any Lens, but would some of them diverge, some more, some less, besides that the Foci would be disturbed ; the Focus of the more refrangible Rays being nearer the Lens than those of the least refrangible Rays, by a Distance which is the 27th Part of the Distance between the Object-glasses and the Focus of the least refrangible ones.

Hence he concludes, that Refraction was too unequal a Principle, and that Lenses of whatever Figure, whether spherical, parabolical, or any other of the Conic Sections ; and how true soever ground, will never suffice for the Perfection of Telescopes.

Upon this he had recourse to another more equitable Principle, viz, Reflection, and made a Telescope, consisting of a

Metalline Speculum, the first Hint whereof he owns he took from Dr. Gregory's Optics.

The Construction of Sir Isaac Newton's reflecting Telescope as follows. The Object-Metal A, Plate 8. Fig. 3. is placed at one End of the Octangular Tube B B at a a; the Tube is about Six Feet long, and a little wider than what is sufficient to receive the Metal, dyed Black on the inside. The Radius of the Sphere, on which the Concave Metalline Speculum must ground fit for a Tube of such a Length, will be about Ten Feet, and consequently its Focal Length will be about 62 Inches. The Metalline Speculum is solder'd on the Back to another Brass, in the Back of which there is a Female Screw to receive a Handle, whenever the Metal is to be moved, in order to void soiling its polish'd Surface by handling. As far within the Focus of the Concave Speculum as is the Semidiameter of the Tube, there is to be placed an Oval Plane, composed of a Plate of the same Metal with the great Speculum, solder'd on the Back to another of Brass. Its Breadth is something less than half an Inch, and is in Proportion to its Length as one is to the Square Root of two. This plane Speculum is to be disposed so, as to reflect the Rays to E, which Point will be the Focus of the Concave Speculum; and if a Sheet of Paper were held to the Point E, the Image of the Object would be painted on the Paper by Reflection. There are belonging to the Instrument three Boxes with Convex Eye-Glasses, to be screwed on at the Focus E, that by the Help of those Glasses, the Eye may receive the Rays parallel, which proceed from the Image of the Object at E. When the first or Shallowest of the Eye-Glasses is made use of, it magnifies about 180 times the Diameter, with the Second about 200, and with the Third about 230 times: Each of those Glasses has placed in that Focus nearest the Oval, a Circle to determine the Part of the Object seen at one View; and in the other Focus, towards the Eye, a Brass Plate, with a little Hole in the Middle, to let no Light pass from the Eye to the Inside of the Tube, but what comes from the Oval. Besides these three Convex, there are two Concave Eye-Glasses, with which it magnifies about 200 and 210 times, and also a Sett of three Convex Eye-Glasses, which turn it into a Day-Telescope, magnifying about 125 times. The Aperture is limited by a Circle of Card or Pasteboard, placed before the Object-Metal in the Tube. To vary the Aperture, there are three of those Circles, and the Apertures allowed by them are Five Inches and an Half, Five Inches, and Four and an Half, tho' for some Objects the whole Metal may be left open.

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On the Top of the Tube is fix'd, on two small Pedestals, a common Dioptric Telescope about 18 Inches long, its Axis parallel to that of the Tube, and having two Hairs placed in the common Focus of its Object, and Eye Glasses crossing one another in its Axis. By this Dioptric Telescope, the Object may be brought to be opposite to the Tube of the reflecting Telescope, much sooner than to the reflecting Telescope alone, and is represented in the Figure at M N.

The open Air has commonly an undulating Motion in its parts, especially in the Day-time, which occasions the Rays of Light to deflect a little from the strait Lines in which they ought to move, in order to render the Species perfectly distinct: The Effect of this, though insensible to the naked Eye, or even through a small Telescope, becomes considerable when the Object is very much magnified.

Dr. *Gregory's* Reflecting Telescope (who was certainly the first that gave the Construction of those Telescopes, tho' not the first that put them in Practice) is very much different from Sir *Isaac Newton's* Telescope: The Construction of Dr. *Gregory's* is thus; Let A B C D. Plate 8. Fig. 4. be a Tube, open at D; in the End B C there is to be fitted a Concave Speculum, m n, in which there must be a Hole x x agreeing to a Hole y y of the Tube A B C D; within the Focus of the Concave Speculum, as at G, there is to be placed a plane Convex Speculum as c c, which receiving the Image of the Object from the Concave Speculum, reflects the Rays back upon the Concave Speculum, diverging, a Quantity of those Rays pass thro' the Hole x x, where they are received by the Tube M o c n, in which there are Eye-Glasses of the same Nature with common Refracting Telescopes, which Tube M o c n, being screw'd to the Tube at y y, the Observer will receive a distinct Image of the Object, and erect: Thus tho' the Principles of Sir *Isaac's* and Dr. *Gregory's* Telescopes be the same, yet their Construction are different, Sir *Isaac's* Telescopes having the Eye-Glasses placed upon the Side of the Tube, as at e, and in Dr. *Gregory's* Telescopes they are placed in the End, as at y, where they look directly as in Refracting Telescopes. Both Sorts of these Reflecting Telescopes are now made to very great Perfection, by *Edward Scarler*, Optician to his Majesty, by St. *Ann's* Church, *Soho*; he has lately made one of Dr. *Gregory's* Telescopes of about 9 Inches in Length, by which the Satellites of *Jupiter* are very distinctly observed: Also, there is a late Contrivance, by which the Azimuth and Altitude of any Cœlestial Phænomenon, may be observed at the same Time that the Object is observed by those reflecting Telescopes: But this Contrivance, as also the Movements, which

carry the Telescope either vertically or horizontally, are immediately understood when seen.

### XIII. *Of the Uses of T E L E S C O P E S.*

By the Help of Telescopes distant Objects are more certainly and exactly observed than they can be by our simple View; for by the Measure of Angles we find the apparent Diameters of distant Bodies, for the apparent Diameters of Bodies grow bigger the nearer we come to them, and that they are increased almost in the same Proportion that the Eye approaches them; (for Example; If any Man were ten times nearer to the Moon than we are, and did there observe her, he would see the Moon ten times bigger in her Diameter, and clearer than we do; (in Diameter, I say, for the Surface would appear 100 times larger than it does to us). If here on our Earth we should take a Telescope, which only increases the Diameter ten times, and look to the Moon with it, the Moon will have the same Appearance seen with such a Telescope, as would appear to a Spectator ten times nearer the Moon than we are; but if we should use Telescopes (and such there are, which magnify the Diameters of Objects 100 or 200 times) they will shew the Moon in the same Manner, Figure, and Bigness, as it would appear in, at a Distance 100 or 200 times less than ours is from the Moon. Hence we can perceive, with our Eyes, what Face, and how large the Moon would shew itself at the Distance of three Diameters of the Earth: As likewise, we can discern how the Moon would appear if we approach'd much nearer, and view her only at the Distance of 1900 Miles, for from thence we should be able to discover, in the Moon, vast Ridges of Mountains, deep Caverns, many Vales, and large open Fields. By the Means of Telescopes we still ascend higher in the Heavens, and we can approach the Planets and Comets and fixed Stars, so near, that of such immense Distances there remains only the Hundredth or Two Hundredth Part to have the whole Journey finished; for, as is before observ'd, a Telescope, that magnifies One Hundred Times, makes any Object appear to us, when view'd by such Telescope, as if the Distance between the Observer and that Object were divided into One Hundred equal Parts, and if the Observer were removed Ninety Nine of those Parts nearer to the Object, the Observer, with the naked Eye, would then see the Object in the same Bigness in Diameter and Surface, and other Appearances, as the same Observer on our Earth observes the same Object.

# of TELESCOPES.

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ject with a Telescope that magnifies One Hundred times; and Telescopes are of vast Use in observing the apparent Diameters of the Cœlestial Bodies, so likewise we thereby are able to judge of the Proportion of their Distances from us, and the proportion their true Diameters bear to one another; for if their Distances be equal, their true Diameters will be as their parent, and if their apparent Diameters are equal, their true diameters will be proportional to their Distances: Hence, if the parent Diameters of the Sun and Moon be equal, let the Sun be One Hundred times further from us than the Moon, the Sun must needs be One Hundred times in Diameter bigger than the Moon.

If we know the apparent Diameter of any Body, we can from thence exactly know by the help of Trigonometrical Tables what Proportion the Distance of that Body bears to its true Diameter; for suppose any Object to be seen by the Eye under an Angle of one Degree; the Distance of that Object will be to its Diameter, as the Radius of a Circle is to the Tangent of one Degree. The Sun appearing under an Angle of about half a Degree, or 30 Minutes; this Distance will be to its real Diameter as 10000 to 87, the Tangent of half a Degree. Hence we are certain, that the Sun's Distance from us is nearly equal to 115 of his own Diameters; and if an Eye were placed on the Sun to observe the Angle under which the Diameter of the Earth appear'd from thence: we then should be able to tell exactly the Distance of the Sun from us in Diameters of the Earth or Miles.

In order to determine the apparent Diameters of the Planets; as also to measure other small Distances in the Heavens accurately; there have been several sorts of Micrometers apply'd to the Focus of Telescopes: the Construction of the most simple of those Micrometers is as follows: In the Focus of a Telescope fit a Brass or Iron Ring A B with Female Screws diametrically opposite to each other; into these Female Screws insert Male Screws A E and F B of such Lengths as that they may be turn'd into the Tube so as to meet each other, and with this Instrument very small Spaces in the Heavens may be accurately measured; for when any two Objects view'd thro' the Tube appear contiguous to the Screws, if the Telescope be turn'd about to two other Points that do also exactly appear contiguous to the Screws, they remaining in the same Position as before, if the Distance asunder of those two latter Points be known or can be measured, the same will be the Distance asunder of the first two Objects. To determine how many Seconds answer to each Thread of those Screws, observe two Points in the Heavens, whose Distance is accurately known, and

turn

turn the Screws till they appear contiguous with those known Objects; and observe the Number of Threads corresponding to that Interval; then by the Rule of Three it may easily be determin'd how much of that, or any other Interval agrees with every Thread of the Screw; thus, by saying, As the Number of the Threads of the Screws requir'd to measure the known Distance, is to the known Distance in Seconds; so is one Thread to a fourth Number, which fourth Number is the Number of Seconds answering to each Thread of every Screw. After the same manner may a Table be made, by which the apparent Distances of Objects, or the apparent Diameters of the Planets may be found by Inspection; having the Number of Threads of the Screws that measure that Interval.

N. B. The Screws should be as exactly made as possible.

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A Complete ACCOUNT  
OF OUR  
SOLAR SYSTEM,  
CONTAINING the  
PLANETS, COMETS,  
AND  
FIXED STARS.

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## S E C T . I .

**T**HIS true Solar System was the most Antient of all first introduced into *Greece*, by the Great *Pythagoras*, and his Disciples, who had learnt it from the Wisemen of the *East*, to whom as to an University, they then all resorted for Instruction. 'Tis true the other Apparent System, which supposes the Earth immovable, and the Heavens to revolve about it, was received among the Vulgar, and Illiterate part of Mankind; yet the Philosophers retain'd the true System; *Aristotle*, and the Philosophers that came after him, degenerating from their Predecessors, and not being acquainted with the Philosophy, embraced the common System of the Vulgar: so that the Antient System was forgot, and not minded till the Time of *Nicolaus Copernicus*, who again brought it to Life, and retrieved

retrieved it from Oblivion, and established it by Solid Arguments and Reasons, whence this System is now call'd the *American System.*

After the Invention of Telescopes, the Secundary Planets with many New, and unthought of Appearances were observ'd in the Heavens by the Astronomers since the last Century which did wonderfully enlarge the Antient System, and confirm'd it with Invincible Demonstrations, *viz.*

That the Earth could not be the Center of the Planetary Motions at rest, because of

The Retrogradations of the Planets. The Appearance of the unequal, and irregular Motions. The Phænomena of  $\delta$ ,  $\varphi$  and especially prove they revolve about the  $\odot$ . The Gravitation of  $\odot$  and Earth. The Harmony of the Planets, Periods, Distances and Revolutions about their Axes. The Oblate Spheroidal Form of the Earth, which is 31 Miles higher at the Equator than the Poles. Also,

When two *fixed Stars* sometimes asunder, do appear at other Times to eclipse each other; and above all the Annual Parallaxes of the *fixed Stars*. Also, If the Earth were the Center  $\varphi$ , and must have all the Aspects, whereas neither has so much as  $\odot$ :  $\star$ :  $\varphi$  and  $\odot$  pass between the Earth and Sun, and appear Spots, which could not be, if the Earth was the Center of the Motion: Lastly, the *Phases* of  $\varphi$ , which the Telescopes discover to be like those of our  $\odot$  do invincibly confirm the same.

Before the Invention of this noble Instrument, when *Copernicus* first revived the antient Pythagorean System, and propos'd it to the Learned in Astronomy, to whom he maintained, that the Planets, among which, he reckon'd the Earth did move round the Sun, which was immovable in the Center: It was objected to him, that if the Motions of the Planets were as he supposed them to be, that then  $\varphi$  ought to undergo the same Changes and Phases, as the  $\odot$  does. *Copernicus* answer'd, that perhaps the Astronomers in after Ages, would find that  $\varphi$  does not undergo all these Changes. This Prophecy of *Copernicus* was first believ'd and fulfill'd by that great Italian Philosopher *Galileus*, who, setting his Telescope to  $\varphi$  observed her Appearances to emulate the  $\odot$ , as *Copernicus* had foretold, and these Observations did surprizingly confirm the Old System.

True Astronomy has all its Parts fitly joyn'd together in most agreeable Harmony and Order, it leads us to the Knowledge of the Universe, and the wonderful Symmetry, Beauty and regular Disposition of all the Bodies that compose it, that Infinite Wisdom, who made all things in Number, Weight and Measure, who doth nothing in Vain, nor uses many things, when one will perform: There is nothing in Nature, that does more

piercing Force of human Understanding, the Sublimity of its Calculations, and deep researches, than true Astronomy : It raises our Minds above our Senses, and even in Contradiction them shews us the *true System of the World*. The Faculty of Reason, by which we have made these great Discoveries in the Heavens, must needs be derived from Heaven : since no Earth-principle can attain so great a Perfection, and since the Orientation of our Minds is from Heaven, it may be expected that they will endeavour to return thither, and Heaven will become their final Habitation.

Twas necessary for the Advancement of Astro-tomy to distinguish the Stars into Asterisms or Constellations by Figures and Names, which are of great Antiquity, and seem to be as Old as Astronomy or Philosophy it self : for in the most antient Book of Job, *Orion*, *Arcturus*, and the *Pleiades* are mention'd, and meet with the Names of many in the Writings of the first Poets, *Homer* and *Hesiod*, by the Help of which Constellations, the antient Astronomers have been able to distinguish, and mark out the Stars of the Firmament, and with great Care and Industry they have digested them into Catalogues, which they have deliver'd down to Posterity ; these Catalogues have been much increased, and corrected by our Modern Astronomers, for now they not only comprehend the Stars visible by the naked Eye, but also many that are not to be observ'd or seen without a telescope.

*Hipparchus* the Rhodian, about 120 Years before the Birth of CHRIST, was the First among the Greeks, who reduced the Stars into a Catalogue, daring, according to *Pliny*, to undertake a thing, which seem'd to surpass the Power of Mortals, that is to Number the Stars for Posterity, and to reduce them to Rule, &c.

*Hipparchus*, from his own proper Observations, and those of the antient Astronomers before him inserted into his Catalogue 1022 Stars, and annexed to each of them their proper Longitude and Latitude ; which they had at that Time.

*Ptolemy* enlarg'd *Hipparchus's Catalogue* only with four Stars sumbring 1026.

Then *Ulug Beighi* the Grandson of the great *Tamerlane* observ'd again the Stars, and reduced 1017 of them into a Catalogue.

In the Sixteenth Century, and since, Astronomy was courted by many Admirers and Suiters, among whom we may chiefly reckon *Regiomontanus* and *Copernicus*. But the noble Danish Astronomer, *Nicolaus Copernicus*, in adorning, and perfecting this Science did far surpass the Labours of all that went before him ; who procured very large, and exquisitely well contrived Instruments, for observing

*The Introduction.*

serving the Heavens, and particularly he determin'd the places of 777 fixed Stars, and reduced them into a Catalogue, the places being all calculated from his own proper Observations. Kepler increased that Number, to 1163, from *Ptolemy*, and other Authors.

Contemporary with *Tycho*, was *William Prince of Hesse*, who likewise observ'd the Stars, and with the Assistance of *Rubens* and *Brygias* two Mathematicians, by 30 Years continual Labour computed the places of 400 Stars, all founded on his own Observations, and inserted them in a Catalogue.

The Jesuit *Ricciolius* enriched the Catalogue of *Kepler*, with 305 Stars, by which means their Number was increased to 1468; but not above 100 were of his own Observation, the rest took from *Tycho*, *Kepler*, and others.

*Bartschius*, in his Book of the 4 Foot Globe, boasts that himself had painted on his Globe 1762 Stars; but does not tell us by whom, or in what Year they were observed.

The Southern Stars, which are not seen in our Climate, were first accurately observ'd by Doctor *Edmund Halley*, now Royal Professor of Astronomy, in the Island of St. Helena, and published a Catalogue of 373 of them, whose places he adapted to the End of the Year 1677.

The illustrious *John Hevelius of Danzick*, with indefatigable Industry computed the places of 1553 Stars from his own proper Observations, and so he composed a New Catalogue, which contain'd 1388, viz. 950 known to the Antients, 603 New ones, which no one before had ever rightly observed, and to these he joyn'd 335 Southern Stars taken out of Doctor Halley's Catalogue, which never appear in the Horizon of Danzick.

But the Largest, and most Complete Catalogue of the Stars we have from the Labours of that excellent Observer, *Dr. Flamsteed*, late Royal Professor of Astronomy: whose Number reach to 3000, rectified to the Year 1716. as *Hevelius* doublet by his Observations, the Number of Stars observ'd by *Tycho*, our British Astronomer has as far out done *Hevelius*. We are much indebted to this Astronomer for the Increase of our Knowledge we have of the Celestial Bodies, that there is not the least Star in the Heavens to be seen, whose Place and Situation is not better known, than the Position of many Cities, thro' which Travellers do daily pass. Nor is it any Wonder, that the Astronomers should take so much Pains, and so obstinately watch the *fixed Stars*, to determine their places: for without the exact settling of their Positions and Places they could never have found out the Ways of the Planets, nor have described their Orbits; for this is upon the Observation

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# THE SOLAR SYSTEM according to their mean

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The Line of the Comet

which appeared 1662

684 A.D. and upwards

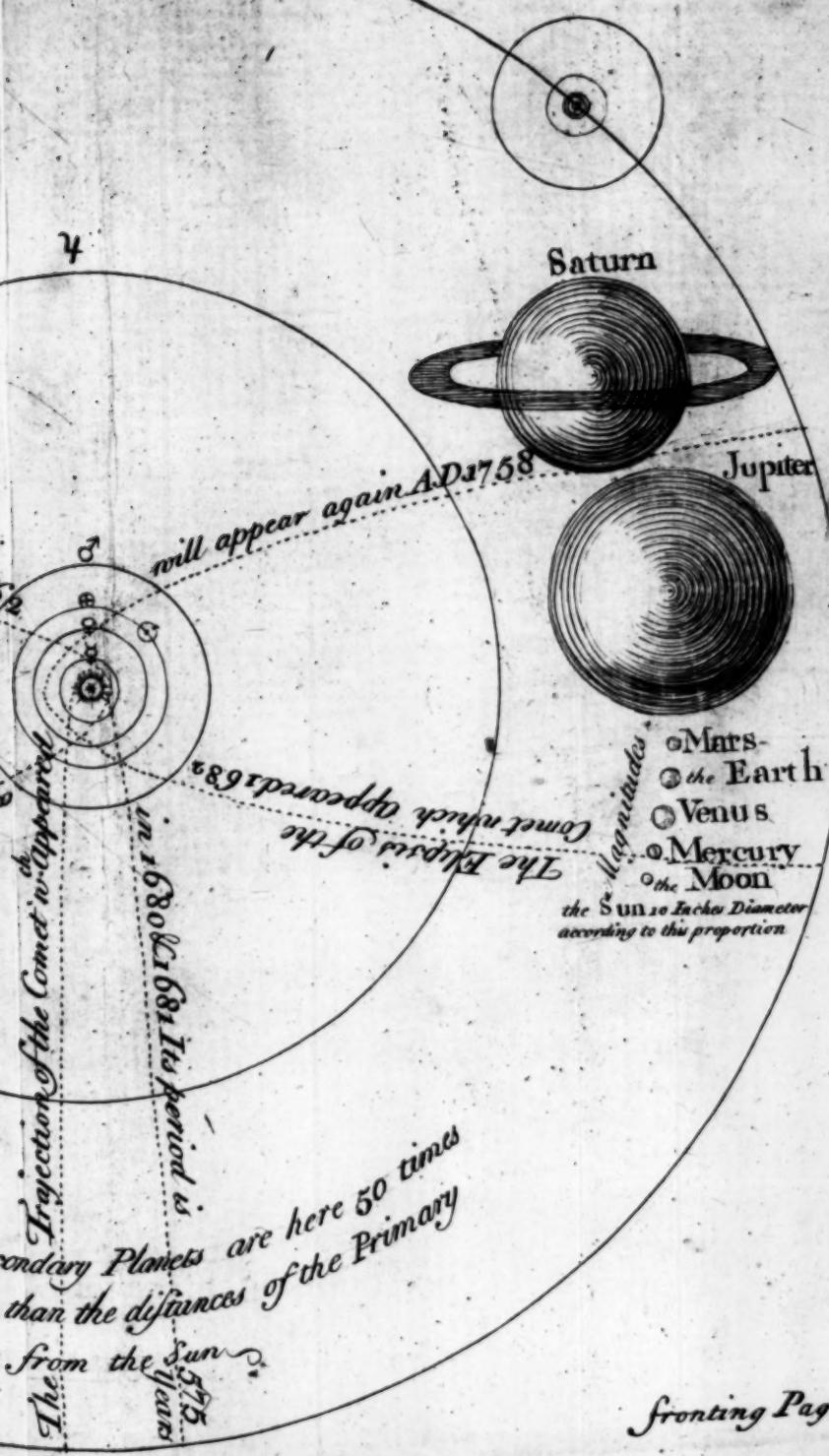
The Trajectory of the Comet which appeared

NB The Orbit of the Secondary Planets from the Sun is greater in proportion than the distance of the Primary Planets from the Sun.

Plate IX.

J. Grimes.

# THEM Or the Orbits of the Planets distances from the Sun



fronting Page 62

Stars, that the whole Science of Astronomy is erected, them it is sustain'd. e not in the following Sheets, which are principally d to Instruct, divert, and improve young Gentlemen, ed them with the physical Causes of the Celestial Moti- ch to understand clearly, require an Insight into deep ry, lest it should at first confound, and make the e too difficult: therefore, ought it more advantageous to explain the Motions, and Account of the Phænomena, that arise from these Mo- which when once understood, there will be an easy Ad- into the Knowledge of their Physical Causes, which n with Ease and Advantage be learnt from the Excellent of Doctor Gregory, and the incomparable Sir Isaac Newton. I enter upon the Planetary, and Cometary System, the Noblest part of Astronomy, give me leave to ad- Courteous Reader, that I shall confine my self to the Account, and meddle with nothing of Eccentrics, Epicycles,ibrations. Solid Orbs, and the Hypotheses of Ptolomy, Tycho, why should I tire and perplex with Shadows and Sy- llly exploded, when the Truth is manifest, whereby the Order, Position and Places of the Planets may be ad understood far better, and more easily, according we, than according to these Fictitious Systems. I may not set forth the Contrivances of Mortals; but to be admired and adored Wisdom of the Great and Glo- eator, of whom the Royal Psalmist under a Divine In- thus breaks forth. *The Heavens declare the Glory of God, and men shew his handy Work;* and again, *the Heavens declare his ess, and all the People have seen his Glory.*

*the Order and Periods of the Primary Planets  
going about the Sun; and of the Secondary Planets  
round their respective Primaries.*

un is placed in the midst of an immense Space, where-  
Spake Spherical Bodies revolve about him  
Center. These wandering Globes are called Planets.  
ers, who at different Distances, and in dif-  
eriods, perform their Revolutions from West to East, in  
wing Order.

Mercury is neareſt to the Sun of all the Planets, and  
its Course in about three Months. ♀ Venus in a-

acters placed before the Names of the Planets, are for Brevity's sake  
made use of by Astronomers, instead of the Words at length, as ♀

bout seven Months and a Half. 3. E. The Earth in a Year, & Mars in about two Years. 5. ♀ Jupiter in twelve. And lastly, ♂ Saturn, whose \* Orbit includes all the rest, spends almost 30 Years in one Revolution round the Sun. The Distances of the Planets from the Sun are nearly in the same Proportion as they are represented in Plate 9. viz. Supposing the Distance of the Earth from the Sun to be divided into 10 equal parts, that of Mercury will be about 4 of these parts; of Venus 7; of Mars 15; of Jupiter 52; and that of Saturn 95.

The Orbits of the Planets are not all in the same Plane, but variously inclined to one another; so that supposing one of them to coincide with the above Scheme, the others will be one half above, and the other half below it; intersecting each other in a Line passing through the Sun.

#### Ecliptic.

The Plane of the Earth's Orbit, is called the Ecliptic, and this the Astronomers make the Standard, by which the Planes of the other Orbits are judged to incline. The right Line passing thro' the Sun, and the common Intersection of the Plane of the Orbit of any Planet, and the Ecliptic, is called the Line of the Nodes of that Planet; and the Points themselves, wherein the Orbit cuts the Ecliptic, are called the Nodes.

The Inclinations of the Orbits of the Planets to the Plane of the Ecliptic, are as follows, viz. The Orbit of Mercury makes an Angle with it of almost 7 degrees; that of Venus something above  $3\frac{1}{2}$  degrees; of Mars, a little less than 2 degrees; of Jupiter,  $1\frac{1}{2}$  degrees, and of Saturn, about  $2\frac{1}{2}$  degrees. The Orbits of the Planets are not Circles, but Ellipses or Ovals. What an Ellipsis is, may be easily understood from the following Description. Imagine two small Pegs fixed upright on a Plane, and suppose them tyed with the Ends of a Thread somewhat longer than their Distance from one another; now if a Pin be placed in the double of the Thread, and turned quite round, (always stretching the Thread with the same force) the Curve described by this Motion is an Ellipsis. The two Points where the Pegs stood, (about which the Thread was turned) are called the Foci of that Ellipsis; and if without changing the Length of the Thread, we alter the Position of the Pegs, we shall then have an Ellipsis of a different Kind from the former; and the nearer the Focus's are together, the nearer will the Curve described be to a Circle; until at last the Focus's coincide, and then the Pin in the doubling of the

\* By the Orbit of a Planet, is commonly understood the Tract or Ring described by its Center round the Sun; but by the Plane of the Orbit is meant that Surface extended every way thro' the Orbit infinitely.

thread will describe a perfect Circle. The Orbit of all the Planets, have the Sun in one of their Focus's; and if the Distance between the two Focus's is called the Eccentricity of the Orbits. This Eccentricity is different in all the Planets; but in most of them it is so small, that in little Schemes or Instruments, made to represent the planetary Orbits, it need not be considered.

The Six Planets above-mention'd, are called *Primitives*, or *Primary Planets*; but besides these, there are other lesser Planets, which are called *Secondaries*, or *Satellites*. These Moons always accompany their respective Primaries, and perform their Revolutions round them; whilst both together are also carried round the Sun. Of the Six Primary Planets, there are at three, as far as Observations can assure us, that have these attendants, viz. the *Earth*, *Jupiter*, and *Saturn*.

The Earth is attended by the *Moon*, who performs her Revolution in about  $27\frac{1}{2}$  days, at the Distance of about 30 Diameters of the Earth from it; and once a Year is carried round the Sun along with the Earth.

*Jupiter* has four *Moons* or *Satellites*; the first or innermost performs its Revolution in about one Day and  $\frac{1}{2}$  Hours, at the Distance of  $5\frac{2}{3}$  Semidiameters of *Jupiter* from his Center; the second revolves about *Jupiter* in 3 Days and 13 Hours, at the Distance of 9 of his Semidiameters; the third in 7 Days and 4 Hours, at the Distance of  $14\frac{1}{3}$  Semidiameters; the fourth and outermost, performs its Course in the space of 16 Days 17 Hours, and is distant from *Jupiter's* Center,  $\frac{1}{2}$  of his Semidiameters.

*Saturn* has no less than five *Satellites*; the first or innermost revolves about him in 1 Day and 21 Hours at the Distance of  $4\frac{2}{3}$  Semidiameters of *Saturn* from his Center; the second completes its Period in  $2\frac{1}{2}$  Days at the distance of  $5\frac{2}{3}$  of his Semidiameters; the third, in about  $4\frac{1}{2}$  Days at the Distance of 8 Semidiameters; the fourth performs its Course about 16 Days, at the Distance of 18 Semidiameters; the fifth and outermost takes  $79\frac{1}{2}$  Days to finish his Course, and is at a Distance of 30 Semidiameters of *Saturn*, Distant from his Center. The Satellites as well as the Primaries perform their Revolutions from West to East: the Planets or the Orbits of the Satellites of the same Planet are variously inclined to one another, and consequently are variously inclined to the Plane of the Orbit of their Primary.

Besides these Attendants, *Saturn* is encompassed with a thin plane Ring that does no where touch his Body; the Diameter of this Ring is to the Diameter of *Saturn* as 9 to 10.

Eccentricity.

Primary Planets.

Secondary Planets.

*Jupiter's* four Moons.

*Saturn* has five Moons.

9 to 10.

9 to 4; and the void space between the Ring and the Body of *Saturn*, is equal to the breadth of the Ring it self; so that in some situations the Heavens may be seen between the Ring and his Body. This surprising Phenomenon of *Saturn's Ring* was first discovered by the famous Italian Philosopher *Galilaeus*, by a Telescope, which he first invented; and the celebrated *Cassini*, French King's Astronomer, was the first that saw all the *Seas* of *Saturn*; which by reason of their great Distances from the Sun, and the smallness of their own Bodies, cannot be seen by us, but by the help of very good Glasses.

*Annual Motion.* The Motion of the primary Planets round the Sun (as also of the Satellites round their respective Primaries) is called their *Annual Motion*; because they have one Year or Alteration of Seasons complete in one of these Revolutions. Besides this Annual Motion, four of the Planets, viz. *Venus*, the *Earth*, *Mars*, and *Jupiter*,

*Diurnal Motion.* revolve about their own Axes, from West to East; this is called their *Diurnal Motion*. For by this Revolution each point of their Surfaces, is carried successively towards or from the Sun, who always illuminates the Hemisphere which is next to him, the other remaining obscure; and while any Place is in the Hemisphere illuminated by the Sun, it is *Day*; but when it is carried to the obscure Hemisphere, it becomes *Night*; and so continues until by this Rotation, the said place is again enlightened by the Sun.

*Diurnal Motion of the Earth, Venus, Mars, and Jupiter.*

*Sun and Moon likewise turn round their Axes.*

*The Planets are Opake and Globular.*

I. The Planets are all opake Bodies, having no Light but what they borrow from the Sun: For that side of them which is next towards the Sun, has always been observed to be illuminated, in what position soever they be; but the opposite side, which the Solar Rays do not reach, remain dark and obscure; whence it is evident that they have no Light but what proceeds from the Sun: for if they had, all parts of them would be lucid without any darkness or shadow. The Planets are likewise proved to be Globular, because let what part soever of them be turned

toward

wards the Sun; its Boundary, or the Line separating that from the opposite, always appears to be Circular; which could not happen if they were not Globular.

II. That the Earth is placed betwixt the Orbs of <sup>The Planets</sup> Mars and *Venus*, and that  $\oplus$ ,  $\odot$ ,  $\delta$ ,  $\oplus$ , and  $\oplus$ , do <sup>turn round the Sun</sup>, is proved from Observati-

as follow :

i. Whenever *Venus* is in Conjunction with the Sun, that is, when she is in the same Direction from the Earth, or towards the same part of the Heavens the Sun is in; she either appears with a bright and round Face like a full Moon, or else disappears; or if she is visible, she appears horned like a new Moon; which Phænomena could never happen, if  $\oplus$  did not turn round the Sun, and was not betwixt him and the Earth: For since the Planets borrow their Light from the Sun, it is necessary that  $\oplus$ 's lucid Face should be towards the Sun; and when she appears fully illuminated, she shews the same Face to the Sun and Earth; and at that time she must be above or beyond the Sun, for in no other Position could her illuminated Face be seen from the Earth. Farther, when she disappears, or if visible, appears horned; that Face of hers which is towards the Sun, either wholly turned from the Earth, or only a small part of it can be seen by the Earth; and in this case she must of necessity be betwixt us and the Sun. Let <sup>Place to Fig.</sup>  $\odot$  be the Sun,  $T$  Earth, and  $\oplus$  Venus, having the same <sup>1. 2.</sup> presented both towards the Sun and Earth: here it is plain that the Sun is betwixt us and *Venus*, and therefore we must either place *Venus* in an Orbit round the Sun, and likewise betwixt him and us, as in Fig. 1. or else we must make her to move round the Earth in an Orbit within that of *Venus*, as in Fig. 2. Again, after *Venus* disappears, or becomes horned, either <sup>\*</sup>  $\oplus$  with the  $\odot$ , she then must be betwixt us and the Sun, and must move either in an Orbit round the Sun, and betwixt us and him, as in Fig. 1. or else round the Earth, and betwixt us and the Sun, as in Fig. 2. But *Venus* cannot move sometimes within the Sun's Orbit, and sometimes without it, we must suppose if she moves round the Earth; therefore it is plain that her Motion is round the Sun.

Besides the foregoing, there is another Demonstration that *Venus* turns round the Sun, in an Orbit that is within the Earth's; because she is always observed to keep near the Sun, and in

$\oplus$  is a Mark commonly used for Conjunction; thus  $\oplus$  with the  $\odot$  is to be understood Conjunction with the Sun.

the same Quarter of the Heavens that he is in: for she recedes from him more than about  $\frac{1}{4}$  of a whole Circle; therefore can never come in Opposition to him; which necessarily happen, did she perform her Course round the Earth either in a longer or shorter time than a Year. And the reason why *Venus* is never to be seen near Midnight, but either in the Morning or Evening, and at most not above

or four Hours before Sun-rising, or after Sun-set.

*Why Venus is always either our Morning or Evening Star.* From the time of  $\mathbb{Q}$ 's superior Conjunction (she is above the Sun) she is more Easterly than the Sun, and therefore sets later, and is seen a

setting, and then she is commonly called the Evening Star. But from the time of her inferior conjunction till she comes again to the superior, she then becomes more Westerly than the Sun, and is only to be seen in the Morning before Sun-rising, and is then called the Morning Star.

After the same manner, we prove that *Mercury* turns round the Sun, for he always keeps in the Sun's Neighbourhood, and never recedes from him, so far as *Venus* does; and therefore the Orbit of  $\mathbb{Q}$  must lie within that of  $\mathbb{V}$ ; and on the account of his Nearness to the Sun, he can seldom be seen without a telescope.

*The Orbit of Mars includes the Earth's.* Mars is observ'd to come in Opposition, and to have all other Aspects with the Sun, and always preserves a round, full, and bright Appearance, except when he is near his Quadrat Aspect,

he appears somewhat Gibbous, like the Moon three Days before or after the Full: Therefore the Orbit of Mars includes the Earth within it, and also the Sun; for if he were placed betwixt the Sun and us, at the time of his inferior Conjunction, he would either quite disappear, or appear

*Fig. 1.* nated, as *Venus* and the Moon do in that Position. Let *S* be the Sun, *T* the Earth, and *A, P* Mars, his Conjunction and Opposition to the Sun, and in his Quadratures, when he is somewhat gibbous from the Earth at *T*: 'Tis plain hence, that the Orbit of Mars does include the Earth, otherwise he could not come in Opposition to the Sun; and that it includes the Sun, else he could not appear full at his Conjunction.

*Mars*, when he is in Opposition to the Sun, looks about seven times larger in Diameter, than when he is in Conjunction with him; and therefore must needs be almost seven times nearer to us in one Position than in the other: For the apparent Magnitudes of far distant Objects increase or decrease

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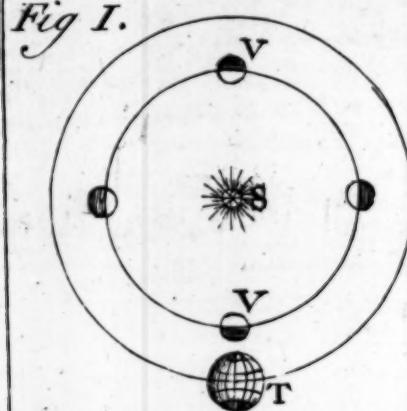
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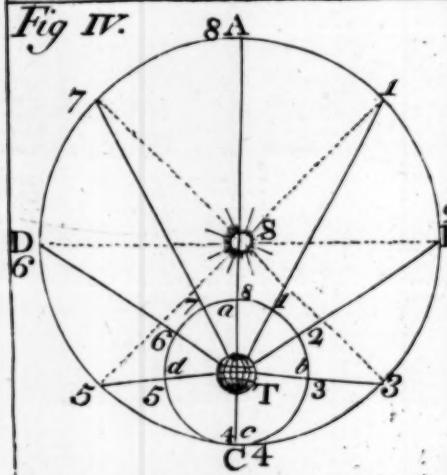
*Fig. I.*



*Fig II.*



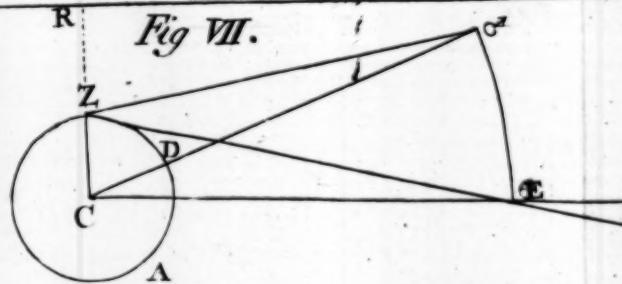
*Fig IV.*



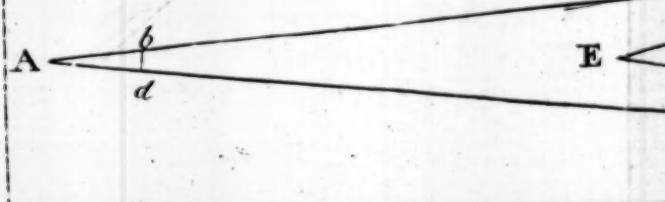
*Fig V.*

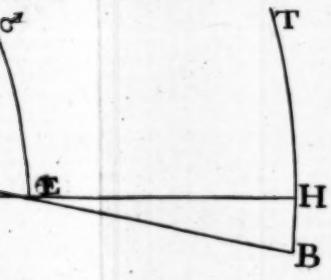
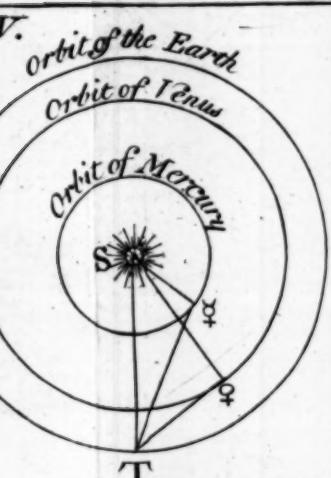


*Fig VII.*

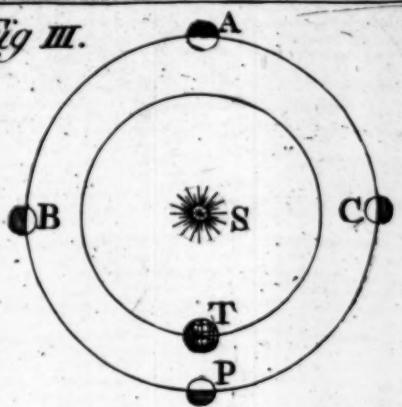


*Fig VIII.*

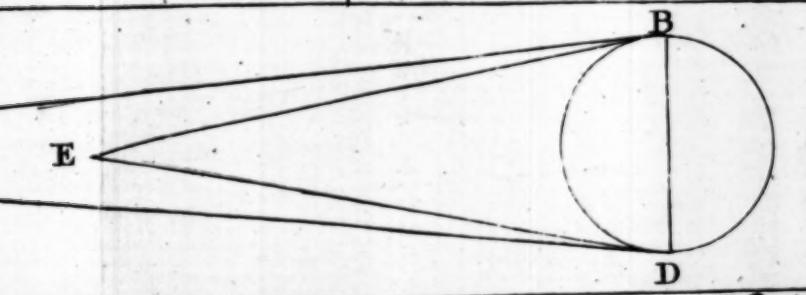
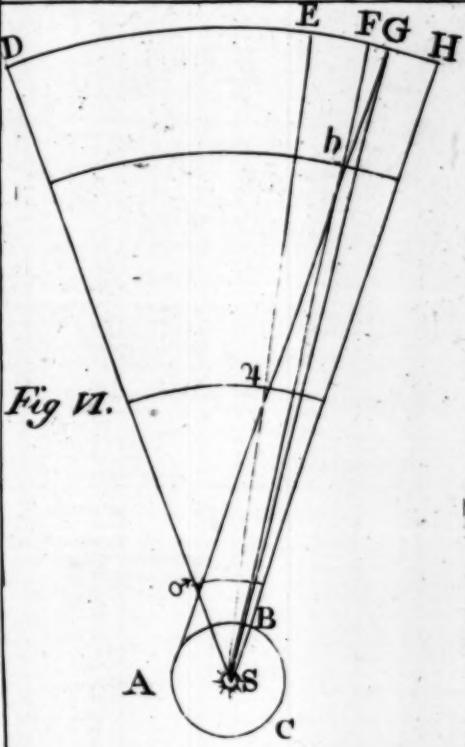




*Fig III.*



*Fig VI.*



ion to their Distances from us. But *Mars* keeps always the same Distance from the Sun ; therefore it is plain, is not the Earth, but the Sun that is the Center of his

proved in the same way, that *Jupiter* and *Saturn* have the Sun and the Earth within their Orbits, and that the Sun, and not the Earth, is the Center of their Motions ; altho' proportion of the Distances from the Earth, is not so Jupiter as it is in *Mars*, nor so great in *Saturn* as it is in *Earth*, by reason that they are at a much greater Distance from

have now shewn that all the Planets turn <sup>Inferior and Superior Planets.</sup> the Sun, and that *Mercury* and *Venus* are interposed between him and the Earth ; whence they are the *Inferior Planets* : and that the Earth is placed

in the Orbit of *Mars* and *Venus* and therefore included in the Orbit of *Mars*, *Jupiter* and *Saturn*; whence they are the *Superior Planets* : And since the Earth is in the middle of moveable Bodies, and is of the same Nature with them, we conclude, that she has the same sort of Motions ; but

she turns round the Sun, is proved thus, The Earth does not stand still but turns round the Sun.

The Planets seen from the Earth appear to move unequally ; as sometimes to go faster, at other times slower ; sometimes to go backward, and sometimes to be stationary, or not to move at all ; which could not happen if the Earth stood still. Let

the Sun, T the Earth, the great Circle A B C D, Orbit of *Mars*, and the Numbers 1, 2, 3, &c. its Motion round the Sun ; the correspondent Numbers &c. in the Circle a, b, c, d, the Motion of *Mars* as it would be seen from the Earth. It is plain from this Figure, that if the Earth stood still, the Motion of *Mars* would be always progressive, (tho' sometimes very unequal;) but since the observations prove the contrary, it necessarily follows, that

the Earth turns round the Sun.

Annual Periods of the Planets round the Sun determined, by carefully observing the length of time since their Departure from a certain Point in the Heavens (or from a Fixed Star) until they arrive at the same again.

By these sorts of Observations the Antients determined the periodical Revolutions of the Planets round the Sun ; and were so exact in their Computations, as to be capable of predicting Eclipses of the Sun soon. But since the Invention of Telescopes, Astronomical Observations are made with greater Accuracy, and of consequence our Tables are far more perfect than those of the Antients.

tients. And in order to be as exact as possible, Astronomers compare Observations made at a great Distance of time from one another, including several Periods; by which means the Error that might be in the whole, is in each Period subdivided into such little parts, as to be very inconsiderable. Thus the mean Length of a Solar Year is known even to Seconds.

The Diurnal Rotation of the Planets round their Axes, was discovered by certain Spots which appear on their Surfaces. These Spots appear first in the Margin of the Planets Disks, (the Edge of their Surfaces,) and seem by degrees to creep towards their Middle; and so on, going still forward, till they come to the opposite Side or Edge of the Disk, where they set or disappear: and after they have been hid for the space of time that they were visible, they again appear to rise in or near the same place as they did at first; then to creep progressively, taking the same course as they did before. These Spots have been observed on the Surfaces of the Sun, Venus, and Jupiter; by which means it has been found, that these Bodies turn round their own Axes in the times before-mentioned. It is very probable, that Mercury and Saturn have likewise a Motion round their Axes, that all the parts of their Surfaces alternately enjoy the Light and Heat of the Sun, and receive such Changes as are proper and convenient for their Natures. But by reason of the nearness of ♀ to the Sun, and his immense Distance from him, no Observations have hitherto been made, whereby their Spots (if they have any) could be discovered, and therefore their diurnal Motions could not be determined. The diurnal Motion of the Earth is computed, from the apparent Revolution of the Heavens, and of all the Stars round it, in the space of a natural Day. The Solar Spots do not always remain the same, but sometimes old ones vanish, and afterwards others succeed in their Room; sometimes several small ones gather together, and make one large Spot, and sometimes a large Spot is seen to be divided into many small ones. But, notwithstanding these Changes, they all turn round with the Sun in the same time.

The better to conceive the apparent Annual and Diurnal Motions of the Sun or the real one's of the Earth. Imagine a Worm creeping slowly in the Ecliptic one degree forward, while the Globe is turn'd once the contrary way, thus may the Earth be said to describe each Day a Parallel to the Equinoctial, though properly 'tis a spiral Line, and yet is never out of the Ecliptic, but to represent to the Eye these Appearances as they truly are. Light a Candle in a dark Room, and take a small Globe of 2 or 3 Inches Diameter, in which mark the Poles, Equator, and some Parallels with some Meridians passing from Pole to Pole.

en so hold this Globe before the Candle, that its Axis may not be Perpendicular to the Plane of the Table, on which the Candle stands; but let it be inclin'd to it in an Angle nearly of  $\frac{1}{2}$  Degrees, then place the Globe in such a manner, that one of Poles may point directly North, and let the Light of the Candle reach from Pole, to Pole that is, let the Circle bounding Light and Shadow first pass thro' the two Poles of the Globe, then the Position of the Axis be well observed, and then move the Globe round the Candle, with your Hand in a Circle parallel to the Horizon, holding it so, that the Axis may always point the same way, and retain the same Inclination to the Horizon: is done, you will see that the Flame of the Candle will in the same manner illuminate this Globe, as the Sun actually does the Earth, and the Poles of the Globe, its Aequator and Paral-  
lels will undergo the same Vicissitudes of Light and Darkness.

The Relative Distances of the Planets from the Sun, and likewise from each other, are determined by the following Methods: First, the Distances of the two inferior Planets  $\text{\textcircled{V}}$  and  $\text{\textcircled{E}}$  from the Sun in respect of the Earth's Distance from him, is had by observing their greatest Elongation from the Sun as they are seen from the Earth.

The greatest Elongation of *Venus* is found by observation to be about 48 degrees, which is the Angle  $\angle \text{S T E}$ ; whence, by the known Rules of Trigonometry, the Proportion of  $S \text{ } \text{\textcircled{V}}$ , the mean Distance of *Venus* from the Sun to  $S \text{ } \text{T}$ , the mean Distance of the Earth from him, may easily be found: After the same manner, in the right-angled triangle  $S \text{ } \text{T} \text{ } \text{\textcircled{M}}$ , may be found the Distance  $S \text{ } \text{\textcircled{M}}$ , of *Mercury* from the Sun. And if the mean Distance of the Earth from the Sun  $S \text{ } \text{T}$  be made 1000, the mean Distance of *Venus*  $S \text{ } \text{\textcircled{V}}$  from the Sun will be 723; and of *Mercury*  $S \text{ } \text{\textcircled{M}}$  387: And if the Planets revolved round the Sun in Circles, having him for their Center, the Distances here found would be always their true Distances; but as they move in Ellipses, their Distances from the Sun will sometimes greater, and sometimes less. Their Eccentricities are computed to be as follow, viz.

Eccent. of  $\left\{ \begin{array}{l} \text{Mercury } 80 \\ \text{Venus } 5 \\ \text{Earth } 169 \end{array} \right\}$  of the parts abovementioned.

The Distances of the superior Planets, viz.  $\text{\textcircled{J}}$ ,  $\text{\textcircled{S}}$ , and  $\text{\textcircled{U}}$ , are found by comparing their true places, as they are seen from the Sun, with their apparent places as they are seen from the Earth. Let  $S$  be the Sun, the Circle  $A \text{ } \text{B} \text{ } \text{C}$  the Earth's Orbit,  $A \text{ } G$  a Line touching the Earth's

*How the Relative Distances of the Planets from the Sun are determined.*

*Fig. 5. Elongation.*

*Fig. 6.*

*Orbit*

Orbit in which we'll suppose the superior Planets are seen from the Earth, in the Points of their Orbits  $\delta$ ,  $\varphi$ ,  $\text{h}$ ; and let  $DG$ ,  $GH$ , be a Portion of a great Circle in the Heavens at an infinite Distance: Then the Place of Mars seen from the Sun is  $D$ , which is called his true or *Heliocentric Place*, but from the Earth he'll be seen in  $G$ , which is called his apparent or *Geocentric Place*. So likewise *Jupiter* and *Saturn* will be seen from the Sun in the Points  $E$  and  $F$ , their Heliocentric Places; but a Spectator from the Earth will see them in the Point of the Heavens  $G$ , which is their Geocentric Place. The Arches  $DG$ ,  $EG$ ,  $FG$ , the differences between the true and apparent Places of the superior Planets, are called the *Parallaxes* of the Earth's annual Orb, seen from these Planets. If thro' the Sun we draw  $SH$  parallel to  $AG$ , the Angles  $A\delta S$ ,  $A\varphi S$ ,  $A\text{h}S$ , will be respectively equal to the Angles  $DSH$ ,  $ESH$ , and  $FSH$ ; and the Angle  $AGS$  is equal to the Angle  $GSH$ , whose Measure is the Angle  $GH$ ; which therefore will be the Measure of the Angle  $AGS$ , the Angle under which the Semidiameter  $AS$  of the Earth's Orbit, is seen from the Starry Heavens. But this Semidiameter is nothing in respect of the immense Distance of the Heavens or Fixed Stars; for from thence it would appear under no sensible Angle, but look like a Point. And therefore in the Heavens the Angle  $GSH$ , or the Arch  $GH$  vanishes; and the Points  $G$  and  $H$  coincide; and the Arches  $DH$ ,  $EH$ ,  $FH$ , may be consider'd as being of the same Bigness with the Arches  $DG$ ,  $EG$ , and  $FG$ , which are the Measures of the Angles  $A\delta S$ ,  $A\varphi S$ ,  $A\text{h}S$ ; which Angles are nearly the greatest Elongation of the Earth from the Sun, if the Earth were observed from the respective Planets, when the Line  $G\text{h}\varphi\delta A$ , touches the Earth's Orbit in  $A$ . The nearer any of the superior Planets is to the Sun, the greater is the Parallax of the Annual Orb, or the Angle under which the Semidiameter of the Earth's Orbit is seen from that Planet. In *Mars* the Angle  $A\delta S$  (which is the visible Elongation of the Earth seen from *Mars*, or the Parallax of the Annual Orb seen from that Planet) is about 36 Degrees; and therefore the Earth is always to the inhabitants of *Mars* either their Morning or Evening Star, and is never seen by them so far distant from the Sun, as we see *Venus*. The greatest Elongation of the Earth seen from *Jupiter*, being nearly equal to the Angle  $A\varphi S$  is about 11 degrees. In *Saturn* the Angle  $A\text{h}S$  is but 6 degrees; which is not much above  $\frac{1}{4}$  part of the greatest Elongation we observe in *Mercury*. And since *Mercury* is so rarely seen by us, probably the Astronomers of *Saturn* (except they have better Optics than we have) have not yet discovered, that there is such a Body as our Earth in the Universe.

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N. B.

The Parallax of the Annual Orb, or the greatest Elongation of the Earth's Orbit seen from any of the superior Planets, being given; the Distance of that Planet from the Sun, in respect of the Earth's Distance from him, may be found by the same methods as the Distances of the inferior Planets were. Thus, to find the Distance of Mars from the Sun, it will be as the sine of the Angle  $\delta \& A$  is to the Radius, so is the Distance  $S$ , (the Distance of the Earth from the Sun) to  $S \delta$ , that Distance from the Sun to Mars. After the same manner the Distances of Jupiter and Saturn are also found. The mean Distance of the Earth from the Sun being made 1000, the mean Distances of the superior Planets from the Sun are, viz. the mean Distance from the Sun of

$$\left\{ \begin{array}{l} \delta \ 1524 \\ \varpi \ 5201 \\ h \ 9538 \end{array} \right\} \text{ and the Eccentricity } \left\{ \begin{array}{l} 141 \\ 250 \\ 57 \end{array} \right\}$$

which if we add to, or subtract from their mean Distances, we shall have the greatest or least Distances of those Planets from the Sun.

There are other Methods, by which the relative Distances of the Planets might be found; but that which has been here illustrated, is sufficient to evince the Certainty of that Problem.

Hitherto we have only considered the Distances of the Planets in relation to one another, without determining them by any known Measure; but in order to find their absolute Distances in some definite Measure, there must be something given, whose Measure is known. Now the Circumference of the Earth is divided into 360 Degrees, and each of these Degrees into  $60$  Geographical Miles, so that the whole Circumference contains 21600; and by the known Proportion for finding the Diameter of a Circle from its Circumference, the Earth's Diameter will be found to be 6872 Miles, and its Semidiameter 3436 Miles. The Parallax of the Earth's Semidiameter, or the Angle under which it is seen from a certain Planet, may be found by comparing the true Place of the Planet as it would be seen from the Center of the Earth, (which is known by Computation) with its apparent Place, as it is seen from some Point on the Earth's Surface. Let  $C Z A$  be the Earth,  $Z C$  its Semidiameter,  $E$  some Planet, and

*How the Absolute Distances of the Planets from the Sun are computed.*

*Parallax of the Earth's Semidiameter.*

Fig. 7.

N. B. 60 Geographical Miles are Equal to  $69\frac{1}{2}$  English Miles.

B H T an Arch of a great Circle in the Heavens, at an infinite Distance. Now the Planet E will appear from the Earth's Center C, in the Point of the Heavens H; but a Stator from the Point Z, upon the Earth's Surface, will see the same Object E in the Point of the Heavens B; and the Arch B H the Difference is equal to the Angle B E H = E C, the *Parallax*; which being known, the Side C E the Distance of the Planet from the Center of the Earth, at the time, may be easily found. Now if this Distance of the Planet from the Earth be determined, when the Centers of the Sun, the said Planet, and of the Earth, are in the same right Line, we have the absolute Distance of the Planet's Orbit from the Earth's in known Measure: then it will be, as the relative Distance betwixt the Earth's Orbit and that of the Planet is to the relative Distance of the said Planet from the Sun, so is the Distance of the Planet's Orbit from the Earth's in known Measure, to the Distance of the said Planet from the Sun in the same Measure: Which being known, the Distances of all the other Planets from the Sun may be found. For, will be, as the relative Distance of any Planet from the Sun, to its Distance from him in a known Measure; so is the relative Distance of any other Planet from him, to its Distance in the same Measure. This may be done by finding the Distance of the Planet *Mars*, when he is in Opposition to the Sun, after the same manner as we find the Distance of a Tree, or the like, by two Stations.

Let  $\delta$  be *Mars*, D the Point on the Earth's Superficies, when *Mars* is vertical, when he is in Opposition to the Sun, (which may be exactly enough found by Calculation) at which time an Observer, at the Point Z, (whose Situation from D must be known) take the Altitude of *Mars*, whose Complement will be the Angle  $\delta Z R$ ; then in Triangle  $\delta Z C$  will be given the Angles  $\delta Z C$ , the Angle C whose Measure is the Arch  $D Z$ , and consequently the Angle  $Z \delta C$  the Parallax, and also the Side  $Z C$  the Semidiometer of the Earth; by which we may find  $C \delta$  the Distance of *Mars* from the Earth. The extreme Nicety required in this Observation, makes it very difficult to determine the exact Distances of the Planets from the Sun; but the celebrated Dr. *Halley* has, in the Philosophical Transactions, shewed us a more certain Method for finding the Distances of the Planets; which is by observing the Transit of *Venus* over the Sun.

*How the Magnitudes of the Planets are determined.*

The Eye judgeth of the Magnitudes of far distant Objects, according to the Quantities of the Angles under which they are seen (which are called their apparent Magnitudes;) and these Angles ap-

or greater or less in a certain Proportion to their Distances; wherefore the Distances of the Planets from the Earth, and their apparent Diameters being given, their true Diameters, and from thence their Magnitudes) may be found. How the Distances of the Planets may be found, has been already shewn; their apparent Diameters are found by a Telescope, having a Machine fixed to it for measuring Angles, called a revolving Achrometer. Let  $B D$ , or the Angle  $B A D$  be the Fig. 8. apparent Diameter of any Planet, and  $A B$ , or  $AD$ , which by reason of the great Distances of the Planets in respect of their Magnitudes) may be considered as being the Distance of the said Planet from the Observer. Now in the Triangle  $ABD$ , having the Sides  $AB$ ,  $AD$  given, and the Angle  $A$ , we have also the other Angles  $B$  and  $D$ , (because the Angles  $A B$ ,  $A D$  are equal) whence the Side  $B D$  the Diameter of the Planet may be easily found by Trigonometry.

From hence it appears, that the same Body at different Distances, will seem to have very different Magnitudes: Thus, the Diameter  $B D$  will appear, from the Point  $E$ , to be twice as large as from the Point  $A$ . It also follows, that a small Body, even at no great Distance from us, may appear to be equal, or even to exceed another at a great Distance, tho' immensely bigger. Thus  $b d$  appears under the same Angle, and consequently of the same Bigness from the Point  $A$ , that the same  $B D$  doth, tho' one vastly exceeds the other. And this is the Reason, why the Moon, which is much less than any of the Planets, appears to us vastly bigger than either of them, and even to equal the Sun himself, which is many thousand times greater in Magnitude.

*Why the Moon  
appears bigger  
than any  
of the Planets.*

The Distances of the Planets, and Periods round the Sun, their Diameters and Velocities round their own Axes, &c according to modern Computations, are as follow in this.

Exact

Periodical Revolution of	Saturn.	Jupiter.	
Daily Motion.	Y. D. H. I. II. 29. 174. 6. 36. 26.	Y. D. H. I. II. 11. 317. 12. 20. 35.	D. H. 331. 23.
Aphelion Anno, 1725.	27. 47. 0.	24. 9. 4.	0.
Ascending Node.	21. 45. 12.	20. 7. 23.	18.
Annual Motion of Node.	36.		
Greatest { Mean Distance from ☽.	{ 1008. 342. 953. 800. 898. 956.	{ 545. 011. 520. 110. 494. 221.	{
Least { Eccentricity.	{ 54. 700. D. H. I. II. 29. 10. 1. 16.	{ 25. 091. H. I. A. 9. 56. 1.	{
Revolution about the Axis of Inclination of Orbit.	D. 2. 30. 30.	D. I. 22. 1.	D. 1.
Bigger than our Earth times		298.	
Apparent Semidiameter.		H. III. 10. 30.	
Less than our Earth times.			
Heat near the Surface.		75	
Diameter in English Miles.	67. 870.	81. 135.	
Weight of Bodies on the Surface.	536.	94.	
Density.	60.	7.	
Quantity of Matter.	97.	21.	
Parallax of Earth's { Greatest Orbit.	{ 6. 28. 5. 34.	{ 11. 11. 10. 35.	{
Least.			

That is a *Saturnian Astronomer* would never observe the Earth more than  $6^{\circ}.28'$ . nor less than  $5^{\circ}.34'$ . from the Sun in its farthest Elongations ; so that it is hard to say, whether they or the *Fovial Astronomer* have yet discover'd that there is such a Body, as our Earth, or our Moon in the Universe.

**SATURN** is the highest Planet, has always a roundfull Face of a heavy dull Lead-colour, and may be Eclipsed by all the Planets, when in ☽ with him ; every 378 Days is in Conjunction with the Sun, and has 5 Moons revolving about his Body, which can be seen only with a very large Tube. He has also a Ring or Belt surrounding him (like the Horizon of an Artificial Globe) and no where touching him, whose Plane is at the time nearly parallel to our Earths Aequator ; but more exac-

### §. III. Exact Planetary Synopsis. 177

Mars.	Earth.	Venus.	Mercury.
D. H. I. II. 321. 23. 27. 30.	D. H. I. II. 365. 5. 48. 57.	D. H. I. II. 224. 16. 49. 24.	D. H. I. II. 87. 23. 15. 53.
31. 27. 0. 27. 0. 18. 13. 0. 43.	VS 7. 35. 12. Præcess Equin. 50.	I. 36. 7. II. 4. 12. 0. III. 14. 35. 0. 37.	4. 5. 31. I. 12. 53. 0. V. 15. 47. 0. I. 36.
$\sum 166. 385.$ $\sum 152. 369.$ $\sum 138. 199.$ 14. 100. H. I. 24. 40. D. 1. 51.	$\sum 101. 732.$ $\sum 100. 000.$ 98. 268. I. 741. H. 24.	$\sum 72. 791.$ $\sum 72. 333.$ 71. 719. 517. 33. D. 3. 23. 0.	$\sum 46. 608.$ $\sum 38. 710.$ 30. 689. 7. 970. H. 6. D. 6. 54. 0. (as some suppose.)
4.	at ☽	II. III. 10. 30.	5.
35.		3.	87.
$\frac{4}{10}.$ 4. 444.	1. 7. 935. 1. 258. 387. 1.	2. 7. 906.	7. 4. 240.
$\sum 36. 22.$ $\sum 30. 34.$		$\sum 36. 32.$ $\sum 35. 12.$	$\sum 25. 22.$ $\sum 16. 47.$

forms an Angle with the Ecliptic of about  $31^\circ$ , and its Diameter is  $2\frac{1}{2}$  of Saturn's Diameter, and the Distance of the Ring from the Planet, is about the Breadth of the Ring it self, which some are call'd the Ansæ or Handles of *Saturn*. He is so removed, that we cant behold his Spots. The Immersions his (or ♃'s Satellites or Moons) can be seen only, when he is oriental i. e. which is from ♈ to ♉, and their Emerisions when he is occidental or from ♉ to ♈, but if they be in exact ♈ to the ♉. It will be in vain to look for either; the Shadow being cast perfectly behind him.

*JUPITER* is the next Planet to *Saturn*, has always a round full Face, of a very fulgent and beautiful Aspect, and may be eclipsed by all the Planets, except H. ♁ is in ♈ with the ☽ every 398 Days, and has 4 Moons, which if observ'd with a

A a

Telescope

Telescope of only 2 Convex-Glasses, they always appear the contrary Side of  $\mathfrak{P}$ .

Now the reason why *Saturn* and *Jupiter* have always a round Face, is because their illuminated Half is likewise turn'd towards the Earth as well as the Sun, because the Earth seen from  $\mathfrak{P}$  is always near the Sun's Body, that is near the Center of their Motions; but the Orbit of  $\mathfrak{J}$  lying near our Earth his Face which is towards the Sun will not always be turn'd towards our Earth, this causes his Increase and Decrease of Light.

Because  $\mathfrak{U}$  is 5 Times further off the Sun, than the Earth, the apparent Diameter of the Sun seen from *Jupiter* will be 5 times less, than it is seen from the Earth, and will be bigger than 6 Minutes, to  $\mathfrak{U}$ , which to us is  $30^{\circ}$ , and the Disk of the Sun will appear 25 Times less than it does to us, who likewise receive but the 25th part of the Light and Heat from him that we enjoy. But *Saturn* being 10 Times farther from the Sun, than we, the apparent Diameter of Sun seen from him will be no bigger than 3 Min. and will be but little more than twice the Diameter of  $\mathfrak{Q}$ , when she approaches nearest to the Earth, and therefore the Disk of the Sun, as it would appear to a *Titanian* Astronomer will be 100 Times less than we see it, as both its Light and Heat are there diminished in the same Proportion, and therefore the nearest Regions in *Saturn*, even under his Equator are supposed much cooler than our Frigid Zone.

*MARS* moves between the Earth and *Jupiter*, is of a red Color, and supposed to have an Atmosphere; because the Fixed Stars when near his Body appear obscure'd, and if he were extinct, when in  $\mathfrak{S}$  to  $\odot$  he is very near our Earth, and his horizontal Parallax  $37^{\circ} 34' 34''$ . and is 2 Years, and so dimensions between every Conjunction with the  $\odot$ .  $\mathfrak{J}$  increases and decreases in Light like our  $\mathfrak{D}$ , and in his Quadratures is almost bisected, and when he is in Perigeon or  $\mathfrak{S}$  he is 7 Times nearer the Earth, than in Apogee or  $\mathfrak{C}$  with  $\odot$ , and is therefore 7 Times bigger and brighter, yea he is nearer us, than  $\mathfrak{Q}$ ,  $\mathfrak{J}$ , and  $\odot$  himself. In 1656, was observ'd to have a broad obscure Zone or Belt to Shadow near half his Disk, he may be eclipsed by the Sun,  $\mathfrak{Q}$ ,  $\mathfrak{J}$ , and  $\mathfrak{D}$ .

*Mars*. In his nearest Approach to the Earth, was most accurately observ'd, and his Parallax determin'd to be  $30^{\circ} 1'$ , from whence the Sun's Parallax is scarce  $11^{\circ} 1'$ , and his Distance about 19000 Earth's midiameters of the Earth.

*Mars* always keeps nearly at the same Distance from the Sun, but not from the Earth; therefore the Sun, and not the Earth is the Center of his Motions the same may be said of *Jupiter* and *Saturn*.

The Earth has one Satellite, i. e. our  $\oplus$ , has a Conical Shadow, whose Vertex reaches not so far as the Orb of Mars at a mean Distance, the length of the Earth's Shadow is 214 Semidiameters and the Moon's Shadow, but 58, and the Height of the Atmosphere 47. 12 English Miles.

An Inhabitant of the Earth observes the Sun, which is really immovable to go thro' the same Circle in the Heavens, and in the same space of Time, that a Spectator in the Sun would see the Earth describe, and the like in all the other Planets *mutatis mutandis*; thus one in  $\mathbb{U}$  would think the Sun turns round him in 12 Years, and one in  $\mathfrak{H}$  in 30 Years, and in different Circles, since therefore 'tis impossible that the Sun can have all these Motions really in it self we may safely affirm, that there are none of them real, but that they are all apparent and rise from the Motions of the Earth, and other respective Planets.

*VENUS* moves in an Orb between the Earth and  $\oplus$ . She is the most splendid of all the Planets, and is a Year and 219 Days between one Conjunction, and another with the  $\odot$  of the same kind, that is  $\oplus$  is conjoynd with the Sun in the Superior Part of her Orb, when she is in Apogaeon direct, and always Oriental, but when conjoynd with the Sun in the lower Part, she is in Perigeon, and Retrograde, and if her Latitude be less than the  $\odot$ 's apparent Semidiameter, she will then appear a black Spot on the Sun's Disk, the like of  $\oplus$ ; but between a Direct  $\odot$ , and a Retrograde  $\odot$  with the  $\odot$ , are only 300 Days; in the last, she is 6 Times nearer us, than the first, even the Diameter of her Orbit: when she becomes Retrograde, she is always Occidental of the  $\odot$ . Every 8 Years she is nearly in the same Place again, when she is Occidental, and near her Perigeon at her greatest Elongation from the Sun, she shines so bright, as to cast a Shadow, and shine in the Day-time, as she did 1630, May 29. at the birth of King Charles II. she appears horn'd, Gibbous and Full, and increases and decreases in Light, as our  $\oplus$ . In May 26th, in the Year 1761.  $\oplus$  will pass by the Body of  $\odot$ , whence the Sun's Distance may be ascertain'd within  $\frac{1}{88}$  part of the whole.

*MERCURY* being so near the Sun, is seldom seen, and in the space of 13 Years may be found nearly in the same Place, and 115 Days between one mean  $\odot$  with  $\odot$ , and another of the same kind, the Color of Mercury somewhat resembles that of Mars, and is too near the Sun, to discover many of his Spots, in so much that some yet question, whether he turns about his Axis.

That *Venus* and *Mercury* in  $\odot$  with  $\odot$  by a Retrograde Motion pass between the Earth, and  $\odot$ . this could not be, if the Earth were the Center of the Universe.

That  $\oplus$  is never more than  $48^{\circ}$ . and  $\odot$  never more, than  $28^{\circ}$  from the Sun, which could not be, if the Earth were at rest in the Center of the Universe.

**IV. The Chief Phænomena of the Sun**

I. The Sun's Center is observed to move every Year in the same Plane, or Ecliptic-line, and is never found to change its Course.

Because by the Laws of Nature, the Earth is always moving in that Plane about the Sun.

II. The Sun appears to be moved unequally, being Swiftest after the *Winter Solstice*, and Slowest after the *Summer Solstice*.

For the Earth is moved about the Sun, not in a Circle, but an Ellipsis, which hath the Sun in one of its Foci; evident, because there are about 8 Days Difference between Motion from  $\text{V}$  to  $\text{A}$ , and that from  $\text{A}$  to  $\text{V}$ .

III. The apparent Diameter of the Sun is greatest in *Winter*, when his Motion is Swiftest, than it is in *Summer*, when his Motion is Slowest.

Because in *Winter* he is in Perigee, or nearest the Earth, in *Summer* in Apogee, or farthest from it. Hence the Diameter must alter in Proportion to its Distance, and seeing the Sun's apparent Motion, and apparent Diameter, are found to answer to the Distance of the Earth from the Sun, when the same is computed, according to an Ellipsis, and not according to an Eccentric Circle, we easily gather, that the Orbit of the Earth is not properly Circular, but Elliptical.

IV. Those Places of the Ecliptic, in which the Difference of those apparent Motions, and Diameters are greatest, are chang'd in Process of Time, and they always with an even Motion, and towards the Consequent Signs.

Because the Apparent Motion of the Aphelion of the Earth is found to be Equal to the Annual Motion of the Equinoctial Points, the Moderns have for very good Reason supposed the Earth to move in an Ellipsis, and to approach the Sun at Aphelia,

helia of the Stars to be unmoved with respect to the *fixed* Stars, but allow they appear to advance as fast as the Equinoctial Points go back.

V. The Ecliptic being divided into two equal Parts by the Equinoctial Points, the Sun makes a longer Journey, by about the Space of 8 Days in the North part, from Spring to Autumn, than it doth in the South part from Autumn to Spring.

because the upper Part of the Ellipse is not only considerably larger, but the Sun's apparent Motion slower than in the lower Part of the Ellipse, hence the Sun must needs appear more slowly in the Northern Signs than in the Southern Signs; 'tis here worthy to observe, that this Inequality of about 8 Days is different from what it was in Ptolomy's Time, and will continually decrease, until length vanish for a Time, and then encrease and decrease alternately, so long as the annual Motion shall endure, being greatest when the Line of the Solstices coincides with the long Axis, and nothing when it coincides with the Shorter.

VI. Yet is the Space of one entire Revolution, which we call a Year equal to it self, or the same one Year, that it is another, consisting of 365 Days, 5 Hours, 48<sup>1</sup>, 57<sup>11</sup>.

though there be an Inequality in the Parts of this Revolution, as compared amongst themselves, yet seeing one Part gives place to the other looses, and this Inequality is always in the same proportion, the Quantity of the whole Revolution must necessarily always be the same.

II. The Declination of the Ecliptic from the Horizon hath been found nearly the same in all Ages, about 23° ½.

so' it was accounted some Minutes more by the Antients, than it hath been by the Moderns, probably occasion'd by the Inaccuracy of their Instruments, and too general Neglect of observations. Parallaxes, &c. yet by Modern accurate Methods, the Declination appears always the same, and unvaried for what time it can be observed, without disturbing the Earth from keeping that Angle perpetually, which it was once constituted.

VIII. The

VIII. The Diurnal Parallax of the *Sun* is almost sensible, and its Menstrual scarce ariseth unto a quarter of a Degree.

The Parallax of the *Sun*, may be found three severall ways. 1st By the Diagram of *Hipparchus* used by all the Antient Astronomers, who like Surveyors attempted to find the Sun's Distance by two Stations, in each of which they noted its Diameter upon the Earth, the other at the top Point of the Shadow; no wonder if they fail'd in the Attempt: yet hence we see that the Sun's Parallax is so very small, as to elude all Attempts this way, it consisting rather of Seconds than Minutes; that its Distance is so immensely Great, that it is to be reckoned not by a few Miles; but many thousand Semidiameters of the Earth.

2d Is by Observation of the *Moon* in her exact Quadrature by *Kepler*, *Vendelinus*, *Ricciolus*, which is an excellent Method, and posesseth the Semidiameter of *Y*'s Orbit equal to 60 Semidiameters of the Earth might bear some sensible Proportion to the Distance tho' a single Semidiameter did not. See *Plate the 11th*.

N. B. The Menstrual Parallax of *Q* is the Difference of the Parallaxes there is in the *Q*, as seen from the Earth, and as seen from the *Moon*; in this Method the precise Moment of Bisection of the *Q* and *P*, and the precise Places of the *Q* and *P*, especially the former, is so difficult to obtain to that Exactness necessary to determine the Difference only of a few Minutes occasion'd our best Astronomers to recur to.

The 3d, which is by far more exquisite, i. e. by the Observations of the Parallax of *Q* (or *P*) discover'd by *Cassini*, and embrac'd and confirm'd by *Dela Hire*, *Flansteed*, and others, found the Parallax of  $25''$  of the *Q*  $10''$ , hence his Distance is about 81 Millions of Miles, and his Diameter 8 Miles.

IX. That this *Sun*, who is the Center of Gravity and Fountain of Light and Heat, revolves about his own Axis in the Space of 27 Days, appears from Spots; which have taken  $13\frac{1}{2}$  Days from the Time of their Appearing or Rising on the *East Limb*, to their Setting on the *West*, and after Setting, being hid, absconded in the opposite side of the *Sun*, for

Space of  $13\frac{1}{2}$  Days have again appear'd, and took same Course as before.

X. Since in *Summer* we are farther from the *Sun*, when *Winter* comes on, we begin to approach nearer to him, is it not a Wonder then c that the Earth grows warmer, while it is still further removing from the *Sun*, and again in the *Winter*, why it should be colder notwithstanding its nearer Access to him.

L B. The Degrees of Heat and Cold depend not altogether upon the Distance from the *Sun*, but there are other powerful and concurring Causes, as the direct force of the  $\odot$ 's Rays in Summer is much Stronger than when they are received Obliquely in *Winter*, moreover there are much fewer Rays, which render Light not so dense, nor the Heat intense, as in Fig. 4. Plate I. A represent the  $\odot$ , DICK &c. Parallel Rays of Light issuing from the  $\odot$ . Let L M represent some Space on the Earth's Surface, to which Place the  $\odot$  is Vertical, the Rays will be Perpendicular, and take up the Space C K. But let the  $\odot$  be removed from a Perpendicular Position, as suppose E F here, the same Quantity of Rays will take up the Space K b. but let the  $\odot$  be removed yet further from a Perpendicular Position as suppose G H, there the same Quantity of Rays will take up the Space K d, and consequently it must be colder in the Last, than in the Second, and in the Second than in the First.

Also the *Sun* being low, near, or in the Horizon all *Winter*, Beams pass thro' a much greater Quantity of Air, than in Summer, and the force of the Rays is broke by the Reflections of many Particles of Air, and this Difference is so very Great, when the  $\odot$  is in the Horizon, we can look upon him without hurting our Eyes, but when he rises higher there is no endurable Sight without blinding us.

To this add another powerful Cause, which is, that the long, hard and solid Body is exposed to the Fire, the hotter it is. Now in the *Summer*, for 16 Hours, we are continually exposed to the  $\odot$ 's Heat, we have only 8 Hours to cool; the Contrary, of which happens in the *Winter*, and therefore it can be no Wonder, that there should be so great a Difference of Heat and Cold in these two Seasons.

For why we should have the greatest Heat about the End of July, tho' the *Sun* has been leaving us above a Month, for the Action of the *Sun*, by which all Bodies are heated, is not transient, as its illumination is, but Permanent, so that a Body

## 184 The Chief Phænomena of the Sun.

dy once heated by the Sun, retains its Heat for some Time after the Sun have gone off it, but afterwards, when these heating Particles fly off, or lose their Force, the Body begins to cool, and therefore if the heating Particles, which are constantly receiv'd be more than they, which fly away, or lose their Power, the Heat of the Body must continually encrease. Thus after the Sun has entred the Tropic, the Number of Particles, which receive our Atmosphere does continually encrease, there entring more in the Day-time, than what we loose in the Night-time; and therefore our Heat must grow greater. But then as the Days decrease, and the Action of the Sun becomes weaker, both by cause of his shorter Stay, and the Obliquity of his Rays, there will at last be more Particles, that fly away in the Night-time, than what we receive in the Day-time, by which means the Heat of the Body will grow every Day less, and the Earth and Air, will by degrees cool.

### V. The Investigation of the Sun's Entring the Equinoxes.

In or near the Equinoxes, with a large and exact Instrument take the Meridian Altitude of the Sun, if it be equal to the Complement of the Latitude, the Sun is that Moment in the Equator, but if it is not equal, take the Difference, which will shew the Sun's Declination, then the next Day observe again the Meridian Altitude, and gather from thence his Declination, these two Declinations being of different Kinds, as one South, the other North: the Equinox happens sometime between the two observations, or if they be both of the same Sort, the Sun is either not entred the Equinoctial or has past it.

Now each Day having the Sun's Declination afore found, his Longitude answerable for the Day before, and the Duration of the Equinox, both which Longitudes add, and say as the Sum is to 24 Hours, so is the first found Longitude to the Number of Hours, and Minutes between the first Observation and the Moment of the Sun's Ingress to the Equinoctial.

### VI. The Phænomena of our Moon.

As the Earth by reflecting Light from the Sun illuminates the Earth, so the Earth does more than repay her Kindness by lightning the Surface of the Moon by the Sun's reflex Light, which she diffuses more abundantly upon the Moon, than the Moon does upon her; about 50 Times more, our Earth appearing to the Sun, 50 Times bigger than the Moon to us. In New

the illuminated Hemisphere of the Earth is fully turn'd towards the Moon, to illuminate the Moon's dark Hemisphere, and then the Lunarians will have a full Earth, as we in a similar position, have a full Moon, from whence arises that dim Light, which we see in the Obscure Part of the Old and New Moon; hereby, besides the bright and shining Horns, we can perceive the rest of her Body.

2. The Light of the Moon is so very weak, even in the Full, that the least Heat could never be perceiv'd from it, the Moon's Light has been computed to be no more than  $\frac{1}{8000}$  Part of the Suns Light, and if the Sun's Light be 7 Minutes coming to us, the Moon's will come in  $2^{11}.$  and  $49^{11}.$

3. The Moon may be observ'd in her highest Altitude, greater than the Sun's greatest, and in her west Altitude, lower than the Sun's lowest Meridian Altitude; because of her Latitude of above  $5^{\circ}$ , either North or South, and the Moon's Density is 7 times the Density of the Sun, also if the Sun's Diameter be 763,460 Miles, the Moons Diameter is but 75.

4. 'Tis Probable the Moon has no Atmosphere about her; For the Planets and Stars, which are sometimes even very near her Limb, have not their Light refracted, as it is when it passes thro' our Atmosphere; moreover, when there are no Clouds in our Air, the Moon constantly appears with the same Lustre. Hence we may suppose no Clouds nor Vapours in the Moon, which would obstruct some of its Regions from our sight, which we never observe them to do; yet some argue from the great Eclipse, April 1715, that it was an Atmosphere, because one might bear looking to the Sun, while the Eclipse was coming on, for the Rays came then by that Side of the Moon, on which the Sun had lately shone, and consequently had raised some Vapours there, which must needs weaken the Sun's

Sun's Rays ; but when the Moon was going from the Sun, then looking to the Sun was not tolerable, the Eye being dazled, but the Rays, which pass'd by the Side of the Moon, on which the Sun had not shone for near 15 Days, which made the Atmosphere very clear of Vapours.

*5. A S Y N O P S I S of the Motions of the Earth's SATELLITE, or Our MOON.*

Periodic Revolution about the Earth and about her Axis.

Synodical Revolu. { Earth in Perihelion  
Earth in Aphelion

Inclination of her Orbit.

Revolution of the Nodes, and Period of Eclipses.

But according to Whiston, for the mean Time of the Return of Eclipses.

Diurnal Motion in { Longitude.  
Anomaly.  
D's Apogeon.

If her mean Distance from Earth be.

Then her { Apogee Distance is.  
Perigeon.  
Eccentricity.

Less than our Earth Times.

Earth's Semidiameter. { at mean Dist. is.  
Moon's Semidiameter.

Horizontal Parallax in { Apogee.  
Mean Distan.  
Perigeon.

Apparent Semidiameter in { Apogee.  
Mean Distan.  
Perigeon.

D. H. l. 1.

{ 27. 7 43.

{ 29. 19.

{ 29. 7.

Deg. 5. 13.

Y. D.

{ 18. 224. 3.

{ 18. 11. 7. 43.

Deg. 13. 10. 3.

Deg. 13. 3. 5.

6. 4.

100. 00.

107. 07.

92. 93.

7. 07.

10. 7.

50. 17.

1. 65.

44.

1. 1.

52. 11.

56. 11.

61. 1.

II. 1.

14. 11.

15. 17.

16. 13.

T.

6. The Moon revolves continually from *West* to *East*,  
and this almost in the same Line with the Sun, which  
we call the Ecliptic.

Yet, this notwithstanding, it is not moved exactly in the  
same Line with the Sun, for sometimes it declines several De-  
grees more from the Equator, than the Ecliptic doth, and  
sometimes several Degrees less.

7. The Moon seems daily to put on a new Face,  
sometimes 'tis Invisible, and when it becomes Visible, it  
appears first Horned, then Biseected, then Gibbous,  
then Round, and then puts on the same Shapes again,  
but in an Inverse Order.

For that Half of the Moon's Body next the Sun is enlight-  
ened by him, whilst the other opposite Half is involv'd in Dark-  
ness, which is turn'd wholly to us in the new Moon, as the  
lightned Half is wholly facing us in full Moon, betwixt  
which we see more or less of the light Hemisphere, and accord-  
ingly she appears Gibbous, Biseected, or Horned.

8. 'Tis observ'd, that the Sun is Eclipsed, when the  
Moon is Invisible, and never else, and that the Moon  
itself is Eclipsed, but never else but when 'tis Round.

9. The Dark part of the Moon, both when 'tis Hor-  
ned, and when either it self, or the Sun is eclipsed,  
not wholly Invisible, but yields a certain dim, dis-  
tinct, and reddish Light, probably occasion'd by the  
reflected Light from our Earth aforesaid.

10. The Eclipses both of Sun and Moon, do not hap-  
pen every Year in the same Places of the Zodiac ;  
but in Places removed from the former gradually to-  
wards the Antecedent Signs.

Because the Nodes go backward every Year.

11. The apparent Diameter of the Moon is not al-  
ways the same, but Greater and Less by turns, and this  
B b 2 with

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with a Difference very sensible, according to her different Distances from us.

12. The apparent Motion of the Moon, is not always equal, but Greater and Less by turns, and likewise with a Difference very sensible.

Because of the Elliptic Figure of her Orbit, and Change its Eccentricity.

13. The Moon's Daily Motion is swiftest (*Celeris paribus*) in the Conjunctions with, and Opposition to the Sun, and slowest in the Quadratures.

Because the Eccentricity is absolutely the greatest in the Conjunction of the Apsides.

14. The Place where the Moon appears the least, and its Motion the slowest, is not always found in the same Degree of the Ecliptic, but removes in the Consequent Signs.

Because the Apsides advance towards the Consequent Signs.

15. The Latitude of the Moon is mutable, sometimes Greater, sometimes Less in the same Degree of its own Longitude, according to its various Situation with respect to the Sun.

This Inequality of the Inclination of Moon's Orbit, is owing to the Regress of the Nodes.

16. The Orbit of the Moon, sometimes approaching in some Measure unto the Circular Figure, other while again recedes from the same, according to divers Situation with respect to the Sun.

Because of the Change of its Eccentricity.

17. The Motion of the Moon is very unequal, no is it like to it self, whether we compare divers Part

the same Month, or the like Parts of divers Months.

And truly no Wonder, because of the various Changes of eccentricity, Apogee, Aphelia, Nodes, true Velocities, Variations no way connected together among themselves.

18. The Moon is always found to pass betwixt the Earth, and the rest of the Stars, whether Fixed or erratic, nor has it ever been observed, that any Star iss'd betwixt the Earth, and the Moon.

The same Face of the Moon, is in general always turn'd to the Earth; yet are there various Librations of the same Face, some Parts are discovered, and hidden alternately.

The first Part is plain from its Diurnal Motion about its axis in the very same Space of Time, as is the Periodic Month; whereby as much of its Face is turn'd to us, as is turn'd away from us by the menstrual Motion *nearly*, which sometimes is greater, and sometimes Less, and we viewing it from the Focus of a variable Ellipse occasions those reciprocal Librations; to which add the Consideration of the Inclination of the Face of the Moon's Equator, to that of its Orbit.

### III. To find the Parallax of the Moon.

In an Eclipse of the Moon, observe when both Horns are in the same Vertical Circle, and then at that Moment, take the Altitudes of both Horns, the Difference of these two Altitudes being halved, and Added to the least, or Subtracted from the Greatest, it does give nearly the Visible Altitude of the Moon's center; but the true Altitude, is nearly equal to the Altitude of the Center of the Shadow at that Time. Now we know the Altitude of the Center of the Shadow; because we know the Place of the Sun in the Ecliptic, and its Depression under the Horizon, which is

## 190 To find the Parallax of the Moon.

is equal to the Altitude of the opposite Point of the Ecliptic, in which is the Center of the Shadow, and therefore we have the true Altitude of the Moon, and the apparent Altitude, whose Difference is the Parallax, which will therefore be known.

By the apparent and real Longitude of a Phenomenon, the Parallaxes may be investigated, the apparent Longitude is found by observing the Distance of a Phenomenon from two Fixed Stars, whose Longitudes and Latitudes are known, and the true Longitude is had by making the same Observations, when the Star is in the 90th Degree of the Ecliptic, where the apparent, and true Longitude coincide.

## C O R O L L A R Y.

Those who can attentively View the Wonderful Beautiful, and Admirably contrived Structure of our adjoyning Planet, with its Sea and Land, Mountains and Valleys, Day and Night, Summer and Winter, together with its Clouds and supposed Atmosphere, all in Correspondence to our Earth, which is every where full of intelligent Beings, its Inhabitants ; and yet shall peevishly deny, that it either now is, or ever was, or is to be in like manner inhabited by such intelligent Beings, and are resolv'd, it shall have no other Use, than to enlighten our Earth, and be peep'd at thro' our Telescopes, seem to me too Unphilosophical to be argued with.

IX. Th

## X. The Doctrine of ECLIPSES explained, and more fully consider'd than in Page 135. &c.

1. All Opake, and Dark Bodies, when exposed to the direct Light of the Sun cast a Shadow behind them, that is opposite the Line the Sun is in.

2. This Shadow is nothing, but the Loss, or Privation of Light in the Space opposite to the Sun, by reason the Sun's Rays intercepted by the Opake Body.

3. Since the Earth is an Opake Body, it must likewise cast a Shadow towards the space Opposite to the Sun, in which Space, the Moon should come, it must necessarily be darkned, and lose the Light, which it had before from the Sun.

4. Because the Earth is Spherical, the Figure of the Shadow would be Cylindrical; if the Earth and the Sun were of equal Diameters, or if the Earth were bigger than the Sun, the Shadow would have the Figure of a Cone, which had lost a Piece at Top or Vertex, and the farther it were extended would grow thicker and thicker.

5. In both these Cases, the Shadow would run out into infinite Space, without ever having an End, and then it would involve sometimes the other Planets  $\mathfrak{J}$ ,  $\mathfrak{V}$ , and  $\mathfrak{H}$  within it, when they come to be opposite to the Sun, and enter within that Space. But this is never observ'd, for then these Planets would be eclipsed.

6. Therefore the Sun must necessarily be greater than the Earth, whose Shadow must consequently be of a Conical Figure, and end in a Point before it reach any of the other Planets: The same Way of Reasoning may be applied to the Moon, which also has a Shadow of a Conical Figure, into which, when any Part of the Earth doth come, that Part is thereby depriv'd of Sun Beams, and to the Inhabitants thereof, the Sun appears eclipsed.

7. Besides the Shadow, which is deprived of all the Sun's Light there is a certain Space all round it, which is but a partial Shadow, and is called a Penumbra, for tho' all the Sun's Light does not illuminate it, there are for all that Rays coming from

from some part of the Sun, which do enter it, and render it  
cid, the rest of the Sun Beams being intercepted by the O  
Body, and the Parts of this Penumbra will have different  
grees of Illumination, according as they are nearer or further  
moved from the Shadow, the nearer the Shadow, so much  
Darker.

8. The Height of the Earth's Shadow, at a mean Distance  
214. 8 Semidiameters of the Earth, and the Height of the Moon's  
Shadow; but 59. 36 Semidiameters, being in Proportion to one  
other, as the Diameter of the Earth to the Diameter of the  
Moon i. e. as 100 to 28.

9. If the Distance of the Moon from the Earth, be greater  
than her mean Distance, which is about 60 Semidiameters of  
Earth, the Shadow of the Moon can't reach the Earth, in which  
there may be a central Eclipse of the Sun, but not a Total.  
For round the Moon, there will appear part of the Sun's Body  
in the form of a Luminous Circle, which like a bright shiny  
Ring of Gold, will embrace the Body of the Moon, this  
nomenon is call'd an Annular Eclipse of the Sun.

10. These Annular Eclipses happen when at  $\sigma$  of the Moon  
near her Apogee, and the Sun near his Perigee, then may  
the apparent Diameter of the Sun, a little exceed that of the Moon,  
and such an Appearance Clavius observ'd at Rome, on the  
Day of April 1567.

11. If in the Time of the Eclipse, the Moon's Anomaly  
less than 3, and more than 9 Signs, there can no where be  
total Eclipse of the Sun, for in all these Degrees of Anomaly  
the Distance of the Moon is greater than her mean Distance.

12. In total Eclipses of the Sun, when the visible Diameters  
of the Sun and Moon, are equal at visible  $\sigma$ , then no sooner  
Sun's Light shall shut on the East Side, but it emerges on the West  
Side, and if the Moon's apparent Diameter be greater than that  
of the Sun, then will the total Darkness continue some Minutes,  
never above 5 Minutes in any one place.

13. In Lunar Eclipses, if the Sum of the Moon's Latitudes  
and Semidiameter be  $\left\{ \begin{array}{l} \text{Greater than,} \\ \text{Equal to,} \\ \text{Less than,} \end{array} \right\}$  the Semidiameter  
the Earth's Shadow the Eclipse will be  
 $\left\{ \begin{array}{l} \text{Partial, or less than} \\ \text{Total, or equal to} \\ \text{Total with Continuance or above} \end{array} \right\}$  12 Digits.

The Moon is never properly obscured by the Shadow of Earth it self, but by the Earth's Atmosphere, because the Rays of Light, which pass thro' the Atmosphere next to the Earth enter the Atmosphere, and from thence go out again, whilst they pass out of the Earth into the Atmosphere, as they pass out of a rare Medium into a Grosser one, they must necessarily according to the known Laws of Refraction, incline from the Perpendicular Rays, and when they pass out of the Atmosphere into the Earth again, they must recede from the Perpendicular, but both in the one Case, and the other, they incline towards the same Part, or towards the Axis, (by reason of the Change of the Perpendicular) which double Refraction computed, it appears, that the Solar Rays, which pass near to the Surface of the Earth are so bent, that they meet together in a Point long before they reach the Distance of the Moon.

But then those Rays, which pass thro' the upper part of the Atmosphere, seeing they are subject to less Refraction, will so soon meet together in a Point, but they will have passed far beyond the Moon first, and thus it is, that the Eclipse of the Moon is caused, in which consequently the Moon is not wholly invisible, but only of darkish Hue, the Terminal Atmosphere bringing that kind of Obscurity whilst on one Hand it deadens, and wholly stops the greatest Part of the Solar Rays, and on the other tinges the rest with a dark and direful Color.

The middle Time of Eclipses, or the nearest Approximation of the Centers of the Sun and Moon is not the very Moment of the New or Full Moon; but a little before or after, according to the Moon's Latitude and Position of the Nodes. Consider, if the Sun were moved in the Ecliptic, in the mean while, that the Moon rested in her own Orbit, the middle Moment of Eclipses would be in a plane Perpendicular to the Ecliptic: Again if the Moon were moved in her Orbit, the Sun being unmoved in his Orbit, then the said Moment would be in a plane Perpendicular to the Lunar Orbit; but both the Sun and Moon be moved, and with unequal Velocity (as 13 to 1) then the middle Moment must partake of both Conditions, and consequently be in some Plane, which is interposed betwixt the two former, and that 13 Times nearer the Ecliptic than to the Perpendicular to the Lunar Orbit, than to the Perpendicular to the Solar Orbit or Ecliptic; but this Difference, the ingenious Flamsteed, has prudently removed, by his Table of

the Angle, made with the Ecliptic, by the Motion of the Moon from the Sun, which because it respects the moveable Centers of the Sun, and of the Earth's Shadow determines the Angle always greater, than the greatest Inclination of the Lunar Orbit to the Ecliptic.

17. The Difference betwixt Eclipses of the Sun and Moon in sundry Particulars follow. The Eclipse of the Moon has same Appearance to all the Spectators, at the same Instant; the Eclipse of the Sun may appear in one part of the Earth, totally obscured: in another, but in part on its North Side; in 3d, on its South Side; and in many other Places, no Eclipse at all; and all this at the same Moment of Time.

18. Hence Eclipses of the Moon, may be reduced to another Meridian, by allowing the Difference of Time after Calculation is ended; but an Eclipse of the Sun must be calculated for every different Meridian to obtain its true Appearance: wherefore, change the Time of the true Conjunction by the Tables into the Time proper to the other Meridian, by allowing its Difference, to which Time and Place, find Parallaxes &c. for the Parallax of the Moon differs in Climate, on which Parallax the visible Eclipse of the Sun principally depends.

19. In Lunar Eclipses, there being a true Loss of Light, no matter from what Place of the Earth it is seen, it will be the same, but in Solar Eclipses, there being no true Loss of Light in the Sun, and no more, than an Intercepting of Light, by the Moon coming between, it will necessarily be different; according to the different Position of the Observer: 'tis not the Sun, but part of the Earth, over which, the Moon's Shade passes, is in Darkness, and therefore some call it rather an Eclipse of the Earth.

20. The Calculation of a Solar Eclipse is much more difficult, than that of a Lunar; because in a Solar Eclipse, there is so great Difference betwixt the Parallaxes of Sun and Moon, according to their different Altitudes. nay during the whole Time of the Eclipse, they are changeable and perpetually varied, both in Longitude and Latitude. likewise from which Anomalies of Appearances we being free in Lunar Eclipses, the Calculation must needs be more easy and exact.

21. In Lunar Eclipses, the Moon enters the *West* part of the Shadow, with the *East* part of her Limb, and in the End, she leaves the *East* part of the Shadow, with the *West* part of her Limb; but in Solar Eclipses, the *East* Limb of the Moon will first cover the *West* Limb of the Sun, and the *West* Limb of the Moon, will last uncover the *East* of the Sun, the Sun's Eclipse belongs sooner to those that inhabit the *West* parts, and later to those more *Easterly*, because the Moon's proper Motion from *West* to *East*, is swifter than the Sun's, near 13 Times, and therefore it begins on the *West* Limb of the Sun, which Part is first restored to Light again, and if the Moon's visible Latitude be *North*, the *North* Part; but if *South*, the *South* Part of the Sun is unclouded, because the Moon intercepts the Light of the same Side of the Ecliptic the Moon appears,

22. There are, respecting the whole Earth, more Eclipses of the Sun than of the Moon; but in respect of any one given place of the Earth, there are much fewer visible Eclipses of the Sun, than the Moon, for the Shade of the Moon, is less than the Shade of the Earth, and consequently the Former will not so often involve any given Place of the Earth, as the latter will some part of the Moon: The Moon oftner takes away the whole Sun from the Earth, than the Earth takes away the whole Sun from the Moon; the Body of the Earth being larger, receives more benefits of the Moon's Shadow, than the Moon of the Earth's Shadow, and because the Sum of the Semidiameters of the Moon, and the Earth is never less than 54 min. and the Semidiameters of the Sun and Moon, never greater than 34 Min. the Eclipse of the Moon may happen in a greater Latitude of the Moon, than the Sun, and in respect of one, and the same Place upon the Earth, the Eclipses of the Moon will be more frequent, tho' in respect of the whole Earth, Solar Eclipses may exceed in number.

23. Because for many Days together, the Sun's Place is once every Year, but a little distant from either Node, during which time, there generally happen two Syzygies, in which the Sun will both hide the Moon from us, and the Earth will hide the Sun from it, hence generally there are 4 Eclipses, which are greater, the nearer any New or Full Moon, happens to the Nodes. In a Year there seldom happens less than two or more, than 6 Eclipses, and when two they are always of the Sun; one before his Apogee, and the other after.

24. Sometimes the Sun may be eclipsed more than 12 Days, and the Moon above 22, the Sun is seldom totally eclipsed in one Place, the Moon often, and the greatest Shadow of the Moon, is not above 200 Miles, being the greatest Difference of Diameters of the Sun and Moon, which according to the Liquity of Horizons may be greater or less.

25. For the best, and exactest Method of calculating Eclipses, See Doctor *Gregory's Astronomy*, Book 4. Sect. 7, 8. *Famsteed's Doctrine of the Sphere*, at the End of Sir *Jonas Moor's System of the Mathematicks*, also *Keil's Introduction to Astronomy*, Lect. 13, 14. or Lastly *Whiston's Astronomical Lectures*, which *Famsteed's Tables* for Calculation.

26. Eclipses are not more frequent nor dismal in our Time than in Ages past, for where no Change is in Causes, there necessarily no Change in Effects, nor in them is any thing monstrous or Preternatural: being no more than the necessary Result of the Motions of the Sun and Moon.

27. Solar Eclipses are very different each from other, notably because of the unequal, and uncertain Motion of the Moon, both true and apparent, the greater or lesser visible Latitude of the Moon's Distance from the Sun, and unequal Distances of both the Luminaries from the Earth: Hence the Eclipse may happen pretty near the same Time and Place; yet will not for the above Reasons, be of the same Quantity, Duration; for this Rule is certain "The Heavenly Motions are Incommensurable among themselves, nor have the Phænomena in every Respect return'd alike in any Place."

28. Eclipses are of manifold Uses in sundry Branches of Mathematicks, as Astronomy, Geography, Chronology, and Navigation, to correct their Tables, Maps, Globes, Account of Time, and contribute very much to the Discovery of Longitude, both by Sea and Land; by the Wings of Eclipses, and Parallaxes, the Mind of Man flies up, and penetrates into the Celestial Regions.

## K. To Observe the ECLIPSE of the SUN, without Hurting the Eyes.

Some simply prick a very small Hole with a fine Needle, in Sheet of Paper: Others use a Looking-Glass, but a better way with colour'd or smoak'd Glass, which defends the Eye from the Beams of the Sun, or by a Burning-Glass, reflecting it on clean Sheet of Paper, held twice as far from the Paper as the Burning.

### *Here follows an easy and cheap ASTRONOMICAL APPARATUS, for Observing ECLIPSES.*

Prepare a Sheet of Paper, whereon draw a Circle about 6 inches Diameter, divide its Circumference into 360 equal Parts and its Diameter by 6 Concentric Circles into 12 equal Parts, for show the Digits, and another Diameter for Decimal Parts up to an 100, whereby the Proportion of the Light and Dark Parts to each other, may be known: the 360 on the Limb may serve to determin the Inclination of the Cusps of the shade, this paste on a Board, which affix to a Telescope, so as to be Perpendicular to its Axis, and at such a Distance, that the Image of the Sun may exactly fill the outmost Circle of 360.

Then rule a Paper like a Surveyor's Field-book in 9 or 10 Columns for the Uses mentioned in each Column.

### Observations

Observations Common to the Eye,  
as

Appearances of the Sky.  
Color of the Eclipse.  
Stars seen.  
Candles lighted.  
Birds flying to their Nests.

Number of Observations.

Digits, and Parts.

Time by Pendulum.

Time by Sun-Dial.

Sun's Altitudes.

Time Corrected.

Astronomical Observations, As

Sun's Azimuth.  
Inclinati. of the Cui.  
Semidiameter of the whether.  
Bigger or Less, than  
Sun's Semidiamet.  
Whether encreases, or  
decreases.  
Whether the Moon  
an Atmosphere, es-  
cially to be obser-  
in total Eclipses  
the Sun, by red streaks  
of Light just before  
and after, the said  
total Darknes.  
How long such are  
able.

Angle at the Sun when Stationary  
to Retrograde.

66

53½

22½

15

32

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Being thus furnish'd, get a Room well darkn'd, and let no Light into it any where, but thro' the Telescope, which sometime before the Eclipse begins, on a Surveying Instrument, or the like with a Ball and Socket ; that it may move higher or lower, or to any Point of the Compass to suit the Sun's Altitude and Azimuth, then appoint one to attend the Commencement of the Shade, its Progress Increase and Decrease, both Digits and Decimal Parts ; let another watch the Time by the Pendulum, Watch, or Clock : a third mind the Sun Dial by Hours and Minutes : a Fourth mind the Sun's Altitude by a large Quadrant, or by a Gnomon, and End of its Shadow, whether Wall or Stake, all which Accounts, register in their proper Columns, principally noting not only the Beginning and End of the Eclipse, but also of total Darkness, when also each Digit is eclipsed, and Angle of Incidence, if the Air be clear, and will permit.

I. A TABLE Of the STATIONS of the  
PLANETS.

Angle at the Sun when Stationary to Retrograde.	Days Retrograde.	Angle at the Sun, when stationary to Direction.	Degrees Retrograde.	Elongation of the Sun, when be- ginning to be Retrograde.	Greatest Distance of the Sun in Op- position.	Elongation of the Sun, when be- ginning to be Direct.	Angle at ☽ of ♀ & ♂, when in ♂ to the Sun.	Angle at the Sun of ♀ & ♂, when in ♂ with Sun.
66	140	66	7	108	180	108	180	0
53½	120	53½	10	116	180	116	180	0
22½	80	22½	20 15 10	135	180	135	180	0
15	44	15	18	28	48	28	180 ♂ Sun when Retrogra.	0. ♂ ☽ when Di- rect.
32	24	32	16 8½	22	28	22	180 ♂ Sun when Retrogra.	0. ♂ ☽ when Di- rect.

The middle Direction happens in the ♂ with the Sun, and the Stations in or about the Octants: the middle Retrogradations in the Oppositions, and that they always fall thus, and never at other Times, is a thing that neither is nor can be denied.

Fromondus, one who was averse enough to the Annual Motion of the Earth, saith, *The Annual Motion of the Earth is maintained by the Copernicans by no Argument more Probable and Specious*

Specious, than that of the Station, Direction, and Retrogradation of the Planets. For 'tis plain if the Spectator remain unmoved, tho' of the Center, and thereby equal Motions may appear unequal; yet the Object can never be seen to go backward, or stand still, unless the Place of the Spectator is likewise moved.

Because the Retrogradations of the Planets, are not real themselves; but only appear so to us at the Earth, caused by the Earth's Motion; therefore by Reason of the various Positions of the Earth at different Times there cannot be any certain universal and perpetual Rule given in Numbers: yet the foregoing Table will be serviceable, of which the Title of its Column is a sufficient Explanation.

Finally, Tho' the Planets by their proper Motion advance from West to East; yet sometimes they seem to tend the contrary Way, from East to West; before which Change they seem to rest a while, tarrying some Days in the same place, their Motion is very unequal, their swiftest Progress when in Conjunction with the Sun: and their swiftest Regress, when in Opposition, at which Time their apparent Magnitudes considerably increase, especially in Mars and Jupiter. Tho' all these Planets are to be found in the Bounds of the Zodiac, yet seldom are they in the Ecliptic Line it self; but decline North and South from it; which Latitude or Deviation, is different amongst them all; and tho' the Places wherein these Planets cut the Ecliptic, continue the same, with respect to the Fixed Stars, yet they go forwards continually in the Signs of the Zodiac. Also the places, where their true Motion is slowest or swiftest, continue the same with reference to the Fixed Stars; but as to the Ecliptic, they seem to be transfer'd in consequentia. Also the Superior Planets i. e. *Saturn, Jupiter, Mars*, may form to us all Aspects with the Sun, yet the Inferior *Venus* and *Mercury* form not so much as a Sextile; none but a Conjunction, which is either in the upper or opposite Part of their Orbits, and sometimes tho' seldom, both *Venus* and *Mercury* may be interposed between the Sun and Earth in the form of Spots upon the Discus or Body of the Sun, as aforesaid.

### III. A Synopsis of the Satellites, or Moons of Saturn, and Jupiter.

Names.	Distance from him	Periodical Revolu.	Magni.
SATURN'S. , and next Satel.	English Miles.	D. H. I. II.	
1	146 000	1 21 18 26 $\frac{1}{2}$	
2	187 000	2 17 41 10 $\frac{1}{2}$	
3	263 000	4 12 25 10	
4	600 000	15 22 41 28	
5 and outmost.	I. 800 000	79 7 46 0	
JUPITER's , and next Satel.			
1	300 000	1 18 28 36	2
2	364 000	3 13 17 54	3
3	580 000	7 3 59 36	1
4 and outmost:	I. 000 000	16 18 5 12	4

\* This 4th Satellite may have Latitude, so as to free it from falling into Jupiter's Shadow, as in the Year 1684, October, November, and December, else every Satellite in one Revolution, twice hid from us; besides when it falls into Jupiter's Shadow, First, when in Conjunction with Jupiter, 'tis as a Spot between us and Jupiter. Secondly, when Diametrically opposite Jupiter's Body may interpose and Eclipse it, tho' the Shadow of Jupiter be intirely free from it.

### XIII. The Phænomena of the Satellite Moons or Attendants of Saturn and Jupiter.

1. These Secondary Planets fall short of their Principals in respect of Magnitude ; that before the Use of Telescopes, which was not until the last Age, they were wholly unseen and unknown.

2. They do not always offer themselves to the Sight of him that looks thro a Telescope ; but do sometimes wholly lie hid.

Because they may be eclipsed by their Principals, or one another, or may be in the Shadow of their Principals, or when between us and their Principals will appear as a Spot hard to be distinguished ; such Eclipses happen to them after the same Manner as they do to our Moon.

3. These Moons in general are each of them on both Sides its Principal, that is, are so successive sometimes on the Right, sometimes on the Left.

Because they revolve about their Principals.

4. They are continually changing their apparent Distances from their Principals, and wander from them several Ways.

For the Reason mentioned in the last.

5. Every one of them hath its certain proper Limits of Excursion, which it never goes beyond, and which are also altogether different from the Limits of other Planets of its kind.

Which shows the Diversity of the Curvilinear Paths, wherein they severally circulate about their Primary ones.

6. These small Planets in their Motion go by turns the contrary Way, to that which their Principals go; they seeming to us sometimes to tend from *West* to *East*, and sometimes again from *East* to *West*.

Which they must needs do to us, who view them far without the Compass of their Orbits, whereas to an Eye placed in their Primary's, they would both in Truth and Appearance resolve perpetually towards the same part of Heaven.

7. Their Periodical Times, in which they return to the same Place in respect of their Principals, are the longer, when the Limits of their Excursions are the larger, and their greatest Elongation is greater than that of others.

This holds in both Primary and Secondary Planets, without exception, that which is more remote from the Center of Motion, takes up a longer Space of Time in its Revolution.

8. They are often seen not only without the Plane of the Ecliptic ; but also without the Annual Planes of their Principals, and declining from both a little, either to the *North* or *South*.

Even as Primary ones do in like manner.

9. Yet, this notwithstanding, the Circum-Jovials appear amongst themselves in almost the same Plane, which also is proper to them, and the Circum-Saturnials, likewise have a peculiar Plane, in which they almost all of them are.

10. The greatest Elongation of every Secondary from its Primary, remains always almost the same

nor are these little Planets Subject to any considerable Variation in this Respect.

These Harmonical Motions and Positions are wholly to be ascribed to the Wisdom, and Pleasure of the great C R E A T O R.

11. Each of the two outmost Primary Planets have a good Company of Attendants, for *Jupiter* keeps no fewer than Four constantly by him, and *Saturn* Five in his Retinue, which is a Sight no less Wonderful, than Delightful; these Satellites, like our Moon, do always accompany their primary Planets in their Circuits round the Sun, and in the mean Time their proper Circulations about their Primaries, and therefore they will have the same Phases and Figures, that our Moon shows us: When they are in Opposition to the Sun they appear to *Saturn* and *Jupiter* bright and full, from thence receding they assume a Gibbous Shape, when they come to a quadrat Aspect, they look like Half-Moon's: Before, and soon after the Conjunction, they show themselves in horned Figures, and when they come to be joyned in the same Line with the Sun, they totally disappear.

12. These Satellites seen from the Earth, tho' they go at the furthest, but a little way from their Primaries: yet sometimes they approach them nearer, and sometimes remove a little further from them. *Plate 7. Fig. 7.* Let A B T be the Orbit of the Earth, in the Middle of which the Sun's resides. Let E F be a Portion of the Orb of *Jupiter*, in which Let *Jupiter* be in ♂, who keeps in the Middle of the Orbits of his four Attendants, these Satellites or Moons, when they describe the inferior Parts of their Orbits L M N seen from the Earth or Sun, will appear to have a Motion *Westward*; but while they are moving thro' the superior Portions

tions G H K, we observe them to move *Eastward*, according to their true Motions. Now when their visible Motion is *Eastward*, they are twice hid from us, once in O behind the Body of *Jupiter* that is, in the right Line which joyns the Centers of the Earth and *Jupiter*, and again they vanish, and become invisible, when they fall into the Shadow of *Jupiter*, or are in the right Line, which joyns the Centers of the Sun and *Jupiter*, and then they suffer Eclipses, which are always when they are at their Full, as seen from *Jupiter*. These Eclipses happening in the same manner as they do to our Moon, by the Interposition of the Earth between the Sun and it.

13. When *Jupiter* is to the *East* of the Sun, and is seen in the Evening after Sun-Setting, that is, when the Earth is in A, they are first hid behind *Jupiter*; because of their visible Conjunction with *Jupiter* before they fall into his Shadow, and their Second Disappearing is in the Eclipse upon the entring the Shadow. But when *Jupiter* is more *Westerly* than the Sun as he appears after Conjunction, when he is only seen in the Morning, that is, when the Earth is about B, then they fall into *Jupiter's* Shadow at C, and are eclipsed before they are hid behind his Body in P. But when these Moon's have a Retrograde Motion, that is, when they are seen to go *Westward*, and describe the inferior Parts of their Orbits, then they only once disappear in Q when they cannot be distinguish'd from the Body of *Jupiter*; but when the Satellites seen from the Sun, are in their inferior Conjunction with *Jupiter*, or as seen from *Jupiter*, they are in Conjunction with the Sun, their shadows will fall upon *Jupiter*, and some Part of the Disk of *Jupiter* will be in an Eclipse, and a spectator within the Shadow would observe a total Eclipse of the Sun.

14. By

14. By the Motions and Eclipses of these Moons the Parallax of the Annual Orb in *Jupiter*, and his Distance from the Sun may be easily known; for let P O R be the Orbit of any Satellite, for Example the outmost, and suppose the Earth in the Point of its Orbit A, the Time must be observ'd when the Satellite lies hid behind *Jupiter's* Body in O. For which Purpose, the Moment of Time must be carefully mark'd when he first disappears, and then also the Moment he becomes again Visible, the middle Moment between these two is the Time, when the Satellite is in O, or in the Line which passes thro' the Earth and *Jupiter*, after the same manner observe when the Satellite is in the Middle of an Eclipse, or in the Middle of *Jupiter's* Shadow, that is, when it is in V, by this means we shall have the Time it takes to describe the Arch O V, and because his Motion about *Jupiter* is equable, and his Periodical Time known, we can thence find out the Arch O V, for this Planet revolves about *Jupiter* in 402 Hours. Let us suppose the Time he takes to move from O to V be 12 Hours, say as 402 : 12 so are 360 to a Quantity, which will be found to be  $10^{\circ} 44'$ , and therefore the Arch O V is  $10^{\circ} 44'$ ; But this Arch is the Measure of the Angle A  $\nparallel$  V, or of the Angle, which is equal to it A  $\nparallel$  S, and the Arch which measures this Angle is the Parallax of the Annual Orb, which therefore is known.

15. In the Triangle A  $\nparallel$  S, we have the Angle at  $\nparallel$ , and also the Angle at A, the Elongation of *Jupiter* from the Sun, which may be had either by a Calculation from Astronomical Tables, or by Observation, besides we have the side A S, the Distance of the Earth from the Sun, which we assume to

consist of 100,000 Parts. Since therefore in this Triangle, we have all the Angles, and one Side by Trigonometry, we shall find the other Sides, and particularly  $S\pi$ , the Distance of Jupiter from the Sun, so likewise we may find  $A\pi$ , the Distance of Jupiter from the Earth, which is always variable, but to do this nicely, there should be repeated Observations with the best Telescopes, and Time-keepers.

16. By the Eclipse of Jupiter's Moon's, we are able to give a Solution of a Problem, which is the most Noble and Curious in Natural Philosophy, and which cannot but raise our Wonder and Amazement, that

Whether Light be propagated to us in an Instant, or if its Motion be successive; and if it takes some Time to arrive from the Sun, or any distant Object to us. Now these Eclipses do shew us, that there is no instantaneous Motion in Light, tho' it comes from the Heavens to us with a prodigious quick Motion, and incredible Celerity.

For if the Motion of Light were in an Instant, when the Earth at T at its greatest Distance from Jupiter, an Astronomer here would observe an Eclipse of a Satellite at the same Moment of Time, he would do, were the Earth at X, at her nearer Distance to Jupiter, for according to this Hypothesis, Light is propagated in the same Distance thro' all Spaces indefinitely, whether near or never so much remote. But if Light takes up any Time for its Propagation thro' Space it will sooner pass thro' a shorter Space, than Greater, and therefore an Observator at X being nearer to Jupiter, than one at T, by the Distance  $X T$ , which is about equal to the Diameter of the Earth's Orbit,

Orbit, will sooner observe the Eclipse of a Satellite than a Spectator can do at T, and therefore from the Difference of those Times, which is proportionable to  $X T$ , the Difference of Distances, we can collect the Velocity of Light; and so this Matter is in Reality: For whenever the Earth is at its nearest Distance from Jupiter the Eclipses are found to happen sooner than they do, when they are observ'd from T at a greater Distance, where they fall out sensibly later than they ought to be, according to our Astronomical Computations: these quicker and flower returns of Eclipses having been observ'd for many Years, by the Sagacious Romer with much Art and Diligence: upon them he founded this Argument for demonstrating the successiv Propagation of Light, and by them he proved the Light, like all other Bodies in Motion, had a determin'd Degree of Velocity, and took a determin'd Time to move thro' a given Space; to which Opinion the greatest Part of Astronomers do now give their Assent.

\* The Particles therefore of Light, tho' their Minuteness be indefinite, and not easily to be imagined: yet they have a progressive rectilinear Motion, and are not diffused, as by the Waves of any Medium, or Fluid. Romer determines the Velocity of Light to be such, that it reaches us here from the Sun in the Space of 11 Minutes, (others since, only 7 Minutes) but that Distance does not seem to be less than 50 Millions of Miles; which Space, Light passes thro' in so small a Time; that so prodigious a Velocity cannot easily be conceived by us, which so much exceeds the Velocity of the swiftest Bodies we know: for tho' the Earth has a very quick Motion round the Sun; yet its Velocity compared with the Velocity of Light is no more than that of a Snail in Comparison of the Swiftnes of the Earth.

## XIV. The Phænomena of Saturn's-Ring, One of the greatest Wonders of Our SOLAR SYSTEM.

1. The Body of *Saturn* it self separate from this Ring is plainly Sphærical, and can yield us nothing of these Phænomena.
2. This Singularity of *Saturn's* Ring would induce any to exempt this Planet from a Diurnal Motion; which some have given it in about a Month's Time.
3. The Ring is about so far distant from the Body of *Saturn*, as it self is broad, and the Diameter of *Saturn* is about 68000, Miles and is in Proportion to the Diameter of his Ring, as 4 to 9. Hence the Interval which is betwixt the Ring, and the Body of *Saturn*, to which the Breadth of the Ring is nearly equal, ariseth to about 21,000 Miles. *A strange and extraordinary phenomenon!*
4. Both the Surfaces of the Ring are somewhat pale, like Fluids, or those Bodies, which, tho' now hardened, have sometimes been in a state of Fluidity, as Glafs, Ice; not unlike those Regions of the Moon, which some call Seas.
5. The Thickness of this Ring is so small, that it runs the Notice of our Astronomers; for when the pale of the Ring passes thro' our Eye, it can scarce be seen, leaving nothing but a small Line, or Stroke of a Shadow passing over the Body of *Saturn*.

E e

6. Altho'

6. Altho' the broad Surfaces of the Ring reflect Light strongly and copiously enough; yet the exterior Surface thereof, that of the Edge reflects little or no Light, but a Shade only, tho' of what Matter it consists, we cannot yet conjecture.

7. As we know not yet, whether it be Solid or Fluid: neither, till we discover some Spots in it, or we discover its circular Motion; if Solid.

8. The Plane of the Ring is inclined to the Plane of the Ecliptic, in an Angle of about 31 Degrees and its Nodes, or Intersections with the Ecliptic in this Age, about the Middle of the 21<sup>st</sup> Degree of *Pisces* and *Virgo*.

9. Seeing the Figure of this Ring is altogether Circular, there will be no Apsides; consequently no Progression of the same.

10. The Inclination of the Plane of the Ring to the Plane of the Ecliptic is in the Space of one Revolution of *Saturn* about the Sun, twice the greatest of all, and as often the least, and its Axis consequently in the Compass of one Annual Revolution twice inclines it self to that Plane, and twice returns to its former Position; as the like happens to the Moon and Earth.

11. Hence *Saturn* appears Solitary, and without this Ring, as often as he is found about the Nodes of the Ring; having only a small Track of a Shadow crossing his Body, as aforesaid, as in the Year 1701.

12. The like Appearance must happen, when the Position of the Earth and Sun, is such, that the Plane of the Ring protracted would pass betwixt them; for at that Time only the obscure Surface of the Ring is exposed to the Eye of the Observer.

13. This Circular Ring must put on an Elliptic Form; but so much the less Elliptic, by how much further *Saturn* is distant from the Line of the Nodes; for a Circle, unless the Eye be in its Axis, degenerates into an Ellipsis, whose greater Axis will be equal to the Diameter of the Circle; but the less Axis will be equal to the right sine of the Elevation doubled e. of the Eye above the Plane of the Ring; which being given, the Species of the Ellipsis, which will appear upon the Earth, will also be given and contra.

14. The various Phases of the Ring in each Resolution of *Saturn* about the Sun, return again in Round, and certain Likeness of Phases, proceeding from divers Surfaces of the Ring, return in Half the Circuit, or within the Space of 15 Years.

15. The Ring begins first to be seen, when the Sun is elevated almost 4 Degrees above the Plane hereof, that is, when *Saturn*'s Heliocentric Place is distant about 7 or 8 Degrees from the next Node, before and after it is in it; which Interval of 15 Degrees, *Saturn* moves thro' in the Space of 15 Months; during which Space *Saturn* will be so long seen without his Ring.

16. The Disappearance of the Ring is sometimes owing wholly and singly to the Position of the Earth, which may be such, that only the outer Surface of the Ring can be seen the Inhabitants of the Earth can no more see the Ring; than it was not illustrated at all, nor will it happen otherwise when the Plane of the Earth is found in the very Plane of the Ring produced, or elevated only little above it.

## XV. Of the Transits of Venus and Mercury over the Sun's Disk.

Table of the Moments of Time, when V E N U S will be so closely in Conjunction with the S U N, as to be seen within its D I S K for 1000 Years, with that Planets Distances from the S U N's Center at the same Moments.

In the Month of November.

Year	Time of Conjunct.			Dist.fromCenter of ☽:		
	D.	H.	I.	I.	II.	
918	20	21	53	6	12	B
1161	20	21	40	6	55 $\frac{1}{2}$	A
1396	23	7	20	4	38	B
1631	26	17	29	16	11	B
1639	24	6	37	8	30	A
1874	26	16	46	3	3	B
2109	29	2	56	14	36	R
2117	26	16	3	10	5	A

In the Month of May.

Year	Time of Conjunct.			Dist.fromCenter of ☽:		
	D.	H.	I.	I.	II.	
1048	24	13	45	3	50	B
1283	23	8	14	5	31	A
1291	25	15	9	14	27	B
1518	25	16	32	14	52	A
1526	23	9	37	5	6	B
1761	25	17	55	4	15	A
1769	23	11	00	15	43	B
1996	28	2	13	13	36	A
2004	25	19	18	6	22	B

The

# The like for MERCURY.

In the Month of April.

Year	Time of Conjunction.			Dist. from Center of O.			
	D.	H.	L.	I.	II.		
1619	22	21	38	**	7	20	B
1628	23	5	15	*	9	25	A
1661	23	4	32	*	4	27	B
1674	26	12	29		12	28	A
1707	24	12	6		1	34	B
1720	26	19	43	*	15	21	A
1740	21	11	43		15	36	B
1753	24	19	20	*	1	19	A
1786	22	18	57	*	12	43	B
1799	26	1	34		4	11	A

In the Month of October.

Year	Time of Conjunction.			Dist. from Center of O.			
	D.	H.	L.	I.	II.		
1605	22	8	29		12	48	A
1618	25	2	3	*	4	45	A
1631	27	19	37	*	3	18	B
1644	30	13	11		11	21	B
1651	23	13	20		11	26	A
1664	25	6	54	*	3	23	A
1677	28	0	28	**	4	40	B
1690	30	18	2		12	43	B
1697	23	18	11	*	10	4	A
1710	26	11	45		2	1	A
1723	29	5	19	*	5	1	B
1730	22	5	28		26	45	A
1736	30	22	53	**	13	5	B
1743	24	23	2	**	8	42	A
1756	26	16	36		0	39	A
1769	29	10	10		7	24	B
1776	22	10	19		15	23	A
1782 Nov.	1	3	44	*	15	27	B
1789	25	3	53	*	7	20	A

Those Transits noted with one \* are in part Visible  
London, and those that have Two, are wholly

At the End of 8 Years, VENUS is revolv'd to the  
n, if there be taken away from the Moment of the for-  
r Transit 2 Days, 10 Hours, 52 Minutes, and 30  
conds. But it moves then in a Path, which inclines  
re to the South, than the Former, by 24 Minutes, 45  
conds.

At the End of 235 Years, if there be added 2 Days,  
Hours, and 9 Minutes, VENUS will again enter  
Sun; but in a way more Northerly, by 11 Minutes  
Seconds: But if the foregoing Year be Bissextile,  
we are to be added 3 Days, 10 Hours, and 9 Mi-  
tes.

At the End of 243 Years, VENUS passeth over the  
n again, only there are 43 Minutes to be taken away  
in the Time of the Former; but she goeth more South 13  
minutes, 8 Seconds: But if the preceding Year were  
Bissextile, add 23 Hours 17 Minutes, to wit, the Com-  
mencement of the Ablatitious Time unto a whole Day, and  
all these Appulses to the Sun in the Month of Novem-  
ber, the Angle of the visible Way with the Ecliptic is 9  
degrees, 5 Minutes, and VENUS's Horary Motion with-  
the Sun, 4 Minutes, 7 Seconds, wherefore seeing the  
n's Semidiameter is 16 Minutes, 21 Seconds, the  
reatest Duration of the Transits of VENUS will be 7  
hours, 56 Minutes.

**XVI.** Having the Year of the Cycle of the Sun, Moon, and Indiction. To find the Year of the Julian Period.

Multiply 4845, by the Cycle of the Sun, and 4200 by the Cycle of the Moon, also 6916, by the Year of Indiction given.

Divide the Sum of these Products, by 7980, neglecting the Quotient, the Remainder will be the Year of the Julian Period required.

**E X A M P L E**

In the Year 1719, Cycle of the Sun was 19, of the Moon 9, and of the Indiction 11 the First Product i. e. 4845, by 19 = 92055, the Second, i. e. 4200 by 9 = 37800, and the Third, 6916, by 11 = 76076 the Sum of these Products, is = 205931; which being Divided by 7980, will have a Remainder of 643 Years, the Year of the J U L I A N P E R I O D sought.

**XVII.**

## CONCERNING

**C O M E T S.****S E C T. XVII.**

1. **B**ESIDES the Planets already mentioned, there are other great Bodies that sometimes visit our System; which are a sort of Temporary Planets; for they come and abide with us for a while, and afterwards withdraw from us, for a certain space of Time, after which they again return. These wandering Bodies are called Comets.

2. The Motion of Comets in the Heavens Of Comets according to the best Observations hitherto made, seem to be regulated by the same immutable Law that rules the Planets; for their Orbits are Elliptical, like those of the Planets, but vastly narrower, or more Eccentric. Yet they have not all the same Direction with the Planets, who move from West to East, for some of the Comets move from East to West; and their Orbits have different Inclinations to the Earth's Orbit; some inclining Northwardly, others Southwardly, much more than any of the Planetary Orbits do.

3. Altho' both the Comets and the Planets move in Elliptic Orbits, yet their Motions seem to be vastly different; for the Eccentricities of the Planets Orbits are so small, that they differ but little from Circles; but the Eccentricities of the Comets are so very great, that the Motions of some of them seem to be almost in right Lines, tending directly towards the Sun.

F f

4. Now

4. Now, since the Orbits of the Comets are so extremely Eccentric, their Motions when they are in their *Perihelion*, or nearest Distance from the Sun, must be much swifter than when they are in their *Aphelion*, or farthest Distance from him; which is the Reason why the Comets make so short a Stay in our System; and when they disappear, are so long in returning.

5. The Figures of the Comets are observed to be very different; some of them send forth small Beams like Hair every way round them; others are seen with a long fiery Tail, which is always opposite to the Sun. Their Magnitudes are also very different, but in what Proportion they exceed each other, is as yet uncertain. It is not probable, that their Numbers are yet known, for they have not been observed with due Care, nor their Theories discovered, but of late Years. The Antients were divided in their Opinions concerning them; some imagined that they were only a kind of Meteors kindled in our Atmosphere, and were there again dissipated; others took them to be some ominous Prodigies. But modern Discoveries prove, that they are Worlds subject to the same Laws of Motion, as the Planets are; and they must be very hard and durable Bodies, else they could not bear the vast Heat, which some of them, when they are in their *Perihelia*, receive from the Sun, without being utterly consumed. The great Comet which appear'd in the Year 1680, was within  $\frac{1}{2}$  part of the Sun's Diameter from his Surface; and therefore its Heat must be prodigiously intense beyond Imagination. And when it is at its greatest Distance from the Sun, the Cold must be as rigid.

**XVIII. Of the Number of the COMETS.**

Within these 4 last Centuries have appear'd to us but 24 Comets, of these Doctor Halle supposes 3 of them, who have had their Orbits and Appearances so very like, and the Times of their Appearing so very equal to be in reality; but one and the same Comet, appearing at 3 several Times, and the like we may suppose of some others. That great Comet, that appear'd in 1680, 1681, was seen before in 1106, once before about 532, and also 44 Years before our SAVIOUR's Birth, and therefore they conclude the Time of its Periodic Revolution round the Sun, to be 575 Years. The Time of the Revolution of another Comet, which Astronomers suppose will appear again in 1758, is 75 Years, another which probably may be seen here again in 1789, makes its Ellipsis round the Sun in 129 Years. The Orbits of these 3 are described in *Plate 9.*

**XIX. To find whether a COMET has a sensible Parallax.**

Its Parallax is that Angle, under which the Earth's Semidiameter would appear to a Spectator in the Comet, which is bigger when near, and vanishes when far distant. Now a Comet just before it disappears, goes so slowly, that it scarce seems to move, and it may be twice observ'd in this manner. First, when it is very high above the Horizon, take any two Stars, between which, the Comet lies in a right Line parallel to the Horizon, which by extending a Thread directly before the Stars may be easily tried afterwards, when

the Comet approaches near to the Horizon, by extending the Thread, we must again try, if it keeps in a right Line between the same two *Fixed Stars*. Now if there be any sensible Parallax, which depresses the Comet, it cannot be seen in the same right Line as before, and therefore if it keeps the same Position as to those Stars, it is a convincing Argument, that the Comet has no sensible Parallax, and must therefore be at a prodigious Distance from us.

These temporary Planets, like the Ordinary ones have a Change in their Motions arising from the Motion of the Earth, and for the same Reasons, appear sometimes Retrograde, sometimes direct, sometimes they move slower, and sometimes with a quicker Motion, and like our Earth, most of them have a dense and dark Atmosphere surrounding their Bodies, which weakens and blunts the Sun's Rays that fall upon them, but when it appears, the Kernel or Solid Body of the Comet, which when the Clouds are dispersed gives a splendid and brisk Light.

## XX. An easy Method of finding the Course of a COMET, by a Celestial Globe.

Let there be every Day observ'd 4 Stars, which are round the Comet, and let 'em be such as the Comet may be in the right Lines, which joyns the two opposite Stars, which may easily be found out by the means of a Thread placed before the Eye, and extended over against the Stars and Comet, then upon a Globe in which are mark't these 4 Stars in their proper Places, extend one Thread Diagonally thro' two opposite

opposite Stars, and another thro' the other two opposite Stars, where the Threads intersect, is the Place of the Comet, if this be daily done, and the Place of the Comet be every Day taken by this means we shall manifestly find out the Course a Comet takes in the Heavens, which will be found to be a great Circle, and having two Points of this Circle we shall find its Inclination to the Ecliptic, and the Places of the Nodes, for it is only observing where a Thread stretch'd thro' the two Points cuts the Ecliptic.

Altho' all the Planets have their proper Motions from West to East, yet many Comets have been observ'd to hold on in a contrary Course from East to West as aforesaid, with a very great Degree of Velocity, such was the Course of the Comet, which Regiomontanus observ'd, in 1472, that described 40 Degrees of a great Circle in one Day. Hence we can positively conclude, that there are no Vortices in the Heavens, else when the Comets enter within the Planetary Regions, they must necessarily be driven out of their Course, by the Rapidity of the Solar Vortex, as by a mighty Torrent, which near the Earth, is of such Force, that it carries it above 2000 Miles in an Hour, and who can think that so Rapid a Stream, were there any, would not affect the Comets, and, when they have a Motion contrary to its Motion, soon destroy it.

## XXI. Of the Tails of the COMETS.

The Tails of Comets grow bigger, as they descend to the Sun, and at the *Perihelions* they are biggest and as they go further off from the Sun, and cool by Degrees, the Tail lessens, till at last it is contracted within the Comet's Atmosphere.

The

222 Of the Tails of the COMETS.

The great Comet, which appeared in the Year 1680 after its Departure from its *Peribelion*, projected such a Tail as extended it self more than 40 Degrees in the Heavens, nor can this be a Wonder, for it was so near the Sun that its Distance from its Surface at the *Peribelion*, was but  $\frac{1}{4}$  Part of the Diameter of the Sun's Body, and therefore the Sun seen from the Body of the Comet would appear to fill the greatest part of Heaven, and its apparent Diameter could not be less than 120 Degrees.

CONCERNING the  
FIXED STARS.

SECT. XXII.

1. **T**H E *Fixed Stars* are those bright and shining Bodies, which in a clear Night appear to us every where dispersed through the boundless Regions of Space. They are term'd *fixed*, because they are found to keep the same immutable Distance one from another in all Ages, without having any of the Motions observ'd in the Planets. The *fixed Stars* are all placed at such immense Distances from us, that the best of Telescopes represent them no bigger than Points without having any apparent Diameters.

*The fixed  
Stars are at  
immense  
Distances  
from us.*

*The fixed  
Stars are lu-  
minous Bo-  
dies, like the  
Sun.*

2. It is evident from hence, that all the Stars are luminous Bodies, and shine with their own proper and native Light, else they could not be seen at such a great Distance. For the Satellites of Jupiter and Saturn, tho' they appear under considerable Angles through good Telescopes, yet are altogether invisible to the naked Eye.

3. Although

3. Although the Distance betwixt us and the Sun is vastly large, when compared to the Diameter of the Earth, yet it is nothing when compared with the prodigious Distance of the fixed Stars; for the whole Diameter of the Earth's Annual Orbit appears from the nearest fixed Star no bigger than a Point, and the fixed Stars are at least 100,000 Times farther from us, than we are from the Sun; as may be demonstrated from the Observations of those who have endeavoured to find the Parallax of the Earth's Annual Orb, or the Angle under which the Earth's Orbit appears from the fixed Stars.

The Distance from us to the Sun is nothing in comparison of the vast Distance of the fixed Stars.

4. Hence it follows, that tho' we approach nearer to some fixed Stars at one time of the Year, than we do at the opposite, and that by the whole Length of the Diameter of the Earth's Orbit; yet this Distance being so small in comparison with the Distance of the fixed Stars, their Magnitudes or Positions cannot thereby be sensibly altered. Therefore we may always, without Error, suppose ourselves to be in the same Center of the Heavens, since we always have the same visible Prospect of the Stars without any Alteration.

As to appearance, the Earth may be considered as being in the Center of the Heavens.

5. If a Spectator was placed as near to any fixed Star, as we are to the Sun, he would there observe a Body as big, and every way like, as the Sun appears to us; and our Sun would appear to him no bigger than a fixed Star: and undoubtedly he would reckon the Sun as one of them in numbering the Stars. Wherefore

The fixed Stars are Suns.

since

since the Sun differeth nothing from a fixed Star, the fixed Stars may be reckoned so many Suns.

*The fixed Stars  
are at vast Di-  
stance from  
each other.*

6. It is not reasonable to suppose that all the fixed Stars are placed at the same Distance from us; but it is more probable that they are every where interspersed thro' the vast indefinite Space of the Universe; and that there may be as great a Distance betwixt any two of them, as there is betwixt our Sun and the nearest fixed Star. Hence it follows, why they appear to us of different Magnitudes, not because they really are so, but because they are at different Distances from us; those that are nearest, excelling in Brightness and Lustre those that are more remote, who give a faint Light, and appear smaller to the Eye.

*The Distribu-  
tion of the  
Stars into fix  
Classes.*

7. The Astronomers distribute the Stars into several Orders or Classes; those that are nearest to us, and appear brightest to the Eye, are called Stars of the first Magnitude; those that are nearest to them in Brightness and Lustre, are called Stars of the second Magnitude; those of the third Class, are called Stars of the third Magnitude; and so on, until we come to the Star of the sixt<sup>h</sup> Magnitude, which are the smallest that can be discerned by the naked Eye. There are infinite numbers of smaller Stars, that can be seen through Telescopes; but these are not reduced to any of the six Orders, and are only called *Telescopical Stars*. It may be here observed, that tho' the Astronomers have reduced all the Stars that are visible to the naked Eye, into some one or other of these Classes; yet we are not to conclude from thence that all the Stars answer exactly to some or other of these Orders; but there

may be in reality as many Orders of the Stars, as they are in Number, few of them appearing exactly of the same Bigness and Lustre.

8. The antient Astronomers, that they might distinguish the Stars, in regard to their Situation and Position to each other, divided the whole starry Firmament into several *Asterisms*, or Systems of Stars, consisting of those that are near to one another. These *Asterisms* are called *Constellations*, and are digested into the Forms of some Animals, as Men, Lions, Bears, Serpents, &c. or the Images of some known things, as of a Crown, a Harp, a Triangle, &c.

*The Stars digested into Constellations*

9. The Starry Firmament was divided by the Ancients into 48 Images or Constellations; twelve of which they placed in that part of the Heavens, where are the Planes of the Planetary Orbits; which part is called the *Zodiac*, because *Zodiac*. most of the Constellations placed therein resemble some living Creature. The two Regions of the Heavens that are on each side of the *Zodiac*, are called the *North* and *South* Parts of the Heavens.

10. Some of the principal Stars have particular Names given them, as *Syrius*, *Arcturus*, &c. There are also several Stars that are not reduced in Constellations, and these are called *Unformed Stars*.

*Unformed Stars.*

11. Besides the Stars visible to the naked Eye, there is a very remarkable Space in the Heavens, called the *Galaxy*, or *Milky Way*. This is a broad Circle of a whitish Hue,

*The Galaxy or Milky Way.*

like

G g

like Milk, going quite round the whole Heavens, and consisting of an infinite Number of small Stars, visible thro' a Telescope, tho' not discernible by the naked Eye, by reason of their exceeding Faintness; yet with their Light they combine to illustrate that part of the Heavens where they are, and to cause that shining Whiteness.

12. The Places of the Fixed Stars, or their relative Situations one from another, have been carefully observed by Astronomers, and digested into Catalogues. The first among the Greeks, who reduced the Stars into a Catalogue, was *Hipparchus*, who, from his own Observations, and of those who lived before him, inserted 1022 Stars into his Catalogue, about 120 Years before the Christian *Era* as aforesaid: This Catalogue has been since enlarged and improved, by several learned Men, to the Number of 3000; of which there are a great many Telescopical, and not to be discerned by the naked Eye; and these are all marked in the Catalogue, as Stars of the seventh Magnitude.

13. It may seem strange to some, that there are no more than this Number of Stars visible to the naked Eye; for sometimes in a clear Night, they seem to be innumerable. But this is only a Deception of our Sight, arising from their vehement sparkling, while we look upon them confusedly, without reducing them into any Order; for there can seldom be seen above 1000 Stars in the whole Heaven with the naked Eye at the same Time; and if we should distinctly view them, we shall not find one, but what is inserted upon a good *Cæleftial Globe*.

14. Altho'

14. Altho' the Number of Stars that can be discerned by the naked Eye, are so few, yet it is probable there are many more which are beyond the reach of our Optics; for thro' Telescopes they appear in vast Multitudes, every where dispersed throughout the whole Heavens; and the better our Glasses are, the more of them we still discover. The ingenious Dr. Hook has observed 78 Stars in the *Pleiades*, of which the naked Eye is never able to discern above 7; and in *Orion*, which has but 80 Stars in the *British Catalogue*, (and some of them Telescopical) there have been numbered 2000 Stars.

### XXIII. *The Principal Phænomena of the Motions of the Fixed Stars, with some brief Solutions.*

1. All the Stars as well the Fixed, as Erratic, with the whole Furniture of the Heavens, do rise and set every Day, or appear to revolve from *East* to *West*, in a Circular Motion, which is perform'd about the Axis of the World, and this along Line's nearly parallel to the Equinoctial.

For our Earth by turning about its own Axis, like the other Planets must needs present to our Senses this Phænomenon, without the least Circumvolution of the Heavens.

2. Besides this general apparent Motion, which is perform'd daily, the Fixed Stars seem to move a quite contrary Course, seeing they change, and increase their Longitude; for those Stars, which in the Time of *Hipparchus* were in the Beginning of *Aries* are now advanc'd into *Taurus* near  $\frac{1}{2}$  of the

228. *The Phænomena of Fixed Stars.*

Ecliptic about a Degree in 70 Years, and that with an even Velocity.

Now if the Equinoctial Point *Aries* be a Fixed Point, then in reality the Stars must move; but if said Point be moveable, it may be, then the Stars need not move from it, but the Point it self may go back from the Stars, which is certainly the more probable Case: and which the Moderns call the Precession of the Equinoctial Points, a like Parallel is in the Moon and other Secondary Planets; whose Nodes go backwards by Degrees towards the antecedent Signs, and Sir Isaac Newton has demonstrated *a priori*, that the Nodes of the Earth ought to go backwards 50 Seconds every Year. Hence this as well as the former Motion of the Fixed Stars, is not real, but apparent only.

3. Altho' the Fixed Stars perpetually change their Longitude from the Beginning of *Aries*, yet their Latitude or Distance from the Ecliptic, they doin no wise change being now the same, as in the Days of *Hipparchus*.

For if the Fixed Stars do rest, and the Plane of the Ecliptic remains unchang'd, the Precession of the Equinoxes is perform'd without any Change of the Annual Motion of the Earth, as to the Plane of the Ecliptic: 'Tis necessary that the Latitude of the Stars, or their Distance from the said Ecliptic should unto this Day remain unvaried.

Whilst the Poles of the World are moved about the Poles of the Ecliptic in *Antecedentia*, and pass successively thro' all the Points that are 23 Degrees, 29 Minutes, distant from these Poles, these Points themselves, or rather the Fixed Stars that are in them, come towards the Poles of the World successively, and seem to be carried in *Consequentia*, and to describe Circles, which are really described by the Poles of the World about the Poles of the Ecliptic, which being placed in Centers are alone at rest; because they keep the same Situation in respect to one another.

Therefore the whole Sphere of the Fixed Stars seems to move in *Consequemzia*, about an Axis passing thro' the Poles of the Ecliptic, and each Star apparently describes a Circle Parallel to the Ecliptic.

Ecliptic, by which Motion, the Latitude of the Stars is not hang'd.

The Plane of the Aequator makes a right Angle with the Axis of the Earth; therefore by the Motion of its Axis, the Inclination of the Plane of the Aequator, with the Plane of the Ecliptic is moved round, wherefore the Equinoctial Points, &c move thro' the whole Ecliptic Line, in the Space of about 25000 Years in Antecedentia, which Period is called the Great Year, or *Annus Platonicus*.

4. The Diameter of the Fixed Stars, as beheld thro' Telescopes are very small, and almost insensible: and the Stars themselves seem as so many Lucid Points.

This is manifest to such, who use the largest Telescopes, which cut off the adventitious Rays of the Fixed Stars, which appear to the naked Sight, and made the Antients suppose their diameter to be sensible, no less than  $\frac{1}{2}$  of a Minute, before the use of Telescopes.

5. The Fixed Stars do wholly want a Diurnal Parallax; but have a small Annual one.

For the Superior Planets want a Diurnal Parallax, and much more may the Fixed Stars, which are far beyond them. Doctor Hook, was the first that pretended to discover the Annual Parallax of the Fixed Stars; which Flamsteed fully confirmed by correcting his Numbers from the Comparison of 15 Sets of Observations made for Seven Years together, that the Polar Star hath a less Latitude about the Summer Solstice, than it hath about the Winter, by near  $\frac{1}{2}$  of a Minute, which is their Annual Parallax sought, precisely 47 Seconds, for the greatest of all, which is near 5 Times the Sun's Diurnal Parallax. Hence the Distance of the Fixed Stars will be found 9000 Semidiameters of the Annual Orbit, for as 47 Seconds to the whole Sine: so is the Diameter of the great Orb to the Distance of the fixed Stars. But in Observations of such small Angles less than a Minute, Errors are scarcely to be avoided, and what a prodigious Difference would Mistake of only 15 Seconds cause in this Computation, and who can be sure, he has not committed such an Error, and what Instrument is nice enough, to be sure to  $\frac{1}{2}$  of a Minute. See Plate VIII.

6. Thereo

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6. There is a Path in the Firmament of the Fixed Stars, which is much brighter than the rest of Heaven, and is therefore call'd the *Milky Way*, 'tis extended thro' a considerable Part of Heaven, in the Form of a Circle of some Breadth,

The Telescope helps us to solve this, by discerning a Multitude of little Stars, which escape the Sight of the naked Eye, whose close and confus'd Reflection of their Rays cause that Color.

7. The Number of the Fixed Stars, which may be observ'd by the naked Eye, is much under 2000; but by the Help of the Telescopes they are found to be 10 or 20 Times so many, and always by how much the more exquisite our Telescopes are, by so much the greater Number of Stars may be discover'd: So that it is much to be question'd, whether ever we shall obtain a certain, and fixed Number of them.

8. The Light of the Fixed Stars is more Strong and Lively by far, than that of the Planets, altho their apparent Diameters be far less.

Because the Fixed Stars, those Glorious Suns at an indefinite Distance shine with their own native, and not with a borrow'd Light, such as is that of the Planets and Comets, which are Opake Bodies, wholly destitute of Light in themselves, and shine only by the Reflection of the Light of the Sun. For if the Fixed Stars as before computed be 9000 Semidiameters off the Annual Orbit: the Quantity of the Sun's Light on them would be but 81,000.000th Part of that Light of the Sun, which is with us. What will it be then, when 'tis reflected from them to us, in which it must undergo a like Decrease as before, and in Reality become insensible.

9. The Fixed Stars seem to twinkle and sparkle much more than the Planets.

This may be owing to our Atmosphere, and the small Atoms or Corpuscles, which float up and down in the Air, for the higher a Star rises above it, the Twinkling grows less, and why the Planets do not, is because their Diameter are of that sufficient Magnitude, that altho' some part of them be intercepted from our Sight, by the Vapours interposing; yet the rest of the Orb remains to be seen clearly without Interruption; but the Orbs of the fixed Stars are so small, and their Rays so strong and lively, that the least Particle of Vapors do ever and anon disturb, and break off their Rays.

10. The Fixed Stars seem to be disposed in the Heavens in no certain Order, but as it were by chance only.

There may be a certain orderly, and harmonious Disposition of the Fixed Stars amongst themselves, when they are beheld from some other proper Place, altho' that Order appears not, when they are seen from this Earth. 'Tis but meet and just, that from the excellent Order of all the nearer Bodies, which we may, and do see, we should conclude, that the same holds so in some sort or other in those remoter ones, tho' our Distance from them, renders us incapable at present of discerning the same.

Thus we would Judge of an Army of orderly well disciplin'd soldiers at a Distance, which would appear to us in a confused manner, until we came near, and had a regular Prospect of them, which we should then find to stand well in Rank and file, so doubtless of the Stars.

11. Certain wonderful Things are observ'd about the Systems of the Fixed Stars. New Stars are sometimes seen, and presently disappear, the same Stars are observ'd to change their Magnitude, or their splendor by turns, as shining sometimes with a duller, sometimes with a more vivid Light. Lastly, the great *Huygens* observ'd a certain Space in *Orions* word, much brighter than all the rest of Heaven; which notwithstanding appear'd not to have any notable

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notable Stars in it more than usual ; but seemed as it were to have a Gap in that Place, thro' which it yielded a Prospect into a more lucid Region.

'Twas the Appearance of a New Star made Hipparchus first at all set about compiling a Catalogue of them, since which many have been observ'd by Tycho, Kepler, Hevelius, Bullialdus, Cuff, Boyer, Montanar, and others, as aforesaid.

That in the Neck of the *Whale* appears and disappears by Turns and is found to perform its Revolution in 330 Days; and several other Stars observ'd by Caffini and others, which cannot be accounted for, but by supposing them Planets revolving about some Star or Sun.

'Tis our Lot to be born on a Planet near a Fixed Star call'd a Sun, and had we been born on a Planet belonging to another Fixed Star, we should have taken that for our Sun, and counted our selves also in the Center of the Universe, and look'd on the Sun we have now as a Star of the first or second Magnitude according to its Distance : and this Earth might have appeared sometimes to us, as probably *Saturn*, *Jupiter*, *Mars*, and *Venus* do appear to the Inhabitants in other Planetary Systems, when they are at their nearest Distance.

**XXIV. Having the SUN's Place,  
and a good Pendulum Clock, to find the  
Right Ascensions of all the STARS.**

First, Adjust the Clock, so as to run thro' the 24 Hours in the Space a Star leaves the Meridian, till it arrive at it again, which Time is somewhat shorter than the Natural Day; because of the Space, the Sun seems to move thro' in the same Time Eastward.

Then when the Sun is in the Meridian, fix the Hand to the Point, from whence we are to begin to reckon our Time, and then observe when the Star comes to the Meridian, and mark the Hour and Minute the Hand shows, which turn into Degrees, and Minutes of the Æquator will give the Difference between the Right Ascension of the Sun and Stars, which Difference added to the Right Ascension of the Sun will give the Right Ascension of the Star.

Now if we know the Right Ascension of any one Star, we may from it find the Right Ascension of all others, which we see: by marking the Time by the Clock between the Arrival of the Star, whose Right Ascension we knew to the Meridian, and another Star, whose Ascension is to be found, the Time converted into Degrees and Minutes of the Æquator will give the Difference of Right Ascensions, from whence by *Addition*, we collect the Right Ascensions of the Star, which was to be found out.

# CONCLUSION CONTAINING

*Some moral Reflections and Inferences, drawn from  
the aforesaid Discoveries.*

## S E C T. XXV.

*An Idea of the Universe.* **T**Hose who think that all these glorious Bodies were created for no other purpose, than to give us a little dim Light, must entertain a very slender Idea of the Divine Wisdom; for we receive more Light from the Moon it self, than from all the Stars put together. And since the Planets are subject to the same Laws of Motion with our Earth, and some of them not only equal, but vastly exceed it in Magnitude, it is not unfeasable to suppose, that they are all habitable Worlds. And since the Fixed Stars are no ways behind our Sun, either in Bigness or Lustre; is it not probable, that each of them have a System of Planetary Worlds turning round them, as we do round our Sun. And if we ascend as far as the smallest Star we can see, shall we not then discover innumerable more of these glorious Bodies, which now are altogether invisible to us? and so *ad infinitum*, thro the boundless Space of the Universe. What a magnificent Idea must this raise in us of the Divine Being! Who is every where, and at all Times present, displaying his Divine Power, Wisdom and Goodness amongst all his Creatures!

As the Distance from us to the Moon is little in comparison of our Distance from the Sun, so the Distance of the Sun from us is little in respect of the Distance of the Fixed Stars from us: in comparison of which Suns our whole Earth being no more Proportion than a Pin-head to a large Globe. Let then the proud Man consider, and observe how little the whole Earth is in comparison of the Heavens, and how small a Dominion he has, were he Lord of that, whereas what he commands is not in comparison, so much as an *Ant-Hill*, nor himself any other, but even as an *Emmet* crawling upon it, and Subject

Subject upon every Accident to be squash'd to Dirt; surely this Consideration will cause him to humble himself under the mighty Hand of God, and not to despise the meanest of his Fellow-Creatures.

Hence we may learn not to overvalue this World, nor to set our Hearts too much upon it, or upon any of its Riches, Honours or Pleasures, for what is all our Globe; but a Point a Trifle, to the Universe, a Ball not so much as visible among the greatest Part of the Heavens, namely the Fixed Stars.

Is this that Point, which by Fire and Sword is divided among so many Nations? O! how Ridiculous are the Bounds and Pursuits of Ambitious Mortals.

An Emperor indeed may look Big, if he compare himself with a Centinel, and so may he if compared with a Peasant, and a Peasant if compared with Brutes, and they if compared with Insects; but the Emperor compared with him, that made the Sun; that rides on the Chariot of the Wind, and hath the Clouds for the Dust of his Feet, who measures the Heavens, as with a Span, and upholds the Pillars of the Earth: he disappears or is next to Nothing, scarce a Ray of that incomprehensible Divinity, whose Glory fills the Heavens, and Heaven of Heavens cannot contain, whom Million of Angels, with Unity and Harmony adore.

And seeing we have little Light, and as little Heat from the Fixed Stars: 'Tis hard to conceive what so many great Bodies should be made for; if not to give Light and Heat to the inhabitants of the Planets about them, which infinitely magnifies the Power of the Supreme Being.

They seem to have a too narrow and contracted View, that confine Mankind to this Earth, its highly probable, the Almighty hath Millions, that Worship him on other Planets, perhaps more pure and perfect than we are, and tho' the greater part of Men on this Earth were miserable, which some know not how to reconcile with the Divine Goodness; yet their Number compared with those that are Happy in other Parts of the Creation may be but as one to 10,000. who, it may be said, do all possess Heaven on Earthly Planets.

There are likewise 10,000 Things both in the Microcosm of our Bodies, and the Macrocosm of the Heavens and Earth, the Knowledge whereof hath been reserv'd for the latter Times, which calls for a due Improvement from us, and should teach us, that he is a GOD of infinite Knowledge, for sure He that formed our Body understands *Anatomy*, and He that made the Heavens, understands *Astronomy*, and He that made the Eye, understands *Optics*, and He that makes the Herbs to grow, understands *Botany*, &c. that is in short, *Known unto GOD are all his Works from the Beginning*, and they to whom he communicates the greatest Measures of Knowledge are accountable for their Improvement.

A Train of such immense, and numberless Bodies, what less than an Almighty Hand could find Matter sufficient for? and then compose such magnificent Works, which by infinite Wisdom, are set at such due Distances from one another, as not to interfere, clash with, or disorder one another. Nay so great is their Distance, so convenient their Situation; that they do not so much as Eclipse one another, except Secondary Planets.

In the Heavens we have an admirable Oeconomy, observable throughout all the visible Regions of the Universe in the mutual Assists, and Returns, which one Globe affords the other, thus as the Moon gives us Light, we repay the same with one many Times greater *&c.*

If the great Creator, and Contriver of the Universe, hath thus Model'd and Methodized this part, this System of it, where we live, and behold the Order thereof, no great doubt can be made, but the same infinite Wisdom hath done the like in the other Systems: also that every System is set at a due Distance from one another, and every Body in each System at its due Distance from their Sun or Fixed Star.

In the Planets revolving about their Axes, we may consider, and find that an infinitely Wise and Kind, as well as Omnipotent Being, was the Orderer thereof, for were these Globes always to stand Still, which owe both their Light and Heat to the Sun, in this Case, one Half of each would be dazled and parch'd with everlasting Day, whilst the other would be involv'd in everlasting Night and Darkness, and so agree to the State of no Animal or Vegetable.

As GOD's Works are manifest Demonstrations of his Existence, so they are no less of his Perfections: particularly of his infinite Power, Wisdom and Goodness. As every Workman is known by his Works, so the Heavens this Glorious Scene of GOD's Works, plainly demonstrate the Eternal Creators infinite Wisdom to contrive, his Omnipotency to make, and his immense Goodness, in being so indulgent to all Creatures, as to Order all his Works for their Good.

Thus the Learned Apostle *Paul* argues, *Rom. 1. 20.* “ The invisible Things of GOD are clearly seen from the Creation of the World, being understood by the Things that are made, even his Eternal Power and Godhead.

Of the same Faith was the Royal Psalmist long before, *Psa. 90. 2.* Before the Mountains were brought forth, “ or ever he had Formed the Earth or the World, even from everlasting to everlasting, He is GOD.

Hence we may infer, that there is a GOD, or Supreme Being, that this World has not been Eternal; but was Created by that Supreme Being, who is Eternal, and exercises a continual Providence over the Creatures he has made. that he is not a necessary, but a free Agent, that he is Intelligent and Omniscient, that he is an Allwise, and that he is an All powerful Being, that he is Omnipotent, Immortal and Immutable, that he is Good or Beneficent, that he is a Spiritual, Living, and active Being, that he is but One, and that he is therefore the alone Supreme Lord and Governor of the whole Universe.

O Lord how manifold are thy Works, in Wisdom hast thou made them all. *Psalm 104. 28.*

*Etiamsi omnia a Veteribus inventa sint, tamen erit hoc semper novum, Usus & Diffusio inventorum ab aliis.* Seneca, Ep. 64.



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